

LIMIT STATE DESIGN OF R.C. BRIDGE SUPERSTRUCTURE

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DEPARTMENT OF CIVIL ENGINEERING

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LIMIT STATE DESIGN OF R.C. BRIDGE SUPERSTRUCTURE

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Master of Technology Civil Engineering
(Computer Aided Structural Analysis and Design)

By

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08MCL010



DEPARTMENT OF CIVIL ENGINEERING

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Declaration

This is to certify that

- i) The thesis comprises my original work towards the degree of Master of Technology in Computer Aided Structural Analysis and Design at Nirma University and has not been submitted elsewhere for a degree.
- ii) Due acknowledgement has been made in the text to all other material used.

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Certificate

This is to certify that the Major Project entitled “Limit State Design of R.C. Bridge Superstructure ”submitted by Sweta Ojha (08MCL010), towards the partial fulfillment of the requirements for the degree of Master of Technology in Civil Engineering of Nirma University, Ahmedabad is the record of work carried out by her under my supervision and guidance. In my opinion, the submitted work has reached a level required for being accepted for examination. The results embodied in this major project, to the best of my knowledge, haven’t been submitted to any other university or institution for award of any degree or diploma.

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Abstract

Revolutionary changes have taken place in the practices and philosophies in bridge design during the last century. Yet many important factors were lost sight of the design because of inadequate knowledge and experience. This has adversely affected the durability and serviceability of the bridge and has resulted in their premature deterioration and other problems. The bridge designers are now becoming increasingly aware of many new factors and dimensions in the designing of modern bridges. This is going to be great help in designing more beautiful and durable bridges which will be constructed with ease, efficiency and economy and which will remain in service for a very much longer period. There are many factors which affects bridge durability, which is both environmental conditions and design philosophy.

In present study, comparison of limit state design and load and resistance factored design is done. By taking an bridge superstructure data, which is analysed and designed by both methods. And are compared to obtain economical design. The main emphasis is given on limit state method design as per IS 456-2000 and and partial safety factors from IRC-6 amendments no.8, which covers limit state of collapse , limit state of cracking ,limit state of serviceability and partial safety factors. And load and resistance design is done using ASSTHO specifications.

By taking different depth for different span the economical L/D ratio is obtained. Quantity and rate analysis is done to obtain the total economic cost of bridge superstructure. The bridge superstructure is designed by both the methods and compared with working stress design method to find most efficient design philosophy.

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Abbreviation Notation and Nomenclature

A_{st}	Area of Steel in tension
A_{sc}	Area of Steel in compression
A_{sf}	Area of steel in flange
a_{cs}	Deflection due to shrinkage
a_{cr}	distance from the point under consideration to the nearest surface
b_f	Effective width of flange
b_w	Width of web
d', d_c	Effective cover
D_f, h_f	Depth of flange
D	Total depth of section
x_u, a, x	Depth of neutral axis
E_c	Modulus of elasticity of concrete
E_s	Modulus of elasticity of steel
E_{ce}	Modulus of elasticity of concrete
f_{ck}	Characteristic compressive strength of concrete
f_y	Yield stress of the material
I_{eff}	Effective moment of flanged section
I_{gr}	Moment of inertia of gross-section(uncracked section)
I_r	Moment of inertia of gross-section ignoring reinforcement (cracked section)
M_r	Moment of resistance
v_u	Factored shear force
M_u	Factored moment
d	Effective depth of section
τ_{uc}	Permissible shear stress in concrete
V_{uc}	Shear strength of concrete
V_{us}	Shear strength of steel
m	modular ratio

z, j, d_v	Lever arm distance
W_{cr}	Crack width of surface
ϵ_m	Average steel strain at level cracking considered
ϵ_1	Strain at considered level
Z	Crack parameter
v, τ	Nominal shear
ϕ_v	Resistance factor
M_{cr}	Moment of resistance
$D.L.$	Dead load of permanent component
$W.C.L$	Wearing coat load
$L.L$	Live load of vehicle
γ	Partial safety factor
θ	Creep coefficient
$\Delta_{D.L}$	Deflection due to dead load
$\Delta_{L.L}$	Deflection due to live load

Contents

Declaration	iii
Certificate	iv
Abstract	v
Acknowledgements	vi
Abbreviations Notations and Nomenclatures	vii
List of Tables	xii
List of Figures	xiv
1 Introduction	1
1.1 General	1
1.2 Design Philosophy	1
1.2.1 Working Stress Design Method	2
1.2.2 Limit State Design Method	4
1.2.3 Load and resistance factored design	7
1.2.4 Characteristic Strength of Materials	8
1.2.5 Characteristic Load	8
1.2.6 Partial Safety Factors and Design Load	8
1.3 Objective of Study	9
1.4 Scope of Work	9
1.5 Thesis Organization	10
2 Literature Review	12
2.1 General	12
2.2 Literature Review	12
3 Comparison of Design Methods	15
3.1 General	15
3.2 Limit State Design as per IS456:2000	15

3.2.1	Introduction	15
3.2.2	Partial safety factor	16
3.2.3	Stress block	16
3.2.4	Limit state of collapse-flexure	18
3.2.5	Limit state of collapse- shear	19
3.2.6	Limit state of serviceability	20
3.2.7	Limit State of Deflection	20
3.2.8	Limit State Cracking	22
3.3	Load and resistance factor design as per AASHTO specification	23
3.3.1	Partial safety factors	25
3.3.2	Stress block	25
3.3.3	LRFD - Flexure Limit State	26
3.3.4	LRFD-Shear Limit State	27
3.3.5	LRFD-Service Limit State	28
3.3.6	Deformation	28
4	Bridge Superstructure Analysis	30
4.1	General	30
4.2	Structural Data	30
4.3	IRC Loading	32
4.4	Slab Analysis	33
4.4.1	Cantilever slab:	33
4.4.2	Continuous slab	35
4.5	Diaphragm Analysis	38
4.5.1	Internal diaphragm	38
4.5.2	External diaphragm	39
4.6	Girder Analysis	41
4.6.1	Courbon's method:	41
4.6.2	SAP 2000:	42
4.6.3	Live load position	43
4.6.4	Girder Force	45
4.7	Summary	51
5	Bridge Superstructure Design	52
5.1	General	52
5.1.1	Problem Formulation	52
5.2	Limit State Design Method	53
5.2.1	Cantilever Slab Design	53
5.2.2	Continous Slab panel design	58
5.2.3	Diaphragm design	63
5.2.4	External girder	69
5.2.5	Internal girder	76

5.3	Load and resistance factor design	83
5.3.1	Cantilever Slab Design	83
5.3.2	Continous Slab panel design	85
5.3.3	Diaphragm design	88
5.3.4	External girder	91
5.3.5	Internal girder	97
5.4	Summary	103
6	Estimation of Quantity and cost	104
6.1	General	104
6.2	Quantity analysis	104
6.2.1	Estimation of concrete and wearing coat quantity	105
6.2.2	Estimation of steel quantity	105
6.2.3	Rate analysis	105
6.2.4	Total cost	106
6.2.5	Summary	106
7	Parametric Study	107
7.1	General	107
7.2	Section at various depth	107
7.3	Results	108
7.4	Results of costing	112
7.5	Total cost comparision of design method	116
7.6	Summary	117
8	Summary and Conclusion	119
8.1	Summary	119
8.2	Conclusion	120
8.3	Future Scope	120
A	Detailing sheet	122
B	Paper communicated	123
	References	124
	Index	124

List of Tables

3.1	Partial safety factors(IS-456:2000)	16
3.2	Partial safety factors(AASTHO)	25
3.3	Crack width parameter	29
4.1	Cantilever Slab Dead Load Moment	33
4.2	Slab bending moment and shear force	37
4.3	Diaphragm bending moment and shear force	41
4.4	Comparison of bending moment	45
4.5	Comparison of shear force	45
4.6	Unfactored moment and forces on external girder(SAP2000)	46
4.7	Unfactored moment and forces on internal girder (SAP2000)	46
4.8	Factored moment and forces on external girder for LSD	46
4.9	Factored moment and forces on internal girder for LSD	48
4.10	Factored moment and forces on external girder for LRFD	48
4.11	Factored moment and forces on internal girder for LRFD	48
5.1	Longitudinal reinforcement at 0.5L external girder	71
5.2	Longitudinal reinforcement at 0.25L external girder	74
5.3	Shear reinforcement of external girder	74
5.4	Deflection check for external girder	76
5.5	Crack check for external girder	77
5.6	Longitudinal reinforcement at 0.5L internal girder	79
5.7	Longitudinal reinforcement at 0.25L internal girder	81
5.8	Shear reinforcement of internal girder	81
5.9	Deflection check for external girder	83
5.10	Crack check for internal girder	83
5.11	Longitudinal reinforcement at 0.5L external girder	94
5.12	Longitudinal reinforcement at 0.5L internal girder	100
5.13	Flexure and collapse summary	103
5.14	Serviceability summary	103
6.1	Concrete and wearing coat quantity	105
7.1	Maximum bending moment in girder	109

7.2	Maximum shear force in girder	110
7.3	Variation of total cost of material for 15m span with varous L/D ratio	113
7.4	Variation of total cost of material for 20m span with varous L/D ratio	114
7.5	Variation of total cost of material for 25m span with varous L/D ratio	115
7.6	Total cost of 15m, 20m and 25m span	116
7.7	Total cost of comparision of WSD,LSD and LRFD	117

List of Figures

1.1	Stress-Strain Diagram For (a) Concrete Strength In Compression And (a) Steel Strength In Tension	3
3.1	Neutral Axis Lies In Flange Stress Diagram LSD	16
3.2	Neutral Axis Lies In Web Stress Diagram LSD	17
3.3	Parabolic part of stress-block inside flange (LSD)	17
3.4	Parabolic part of stress-block lying outside flange (LSD)	17
3.5	Neutral axis inside flange LRFD	25
3.6	Neutral axis outside flange LRFD	26
4.1	Cross Section of Bridge Deck Slab	30
4.2	Longitudinal Bridge Cross Section	31
4.3	Class A Wheeled Vehicle	32
4.4	Class 70R Tracked Vehicle	32
4.5	Class 70R Wheeled Vehicle	32
4.6	Cantilever Slab	33
4.7	Class A Heaviest Wheel Near To Minimum Distance from Kerb	34
4.8	Concentrated Load on the Slab Panel	36
4.9	Dead Load On Cross Girder	39
4.10	Position of Vehicle for Maximum B.M in Cross Girder	40
4.11	Position of Live Load for Maximum Moment in Girder 'A'	42
4.12	SAP2000 Bridge Model	43
4.13	Class-70R At Minimum Distance From Kerb For External Girder	43
4.14	Position of Class-70R Vehicle For Max. Bending Moment	44
4.15	Position of Class-70r Vehicle for Max. Shear Force	44
4.16	IRC Class-70R Vehicle on Moving Bridge Deck	44
4.17	Variation in B.M of various load along longitudinal span	47
4.18	Variation in S.F of various load along longitudinal span	47
4.19	Factored bending moment on external girder	49
4.20	Factored bending moment on internal girder	49
4.21	Factored shear force on external girder	50
4.22	Factored shear force on internal girder	50
5.1	Cross Section of Bridge Deck Slab	52

5.2	Cracked section of cantilever slab	57
5.3	Cracked section of continuous slab panel	62
5.4	Cracked section of internal diaphragm	65
5.5	Sectional properties of external girder	70
5.6	Sectional properties of internal girder	72
5.7	Centroidal distance from bottom of I-section	75
5.8	Sectional properties of internal girder	77
5.9	Sectional properties of internal girder	80
5.10	Sectional properties of external girder	92
5.11	Sectional properties of internal girder	97
7.1	Cross Section of Bridge Deck Slab	108
7.2	Bending moment variation in external girder along various L/D ratio	109
7.3	Bending moment variation in internal girder along various L/D ratio	110
7.4	Shear force variation in external girder along various L/D ratio . . .	111
7.5	Shear force variation in internal girder along various L/D ratio . . .	111
7.6	Variation of total cost of material for 15m span with various L/D ratio	113
7.7	Variation of total cost of material for 20m span with various L/D ratio	114
7.8	Variation of total cost of material for 25m span with various L/D ratio	115
7.9	Total cost of material for 15m,20m and 25m span with various L/D ratio	116
7.10	Total cost of material for 15m,20m and 25m span with various L/D ratio	117

Chapter 1

Introduction

1.1 General

Bridges are the links in roads, which close the discontinuity across any natural or manmade feature on the ground. Now a day due to requirement of speed of traffic, the requirement of Flyover Bridge, is also increased. Bridges are built spending large sums of money and are expected to remain in service for long period-50 to 100 year of even more. So, it should have a predetermined useful life. Its failure load should be sufficiently greater than the working load in order that the probability of its failure during its life-time is less than a specified limit and the required safety remains inbuilt. The cracking, vibrations and deflection of the bridge under working loads should not be so large as to impair its safety or serviceability during its life-time. The economic considerations with regard to its design, construction and maintenance. For doing so, methodologies like the elastic analyses, are in vogue currently, the limit state approach being the latest trend.

1.2 Design Philosophy

In bridge engineering, there are two principal methods of design in use today. The names used to define these design methods vary depending on the structural material

being used and the design codes being referenced, they are classified as:

- Working stress design
- Limit states design
- Load and resistance factored design

For most of the century, the working stress design approach was the standard by which bridges and other structural engineering projects were designed. It was Russians who set the ball rolling, as far as back as 1938 they chose to break away from working stress design though it continued to enjoy wide patronage in the rest of the world. The limit state design method was developed in the erstwhile USSR in the period 1947-49 and approved in 1955. The Russian Standard of reinforced concrete NITU 123-55 was re-elaborating in 1962 through SNIP II-B.1.62 and the design method was adopted by virtue of the recommendation COMECONN in the East Europe also, in 1963. In 1964, CEB brought out its first edition of a model code adopting semi-probabilistic limit state design method followed by the joint FIP/CEB second edition in 1970. The British Unified Code appeared in late 1972 has new limit state .So, the replacement of the traditional code format by the new one is almost the inevitable natural process like shedding of old clothes and taking on the new. Therefore, by 1970's limit states design began to gain acceptance by the general engineering community. In 1986, in order to overcome the disadvantages of limit state method LRFD method was adopted by Canada, America and other European countries.

1.2.1 Working Stress Design Method

Working stress design is an approach in which structural members are designed so that unit stresses do not exceed a predefined allowable stress. Factor of safety applied to the yield or ultimate stress to get permissible stress. Structure designed to support

working or service loads without exceeding the permissible stresses in concrete and steel. The allowable stress is defined by a limiting stress divided by a factor of safety.

The salient features are described below:

- a. Actual stresses are representative of stresses due to the service or working loads that a structure is suppose to carry. Figure 1.1(a) and (b) show stress-strain diagrams for concrete and steel respectively. The point where a material behaves elastically is defined as the proportional limit. Once stress and strain are no longer proportional, the material enters in plastic region. The working stress method is logically not applicable to concrete structures, because the range of proportionality is very small.

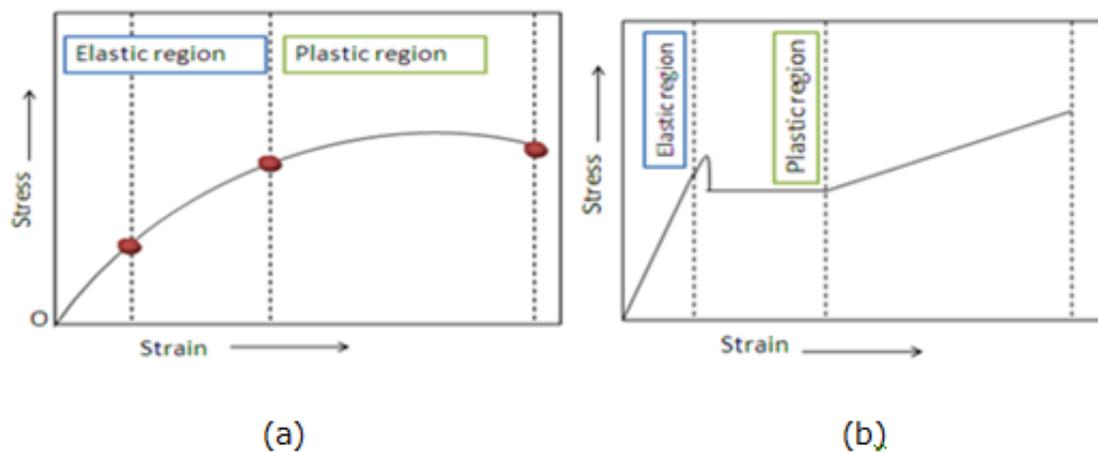


Figure 1.1: Stress-Strain Diagram For (a) Concrete Strength In Compression And (a) Steel Strength In Tension

- b. Due to non-linear stress-strain relationship modulus of elasticity also varies; therefore, constant value of modular ratio cannot be used.
- c. Factor of safety does not predict true margin of safety.

- d. Additional load carrying capacity in the plastic region is not taken in account.
- e. It considers ultimate stress as the limit of safety is a function of ultimate strain and ultimate stress.
- f. Since the structure is subjected to loads, the loads should form the failure criteria and not the stress.
- g. The effect of creep and shrinkage of concrete is totally ignored.
- h. Failure load computed by this method in majority of the cases is less than that obtained by experimental results at collapse.
- i. It is simple and reasonable reliable method.

1.2.2 Limit State Design Method

A limit state is a condition beyond which a bridge system or bridge component ceases to fulfill the function for which it is designed. The limit state design method was, in part, developed to address the drawbacks to the working stress approach mentioned above. This approach makes use of the plastic region for the design of structural members and incorporates load factors to take into account the inherent variability of loading. The quote from the AISC Manual of Steel Construction defines limit state as a condition representing "structural usefulness." The strength required is computed using conventional analysis methods and multiplying computed values by appropriate load factors. If we simply considering dead load times some factor plus live load times

the another factor. Specific values for factors are provided by the applicable design code.

Classification of Limit State

There are two broad categories of limit states, namely:

- Limit states of collapse (Ultimate Limit State)
- Limit states of serviceability

Limit State of Collapse

It is limit state on attainment of which the structure is likely to collapse. It relates to stability and ultimate strength of the structure. Design to limit state ensures safety of structure from collapse. The structural failure can be collapse of one or more member occurring (i.e. material failure, breakage due development of plastic hinge at critical section, bulking) as a result of force coming on the member exceeding its strength. And other condition (i.e. sliding, overturning, and sinking) is displacement of structure bodily due to lack of equilibrium between the external forces and resisting reaction. This limit state is attended to by providing resistance greater than the force coming on it and keeping a margin of safety factors.

Limit State of Serviceability

Limit states of serviceability related to performance or behavior of structure at working loads and are based on causes affecting serviceability of the structure. They mainly subdivided into following categories:

- (a) Limit states of deflection: Design to limit state safeguards the serviceability of the structure from adverse effect of excessive deflection which affects the shape of structure, creates feeling of lack of safety, poor drainage or ponding effect. The limit state is attended to by prescribing maximum allowable deflections or by prescribing maximum allowable span to depth ratios.

(b) Limit state of cracking: Design to this limit state safeguards the serviceability of the structure against damage due to excessive cracking. Due to cracking it creates exposed surface appearance which leads to corrosion of steel bar; reduces the imperviousness, strength and durability of the structure; creates lots of maintenance problems. Cracking is not dangerous directly but lead to ill effects. This limit state is attended to by imposing restrictions on maximum crack width for important structures and by adhering to appropriate detailing rules and restrictions on bar diameter, spacing, cover etc. for structures.

(c) Other limit states: Structures designed for special or unusual functions need considerations of appropriate limit state. They are vibration, fire resistance and durability.

The salient features of limit state are described below:

- a. It considers the actual behavior of the structure during the entire loading history up to collapse.
- b. It is adopts the concept of fitness of structure to serve the desired function during the service life span and defines the limiting state of fitness as the 'limit state'.
- c. It attempts to define quantitatively the margin of safety or fitness on some scientific mathematical foundations rather than on adhoc basis of experience and judgment.
- d. The method adopts the idea of probability of structure becoming unfit, and attempts to achieve the minimum acceptable probability of failure.

- e. The method is based on statistical probabilistic principle.

1.2.3 Load and resistance factored design

To overcome the deficiencies of limit state design, load and resistance factored design new approach. To account for the variability on both sides of the inequality in the equation, the resistance side is multiplied by a statistically based resistance factored ϕ , whose value is usually less than one, and the load side is multiplied by statistically based load factored γ , whose value is usually greater than one. Because the load effect at a particular limit state involves a combination of different types that have different degrees of predictability, the load effect is represented by the summation of values. If the nominal resistance is given by R_n , the safety criterion is

Equation involves both load factors and resistance factors, the design method is called load and resistance factor design. The resistance factored for a particular limit state must account for the uncertainties in material properties, equation that predicts strength, workmanship, quality control and consequence of a failure. The load factored chosen for a particular load type must consider the uncertainties magnitude of loads, arrangement of load and possible combinations of loads. In selecting resistance factors and load factors for bridges, probability theory has been applied to data on strength of materials, and statistics on weight of materials and vehicular loads.

The salient features are described below:

- a. Account for variability in both resistance and load.
- b. Achieves fairly uniform levels of safety for different limit states bridge types without involving probability or statistical analysis.
- c. Provides a rational and consistent method of design.

- d. Provides consistency with other design specification.

1.2.4 Characteristic Strength of Materials

The characteristic strength for all materials is defined as the value of the strength of concrete, and of the yield or proof-stress of reinforcement, below which not more than 5% of the test results may be expected to fall. The value therefore is

$$f_k = (f_m - 1.64s) \quad (1.1)$$

1.2.5 Characteristic Load

Characteristic load means that value of load which has a per 95% probability of not being of not exceeded during the life of the structure. Ideally this should be determined from mean load and its standard deviations from mean, using the same probability as for the materials that

$$F_k = (F_m + 1.64s) \quad (1.2)$$

1.2.6 Partial Safety Factors and Design Load

The safety of the structure depends on each of the two principal design factors, one for load and other, two different safety factors, one for load and the other for material strength are used instead of a single safety factor. Because each of the two safety factors contributed partially to safety, they termed as partial safety factors. Partial safety factor for load enhancing factor (greater than unity) which when multiplied to characteristic load gives a load known as design load for which the structure is to be designed. It takes into account unforeseen possible increase in load, accurate assessment of load effect, unexpected stress redistribution and variation in dimensional

accuracy. Thus, it makes provision for margin of safety.

1.3 Objective of Study

- a. To study the limit state method of design for R.C.C highway (flyover) bridge superstructure.
- b. To study the load and resistance factored design of R.C.C highway (flyover) bridge superstructure.
- c. To analyze and design bridge superstructure under IRC–6 loading.
- d. To carry out the cost analysis for highway superstructure design as per limit state method and load and resistance factored design.
- e. To carry out parametric study of bridge superstructure at different depth for different span for the economical section.

1.4 Scope of Work

- a. Study of design philosophy i.e. working stress, limit state method and load and resistance factored design.
- b. Analysis of superstructure is carried out on SAP2000–12 civil software and design is done using excel worksheet.
- c. Two Lane Bridge with three I-shaped girders considered for analysis and design.
- d. For analysis live load is considered are Class–70R tracked/wheeled and Class–A wheeled as per IRC: 6–1966.
- e. For design of superstructure is done by using following codes: i) Limit state method: Using IRC–6 draft code and IS–456:2000

- ii) Load and resistance factored design: Using AASTHO specification
- f. Comparison of cost for design method for limit state , load and resistance factored design and working stress method.
- g. Parametric study for the economical depth of bridge superstructure of limit state design approach.

1.5 Thesis Organization

The rest of the thesis is organized as follows.

Chapter 1, *Introduction*, deal with the basic introduction of working stress and limit state design. And also includes the objective and scope of work.

Chapter 2, *Literature Review*, shows review of various books and papers describing design philosophy of R.C.C bridge structure, classification of design methods and construction aspects.

Chapter 3, *Comparison of Design Methods*, describes the comparison of both methods working stress and limit state design and behavior of beam with various useful formula.

chapter 4, *Bridge Superstructure Analysis*, shows the analysis of bridge superstructure by calculating dead load and live load by doing manual calculation and using software SAP2000.

Chapter 5, *Bridge Superstructure Design*, describes the design steps required for working stress and limit state method.

Chapter 6, *Estimation of Quantity and cost*, includes estimation of concrete and steel for deck slab, girders and wearing coat with cost.

Chapter 7, *Parametric Study*, Chapter 8 Includes the parametric study for 15m, 20m and 25m span at depth 1.1m, 1.5m and 1.9m gives various L/D ratio to find out the economical L/D ratio. Cost comparison between LSD design and LRFD design. In this parametric study trials are taken at different depths.

Finally, in **chapter 8** concluding remarks and scope for future work is presented.

Chapter 2

Literature Review

2.1 General

Bridges are engineering works that affords passage to pedestrians, animals, vehicles, waterways and services above obstacles or between two points at a height above the ground. And by improving design philosophy of bridge structure we can achieves the safety, serviceability and economy. Literature survey is carried out to review various criteria which are to be considered for the analysis and design for bridge structure. Here various books and papers describing design philosophy of R.C.C bridge structure, classification of design methods and construction aspects are studied.

2.2 Literature Review

Mr.Joglekar [1]paper highlights the necessity and urgency of preparing new generation, rationalization codes for bridge in India, in line with international standards. This paper focus on concept of safety and reliability, provision of sound design philosophy i.e. limit state method which is needed to be improved in existing bridge code in Indian.

Dr.V.K.Raina [2] paper gives the bridge design education and rational approach to structural design of bridge. This paper clears the reason to adopt new design

philosophy in the new code practice and split load factors.

Demetrios E. Tonias [3] intended to serve an overview of the bridge engineering process from the origin of a bridge project through his book “Design, Rehabilitation and Maintenance of Modern Highway Bridge”. This book provides theoretical aspects of design philosophy and bridge design.

Krishna N. Raju [4] describes theory and design of various types of bridge in his book “Design of Bridge”. This book is useful in solving continuous R.C.C slab bridge design by using working stress method as per the codes of the Indian Roads Congress. And shows detailed working drawing of reinforcement, plan, elevation and cross section.

D.J. Victor [5] describes theory and design of various bridge components in his book “Essentials of bridge Engineering”. This book deal with the design of R.C.C bridge having T-shaped girder under IRC loading with reinforcement detailing.

V. K. Raina [6] “Concrete bridge handbook” useful in understanding the design philosophy concepts of elastic design and load factor (limit state) design method. And his book “Analysis, Design and Economics” is useful in solving example with easy analysis techniques.

V.L. Shah and S.R Karve [7] had described limit state theory and design of R.C. structure in his book “Limit State Theory and Design of Reinforced Concrete”. This book is very useful in understanding theoretical aspect of design philosophy including limit state design method. It very useful in solving example of R.C structures such as slab and beams with reinforcement detailing as per I.S:456-2000.

Richards M. Barker [8] had described load and resistance factored design theory and design of R.C. bridge in his book “Design of highway bridges an LRFD Approach”. This book is very useful in understanding theoretical aspect of design philosophy including load and resistance factored design. It very useful in solving sample calculation of bridge superstructure.

Edward G. Nawy [9] had described fundamental approach of R.C structure using ACI318-05 in his book “Reinforced concrete”. This book is very useful in understand-

ing fundamental aspect of design philosophy used by ACI318-05.

I.R.C:6-2000 “Standard Specifications and Code of Practice for Road Bridge” Section-II Load and stress [10] (fourth revision) is useful in application of vehicular load on the bridge structure. **I.R.C:21-2000 “Standard Specifications and Code of Practice for Road Bridge” Section-III Cement Concrete [11]** (third revision) is useful in application of vehicular load on the bridge structure.

I.R.C:6 draft code [12] according to the amendment No.8 is here notified from 1 June 2009 used for load combination for working out the stress in members using limit state design approach. **IS-456:2000 “Indian code practice for plain and reinforced concrete” [13]** (fourth revision) is useful for limit state design of R.C.C bridge.

Design Specifications-2007 by the American Association of State Highway and Transportation Officials.” [14] (fourth edition) is useful for load and resistance factored design of R.C.C bridge.

Chapter 3

Comparison of Design Methods

3.1 General

The traditional method of design was based on the concept of allowable working load stresses, and was associated conventionally with theory of elasticity. The factor of safety, determining the allowable stresses, catered for a margin of safety. Subjective ignorance regarding the resistance of material at the limiting state failure was thus added to the objective uncertainty associated with imperfection of human observation.

3.2 Limit State Design as per IS456:2000

3.2.1 Introduction

The bridge superstructure is designed by both the methods and compared with working stress design method to find most efficient design philosophy. In the limit state design method, the structure shall be designed to withstand safety all loads likely to act throughout the life. It shall not suffer total collapse under the accidental loads, the objective of design is to achieve a structure that will remain fit for use during its life with acceptable target reliability. In other words, the probability of a limit state being reach during its life time should be very low. The acceptable limit for

safety and serviceability requirement before the failure occurs is called a limit state. In general structure must be design for the critical and check for other limit state.

3.2.2 Partial safety factor

Following are the partial safety factors according to the amendment no.8 of IRC:6-2000 given in Table 3.1 ,

Table 3.1: Partial safety factors(IS-456:2000)

Load Type	partial safety factor	
	Ultimate strength	Servicibility strength
Dead load	1.35	1
Wearing surface	1.75	1
Live load	1.5	1

3.2.3 Stress block

The stress block diagram of T-beam for finding out the neutral axis.

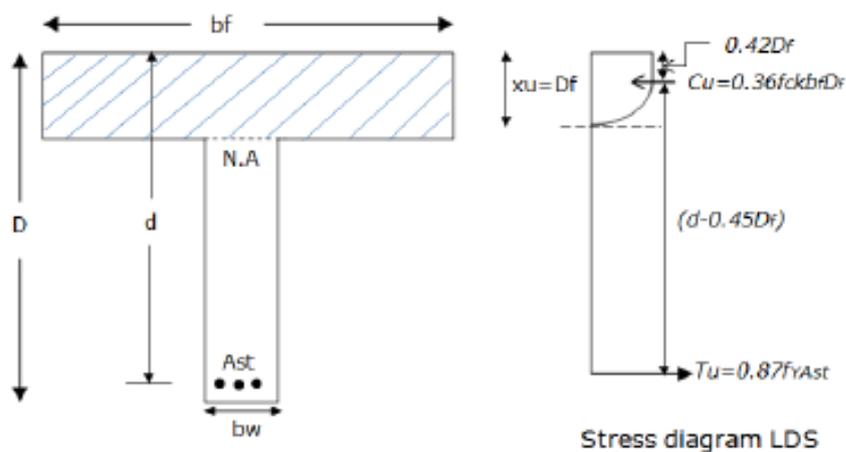


Figure 3.1: Neutral Axis Lies In Flange Stress Diagram LSD

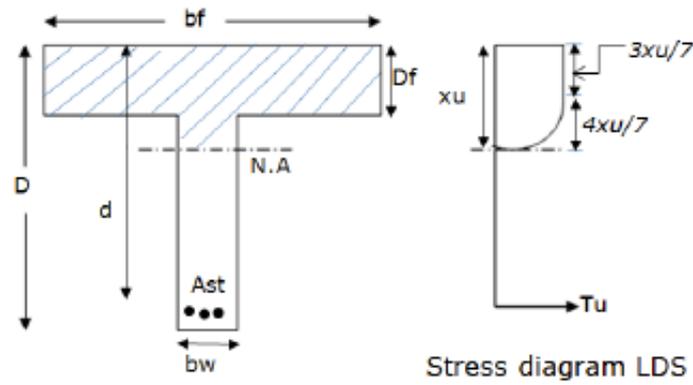


Figure 3.2: Neutral Axis Lies In Web Stress Diagram LSD

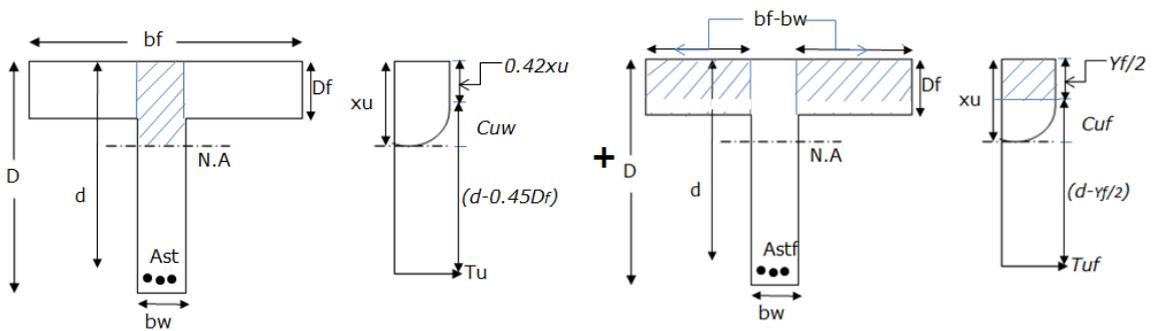


Figure 3.3: Parabolic part of stress-block inside flange (LSD)

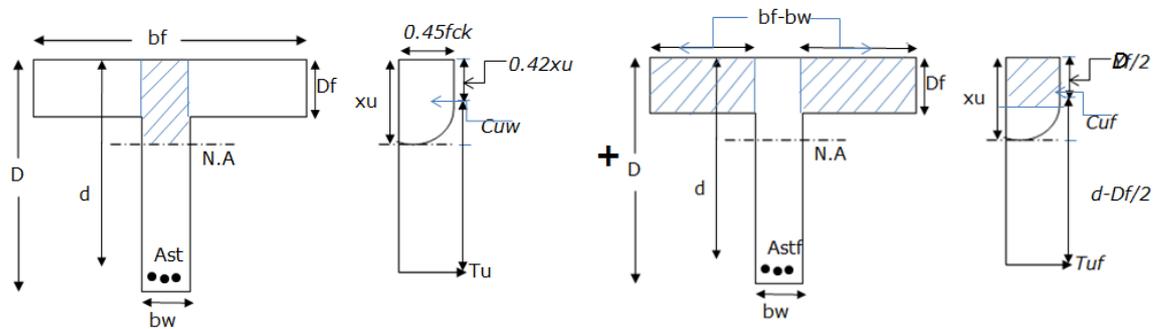


Figure 3.4: Parabolic part of stress-block lying outside flange (LSD)

3.2.4 Limit state of collapse-flexure

Case-I: When Neutral axis lie in flange i.e.($x_u < D_f$) as shown in 3.1.

- x_u can be found out from equilibrium condition $C_u f = T$,

$$x_u = \frac{0.87 f_y A_{st}}{0.36 f_{ck} b_f} \quad (3.1)$$

- Moment of resistance with respect to compression force resisted by flange = $C_u f$ is given

$$MR = 0.36 f_{ck} b_f x_u (d - 0.42 x_u) \quad (3.2)$$

- Moment of resistance with respect to tensile force is given by

$$MR = 0.87 f_y A_{st} (d - 0.42 x_u) \quad (3.3)$$

$$A_{st} = \frac{0.5 f_{ck}}{f_y} \left[1 - \sqrt{1 - \frac{4.6 M_u}{f_{ck} b d^2}} \right] \times b \times d \quad (3.4)$$

- When $x_u = D_f$, then

$$MR = 0.36 f_{ck} b_f D_f (d - 0.42 D_f) \quad (3.5)$$

$$A_{st} = \frac{0.36 f_{ck} b_f D_f}{0.87 f_y} \quad (3.6)$$

When N.A lie in web i.e. ($x_u > D_f$) as shown in fig.3.2. It is divided in two part, one consist of concrete in the web portion of width b_w and depth x_u and other consist of projecting flanges of width $(b_f - b_w)$ and depth D_f .

Case: II(a) The depth of rectangular part of stress block is less than the depth of flange i.e. $3x_u/7 < D_f$ or $x_u < 7D_f/3$ D_f , as shown in 3.2., x_u can be found out from

$$x_u = \frac{0.87 f_y A_{st} - 0.45 \times 0.65 f_{ck} D_f (b_f - b_w)}{0.36 f_{ck} b_w + 0.45 \times 0.15 f_{ck} (b_f - b_w)} \quad (3.7)$$

$$M_{ur} = 0.36f_c k b_w x_u (d - 0.42x_u) + 0.45f_c k (b_f - b_w) b_f (d - \frac{y_f}{2}) \quad (3.8)$$

$$A_{st} = \frac{0.36f_c k b_w x_u + 0.45f_c k (b_f - b_w) y_f}{0.87f_y} \quad (3.9)$$

Where,

$$y_t = (0.15x_u + 0.65D_f) \quad (3.10)$$

Case-II(b): The depth of rectangular part of stress block greater than the depth of flange i.e. $3x_u/7 > D_f$ or $x_u > 7D_f/3$, as shown in 3.3., x_u can be found out from

$$x_u = \frac{0.87f_y A_{st} - 0.45 \times 0.65f_c k D_f (b_f - b_w)}{0.36f_c k b_w} \quad (3.11)$$

$$M_{ur} = 0.36f_c k b_w x_u (d - 0.42x_u) + 0.45f_c k (b_f - b_w) b_f (d - D_f) \quad (3.12)$$

$$A_{st} = \frac{0.36f_c k b_w x_u + 0.45f_c k (b_f - b_w) D_f}{0.87f_y} \quad (3.13)$$

3.2.5 Limit state of collapse- shear

Generally, shear failure in reality occurs under the combined action of shearing forces and bending moments, is characterized by very small deflection and lack of ductility. This failure many times sudden and without any warning. For this reason the shear failure is considered very undesirable and is usually avoided. Nominal shear stress is,

$$\tau_v = \frac{V_u}{bd} \quad (3.14)$$

For solid slab shear strength of concrete shall be $\tau_{uc}k$, k taken from (cl:40.2.1.1), nominal shear stress not exceed the half the values given in table-20 of IS-456:2000. In case of beam, the external shear ultimate state is jointly carried by the concrete

and web steel, and equilibrium equation written as:

$$V_u = V_{uc} + V_{us} \quad (3.15)$$

where,

$$V_{uc} = \tau_{uc} b D \quad (3.16)$$

$$V_{us} = 0.4 b D \quad (3.17)$$

If $V_{uc} \geq V_u$, then no need to provide shear reinforcement.

3.2.6 Limit state of serviceability

Limit state state philosophy of design considers the performance of a structure or rather the fitness of structures to serve the desired function satisfactorily, i.e the serviceability of the structure, as one of the important criteria of structural design besides safety, economy and durability.

3.2.7 Limit State of Deflection

There are two types of deflection are:

- a. Short-term deflection: this is due to initial elastic deformation of the member due to load and permanent imposed load under service condition.

Moment of inertia of gross cross-section (I_{gr}) ignoring reinforcement, for flanged beam section (gross uncracked section):

$$x = \frac{b_w D/2 + (b_f - b_w) D_f^2/2}{b_w D + (b_f - b_w) D_f} \quad (3.18)$$

$$I_{gr} = \frac{b_f x^3}{3} - \frac{(b_f - b_w)(x - D_f^2)^3}{3} - \frac{b_w(D - x)^3}{3} \quad (3.19)$$

Moment of inertia of gross cross-section (I_r) ignoring reinforcement, for flanged beam section (cracked section):

When neutral axis lies in web,

$$b_f D_f \left(x - \frac{D_f}{2}\right) = m A_{st} (d - x) \quad (3.20)$$

$$x = \frac{b_f D_f^2 / 2 + m A_{st} d}{b_f D_f + m A_{st}} \quad (3.21)$$

$$I_r = \frac{b_f x^3}{3} - \frac{(b_f - b_w)(x - D_f)^3}{3} + m A_{st} (d - x)^2 \quad (3.22)$$

When neutral axis lies in flange,

$$I_r = \frac{b_f x^3}{3} + m A_{st} (d - x)^2 \quad (3.23)$$

Effective moment of inertia of flanged beam section (I_{eff}):

For simply supported beams and cantilevers,

$$I_{eff} = \frac{I_r}{1.2 - \frac{M_r}{M} \frac{z}{d} \left(1 - \frac{x}{d}\right) \frac{b_w}{b}} \quad (3.24)$$

- b. Long term deflection: long-term deflection is caused due to creep and shrinkage under sustained load and additional short-term deflection due to temporary live loads.

Deflection due to shrinkage:

$$a_{c3} = k_3 \psi_{cs} l^2 \quad (3.25)$$

Where,

$$\psi_{cs} = k_4 \frac{\varepsilon_{cs}}{D} \quad (3.26)$$

$$k_4 = 0.72 \frac{p_t - p_c}{\sqrt{p_t}} \leq 1 \text{ for } 0.25 \leq P_t - P_c < 1 \quad (3.27)$$

or

$$k_4 = 0.65 \frac{p_t - p_c}{\sqrt{p_t}} \leq 1 \quad (3.28)$$

Deflection due to creep:

$$a_{cc(perm)} = a_{icc(perm)} - a_{i(perm)} \quad (3.29)$$

Permissible deflection:

For dead load, $\Delta_{allowable} = L/350$

For live load, $\Delta_{allowable} = L/800$

For total load, $\Delta_{allowable} = L/600$

3.2.8 Limit State Cracking

To check the width of cracking:

$$W_{cr} = \frac{3a_{cr}\varepsilon_m}{1 + 2\left(\frac{a_{cr} - C_{min}}{D - x}\right)} \quad (3.30)$$

$$\varepsilon_m = \varepsilon_1 - \frac{b(D - x)(a - x)}{3E_S A_{st}(d - x)} \quad (3.31)$$

Permissible deflection:

The total load taken to check crack width D.L+50% L.L.

For moderate environmental condition = 0.3 mm

For severe environmental condition = 0.2 mm

3.3 Load and resistance factor design as per AASTHO specification

LRFD is a method of proportioning structures such that no applicable limit state is exceeded when the structure is subjected to all appropriate design load combinations. The proposed LRFD method provides reasonably accurate solution approach. In addition, LRFD basic principle is same as limit state design method, the difference will be better calibration of the load and resistance factors, a more reasonable combination of various load effects and a better use of the strength of the total structure. This considers the design life of various materials or various types of structures so that paying a little higher price during construction to get more service life can be justified. LSD basically the same as the LRFD being proposed, but the term is more descriptive since the method includes criteria for performance under both serviceably limit state and ultimate limit state. The basic design expression in the AASHTO (2007) LRFD Bridge Specification that must be satisfied for all limit states, both global and local, is given as:

$$\phi R_n \geq \sum \eta_i \gamma_i Q_i \quad (3.32)$$

where Q_i , is the force effect. R_n is the nominal resistance, γ is the statistically based load factor applied to the force effects, ϕ is the statistically based Resistance factor applied to nominal resistance, and Q_i , is a load modification factor. For all nonstrength limit states, $\eta = 1.0$.

The load modifier η is a factor that takes into account the ductility, redundancy and operational importance of the bridge. It is given for loads for which a maximum value of γ is appropriate by:

$$\eta_i = \eta_D \eta_R \eta_I \geq 0.95 \quad (3.33)$$

where, η_D is the ductility factor, η_R is the redundancy factor, and η_I is the operation importance factor. The first two factors refer to the consequence of a bridge being out of service. For all nonstrength limit states, $\eta_D = \eta_R = 1$.

Ductility is important to the safety of a bridge. If ductility is present, over loaded portions of the structure can redistribute the load to other portions that have reserve strength. This redistribution is dependent on the ability of the overloaded component and its connections to develop plastic deformations without failure.

The values to be used for the strength limit state ductility factor are:

$\eta_D \geq 1.05$ for nonductile components

$\eta_D = 1$ for conventional designs and all other limit state

$\eta_D = 1$ for components for additional ductility

Redundancy significantly affects the safety margin of a bridge structure. A statically indeterminate structure is redundant, that is, has more restraints than are necessary to satisfy equilibrium.

$\eta_R \geq 1.05$ for nonredundant member

$\eta_R = 1$ for conventional levels of redundancy

$\eta_R \geq 0.95$ for exceptional redundancy

Bridges can be considered of operational importance if they are on the shortest path between residential areas and a hospital or school or provide access for police, fire, and rescue vehicles to homes, businesses, and

industrial plants. In the event of an earthquake, it is important that all lifelines, such as bridges, remain open. Therefore, the following requirements apply to the extreme event limit state as well as to the strength limit state: $\eta_I \geq 1.05$ for a bridge

of operational importance

$\eta_I = 1$ for typical bridge

$\eta_I \geq 0.95$ for relatively less important bridges

3.3.1 Partial safety factors

Following are the partial safety factors according to the ASSTHO specification given in Table 3.2 ,

Table 3.2: Partial safety factors(AASTHO

Load Type	partial safety factor	
	Ultimate strength	Servicibility strength
Dead load	1.25	1
Wearing surface	1.5	1
Live load	1.75	0.75

3.3.2 Stress block

The section has to be considered as a T-section for findng out neutral axis,

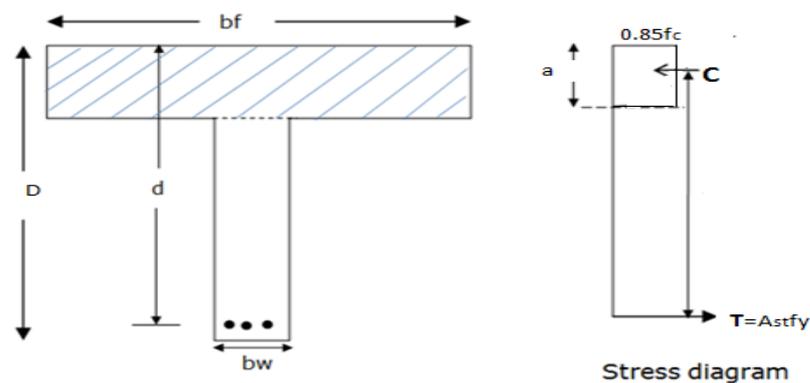


Figure 3.5: Neutral axis inside flange LRFD

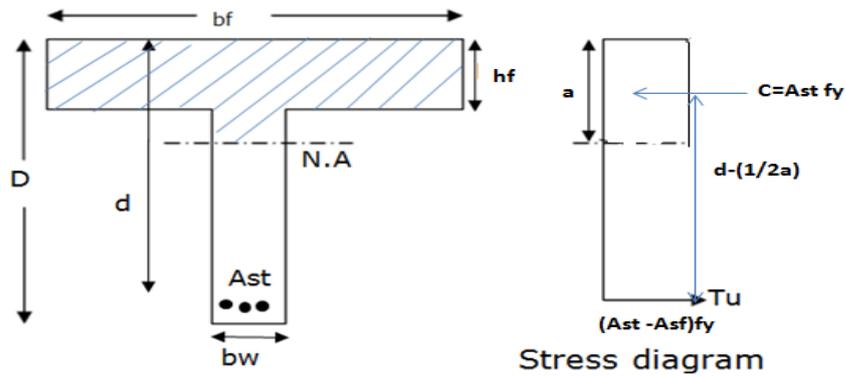


Figure 3.6: Neutral axis outside flange LRFD

3.3.3 LRFD - Flexure Limit State

Case-I: Depth of neutral axis less than flange hf,

This case can be treated similarly to the standard rectangular section provided that the depth a of the equivalent rectangular block is less than the flange thickness. The flange width b_f of the compression side should be used as the beam width analysis. Force equilibrium where $C=T$,

$$0.85f_c b a = A_s f_y \quad (3.34)$$

$$a = \frac{A_s f_y}{0.85 f_c b} \quad (3.35)$$

The nominal moment strength would thus be,

$$M_n = A_s f_y (d - a/2) \quad (3.36)$$

Since the force contribution in tension zone is neglected. It does not matter whether part of the flange is in the tension.

Case - II: Depth of neutral axis larger than flange hf,

In this case, $a > h_f$ the depth of the equivalent rectangular stress block a could be smaller or larger than the flange thickness h_f . This type of T-beam ($a > h_f$) can be treated in a manner similar to that for doubly reinforced rectangular cross section. Force equilibrium where $C=T$,

$$0.85f_c(b - b_w)h_f = (A_{sf}f_y) \quad (3.37)$$

where, A_{sf} is an imaginary compressive steel area whose force capacity is equivalent to the force capacity of the compressive flange overhang. Consequently, an equivalent area A_{sf} of compression reinforcement to develop the overhang flange would have a value of

$$A_{sf} = \frac{0.85f_c(b - b_w)h_f}{f_y} \quad (3.38)$$

For a beam to be considered as a real T-beam, the tension force $A_{sf}f_y$ generated by the steel should be greater than the compression force capacity of the total flange area

$$a = \frac{A_{st}A_{sf}f_y}{0.85f_cb_w} \quad (3.39)$$

The nominal moment strength would thus be,

$$M_n = ((A_{st} - A_{sf})f_y(d - a/2)) + (A_{sf}f_y(d - 0.5h_f)) \quad (3.40)$$

3.3.4 LRFD-Shear Limit State

Nominal shear stress v is divided by f_c to obtain the ratio of v/f_c , this ratio is higher than 0.25, larger cross section required. The nominal shear stress is

$$v = \frac{V_u}{\phi_n b_v d_v} \quad (3.41)$$

Total shear strength of concrete and steel in web portion,

$$V_n = V_c + V_s \quad (3.42)$$

$$V_c = 0.083\beta\sqrt{f_c}b_vd_v \quad (3.43)$$

$$V_s = \frac{V_u}{\phi_v} - 0.083\beta\sqrt{f_c}b_vd_v \quad (3.44)$$

or,

$$V_s = \frac{A_vf_yd_v}{S} \quad (3.45)$$

If $V_u \geq 0.5\phi V_c$ no need to provide shear reinforcement.

3.3.5 LRFD-Service Limit State

The service limit state shall be taken as restrictions on deformation(deflection) and crack width under regular service conditions.

3.3.6 Deformation

$$I_e = \left(\frac{M_{cr}}{M_a}\right)^3 I_g + \left[1 - \left(\frac{M_{cr}}{M_a}\right)^3\right] I_{cr} \leq I_g \quad (3.46)$$

$$I_{cr} = \frac{1}{3}bx^3 + nA_s(d-x)^2 \quad (3.47)$$

$$M_{cr} = f_r \frac{I_g}{y_t} \quad (3.48)$$

Permissible deflection:

For dead load, $\Delta_{allowable} = L/350$

For live load, $\Delta_{allowable} = L/800$

For total load, $\Delta_{allowable} = L/600$

Cracking control

$$f \leq f_{sa} = \frac{Z}{(d_c A)^{1/3}} \quad (3.49)$$

where,

f_c = concrete cover,

Z = crack width parameter value given in table 3.3

A = area of concrete $f \leq 0.6f_y$, then the crack width is under the permissible limit.

Table 3.3: Crack width parameter

Exposer condition	Z(N/mm)	Crack width
Moderate	30000	0.41
Severe	23000	0.3
Buried structure	17000	0.23

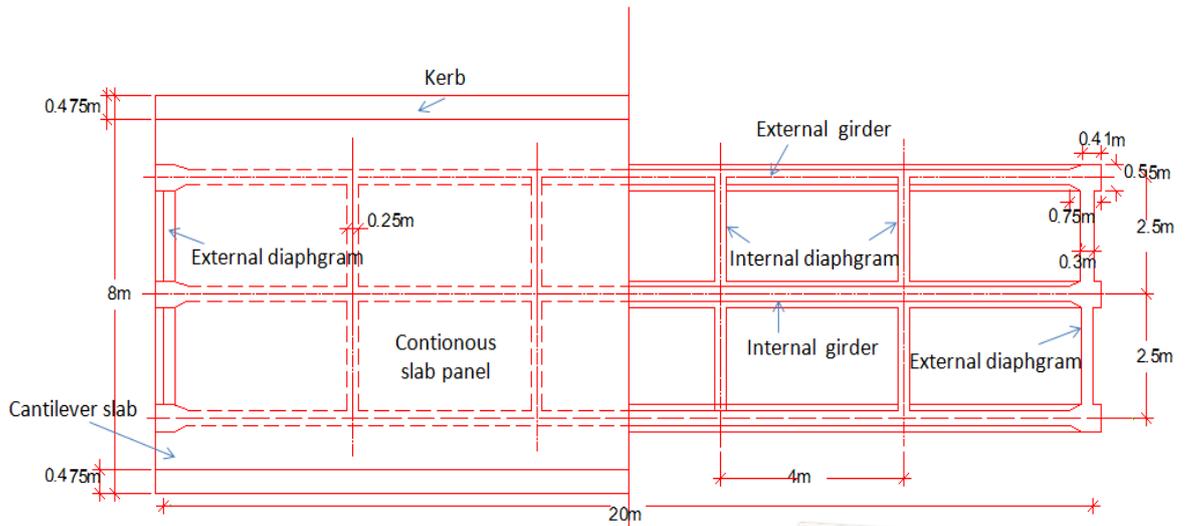


Figure 4.2: Longitudinal Bridge Cross Section

Effective span of Bridge	=	20 m
c/c distance of cross-girder	=	4 m
No. of diaphragm	=	6
Width of carriageway	=	7.5 m
Length of cantilever portion	=	1.35 m
RCC Grade	=	M30
Grade of reinforcement	=	Fe415
Unit weight of RCC	=	24 kN/m ³
Unit weight of wearing coat	=	22 kN/m ³
Unit weight of structural steel	=	78.5 kN/m ³
Width of bridge	=	8 m
No. of longitudinal girder	=	3
c/c distance of longitudinal-girder	=	2.5 m
Width of Curb	=	475 mm
Width of parapet	=	250 mm
Height of curb	=	200 mm
Height of parapet	=	1000 mm
Thickness of intermediate Deck Slab	=	205 mm
Thickness of cantilever Deck Slab	=	230 mm

4.3 IRC Loading

In order to analyze the bridge to these moving loads, IRC-6 (loads and stresses) recommends certain standard hypothetical loading systems. The bridge is then designed for the maximum response values under these standard loads. The live load which gives maximum bending moment and shear force at different position and which are used for analysis is shown in fig.4.3, fig.4.4 and fig.4.5.

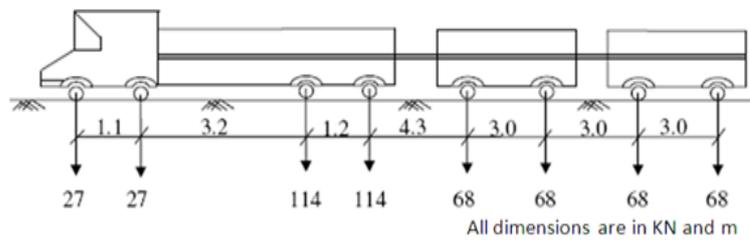


Figure 4.3: Class A Wheeled Vehicle

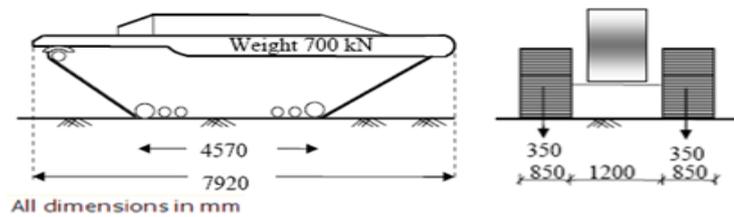


Figure 4.4: Class 70R Tracked Vehicle

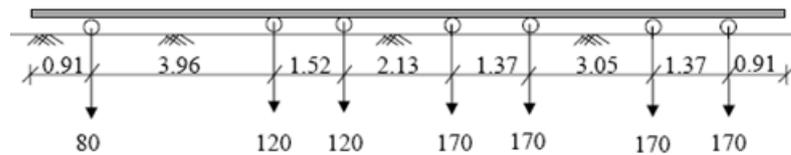


Figure 4.5: Class 70R Wheeled Vehicle

4.4 Slab Analysis

The deck slab is analyzed for dead loads and live loads. Mostly class A wheeled for cantilever portion and class 70R tracked vehicle on two way spanning slab gives critical forces as it is heaviest vehicle. The moments in the two directions can be computed by using the design curves developed by M. Pigeaud.

4.4.1 Cantilever slab:

Dead Load calculation

Table 4.1: Cantilever Slab Dead Load Moment

Components	D.L m ²	C.G m	Moment KN.m	S.F KN
Slab	7.452	0.675	5.03	
Wearing coat(W.C)	2.228	1.35	3.01	
Parapet	5.28	1.35	1.35	
Kerb	3.135	1.11	4.7	
Total			14.09	20.42

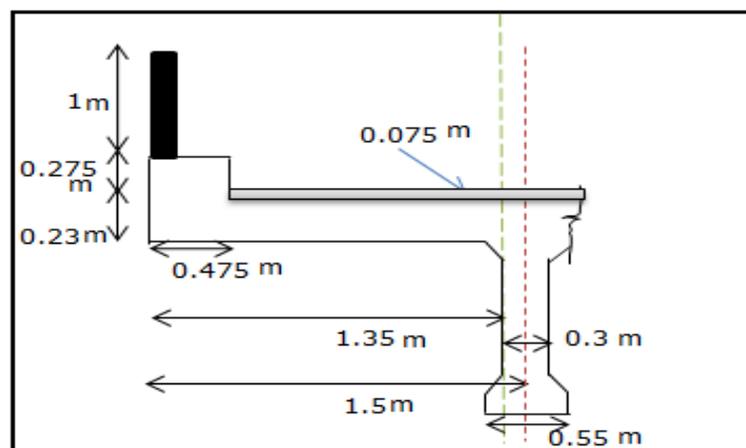


Figure 4.6: Cantilever Slab

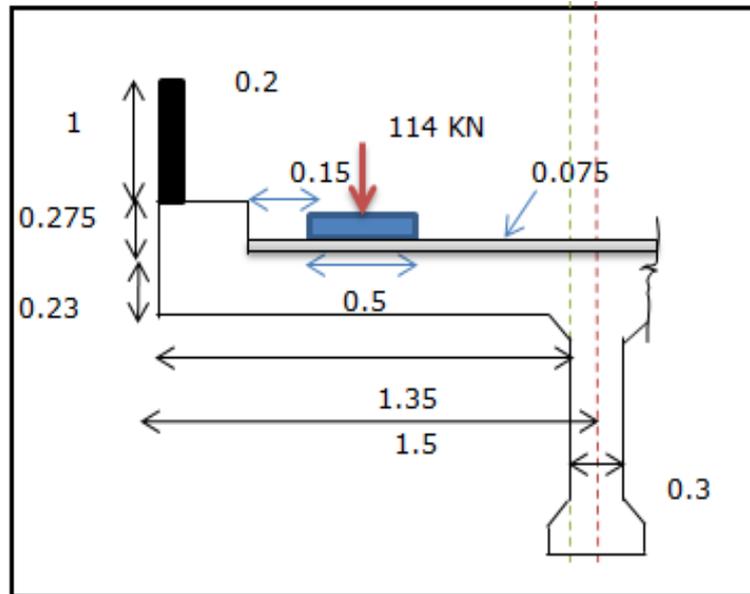


Figure 4.7: Class A Heaviest Wheel Near To Minimum Distance from Kerb

Live Load calculation

On the basis of the criteria of minimum clearance from the kerb. Class-A two wheel live load will be critical on the cantilever portion of the deck slab.

Placing wheel of 114kN axle of Class-A @ 0.15m from kerb.

$$\text{Effective width, } b_{eff} = 1.2 \cdot a + b_1$$

$$\text{where, } a = 1.35 - [0.2 + 0.15 + 0.25]$$

$$a = 0.475 \text{ m}$$

$$\text{Width of wheel along span} = 0.25 \text{ m}$$

$$b_1 = 0.25 + (2 \cdot 0.075)$$

$$= 0.4 \text{ m}$$

$$b_{eff} \text{ across the span} = 1.2 \cdot 0.48 + 0.4$$

$$= 0.97 \text{ m} < 1.2 \text{ m}$$

$$b_{eff} \text{ along span} = 0.5 + 2 \cdot (0.23 + 0.075)$$

$$= 1.11 \text{ m} < 1.8 \text{ m}$$

Load intensity	=	$57 \times 1.53 / 0.97$
	=	90 kN/m
B.M at the face of support	=	47.45 kN.m
S.F at the face of support	=	74 kN
Total Moment	=	62 kN.m
Total shear force	=	94 kN

4.4.2 Continuous slab

Placing one track at the center of the panel to get maximum bending moment. Here, the slab panel of size (4-0.25) x (2.5-0.3) i.e. 3.75mx2.2m. Here L/B ratio is 1.7 which is less than 2, therefore slab is spanning in two direction.

Dead load calculation:

Dead Load Calculation:

$$\text{Self-weight} = 0.205 \times 24 = 4.9 \text{ kN/m}^2$$

$$\text{Weight of wearing coat} = 0.075 \times 22 = 2 \text{ kN/m}^2$$

$$\text{Total} = 6.92 \text{ kN/m}^2$$

$$\text{Total W} = 6.92 \times 4 \times 2.5 = 69.2 \text{ kN}$$

from Pigeaud's curve

$$K = 1.6, 1/K = 0.63$$

$$m_1 = 0.028$$

$$m_2 = 0.042$$

$$M_B = W \times (m_1 + 0.15 m_2) = 2.37 \text{ kNm}$$

$$M_L = W \times (m_2 + 0.15 m_1) = 3.19 \text{ kNm}$$

Design BM including continuity factor

$$MB = 2.46 \times 0.8 = 1.86 \text{ kNm}$$

$$ML = 3.32 \times 0.8 = 2.55 \text{ kNm}$$

Live load calculation:

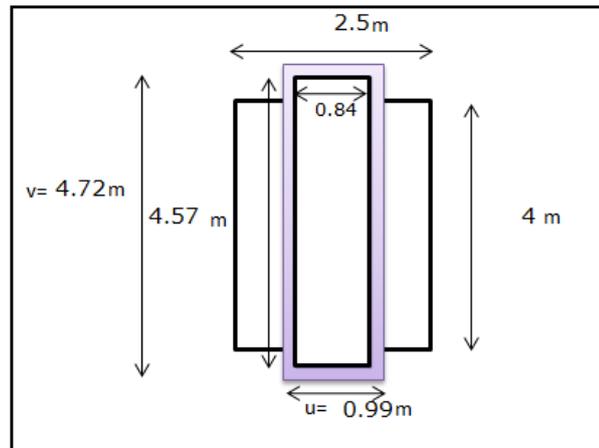


Figure 4.8: Concentrated Load on the Slab Panel

Class-70R Tracked Vehicle :

Live load is class 70R tracked vehicle. One wheel is placed at the centre of panel as shown in fig.

$$\begin{aligned}
 W &= 350 \text{ kN} \\
 u &= 0.85 + 2 * 0.075 = 1 \text{ m} \\
 v &= 4.57 + 2 * 0.075 = 4.72 \text{ m} \\
 (u/B) &= 1/2.5 = 0.4 \\
 (v/L) &= 4.57/4 = 1.25 \\
 (B/L) &= 2.5/4 = 0.67
 \end{aligned}$$

Referring to Pigeaud's curves (refer fig.)

$$m_1 = 0.085$$

$$m_2 = 0.048$$

$$\begin{aligned}
 \text{Short span moment } M_B &= W \times (m_1 + 0.15 m_2) \\
 &= 32.27 \text{ kNm}
 \end{aligned}$$

$$\begin{aligned}
 \text{Long span moment } M_L &= W \times (m_2 + 0.15 m_1) \\
 &= 21.27 \text{ kNm}
 \end{aligned}$$

Design BM including continuity and impact factor :

$$\begin{aligned}
 M_B &= 32.27 \times 0.8 \times (1 + 0.25) = 32.27 \text{ kNm} \\
 M_L &= 21.27 \times 0.8 \times (1 + 0.25) = 21.27 \text{ kNm}
 \end{aligned}$$

Total design bending moment

$$M_B = 1.96 + 32.27 = 34.3 \text{ kNm}$$

$$M_L = 2.65 + 21.17 = 23.9 \text{ kNm}$$

$$\text{Dead Load shear} = 3.5 \text{ kN}$$

For L.L load shear ,

$$\text{Dispersion in direction of span} = 0.84 + 2x(0.075 + 0.205)$$

$$= 1.4 \text{ m}$$

$$\text{The load is kept at} = 0.7 \text{ m from edge of beam}$$

$$\text{Effective width of panel, } b_{eff} = Kx(1-x/L) + b_w$$

$$B/L = 1.6$$

$$K = 2.48$$

$$\text{Effective width} = 6.2 \text{ m}$$

$$\text{Load per m width} = 85.34 \text{ kN}$$

$$\text{Shear force} = 109.7 \text{ kN}$$

$$\text{Shear force with impact} = 137.15 \text{ kN}$$

$$\text{Total S.F} = 141 \text{ kN}$$

Table 4.2: Slab bending moment and shear force

Cantilever slab						
Thickness	Loading	Unfactored		Factored		Remark
(m)		B.M(kNm)	S.F(kN)	B.M(kNm)	S.F(kN)	
0.23	at face	62	94	89	138	LSD
0.26	at face	59	90	95	146	LRFD
Continuous slab panel						
Thickness	Loading	Unfactored		Factored		Remark
(m)		B.M(kNm)	S.F(kN)	B.M(kNm)	S.F(kN)	
0.205	$L_{shorter}$	34.23	94	51	141	LSD
	L_{longer}	23.93		36		
0.235	$L_{shorter}$	35	95	60	165	LRFD
	L_{longer}	24		40		

4.5 Diaphragm Analysis

Diaphragm is analyzed as intermediate and external diaphragm. Intermediate diaphragm is analyzed for dead load and Class 70R tracked vehicular load while as external diaphragm is analyzed for jack force for lifting the super structure for replacement of bearing.

4.5.1 Internal diaphragm

Dead load calculation: As shown in fig 4.8 slab load transfer to cross beam and total dead load on girder is shown in fig 4.9.

Internal diaphragm

Dimensions:

Length = 2.5m

Width = 0.25m

Depth = 1.165m

$$\text{self-wt. of cross girder} = 0.25 \times 0.96 \times 2.4$$

$$= 5.76 \text{ kN/m}$$

$$\text{Dead load from slab wt.} = 2 \times 1/2 \times 2.5 \times 1.25 \times 0.205 \times 24$$

$$= 15.38 \text{ kN}$$

$$\text{Uniformly distributed} = 15.4/2.5$$

$$= 6.15 \text{ kN/m}$$

$$\text{total dead load on cross girder} = 5.76 + 6.1$$

$$= 11.91 \text{ kN/m}$$

$$\text{Reaction on each cross girder} = 13.14 \times 5/3$$

$$= 21.9 \text{ kN}$$

Live load calculation:

For maximum B.M class -70R tracked vehicle on cross girder as shown in fig4.9

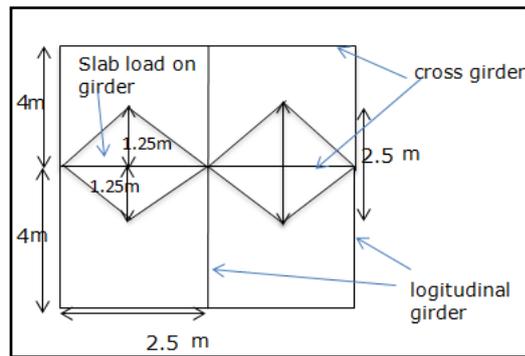


Figure 4.9: Dead Load On Cross Girder

load coming on diaphragm is	= $(350 \times (4 - 1.143)) / 4$
	= 250 kN
Reaction on longitudinal girder	= 166.7 kN
Max. B.M. in cross girder under load	= 190.5 kNm
load coming on diaphragm including impact factor	= 238.11 kN
Dead load B.M	= 16.45 kNm
Live load B.M	= 238 kNm
Total B.M	= 254 kNm
Dead load S.F	= 21.9 kN
Live load S.F	= 198.4 kN
Total S.F	= 220.3 kNm

4.5.2 External diaphragm

Dead load calculation:

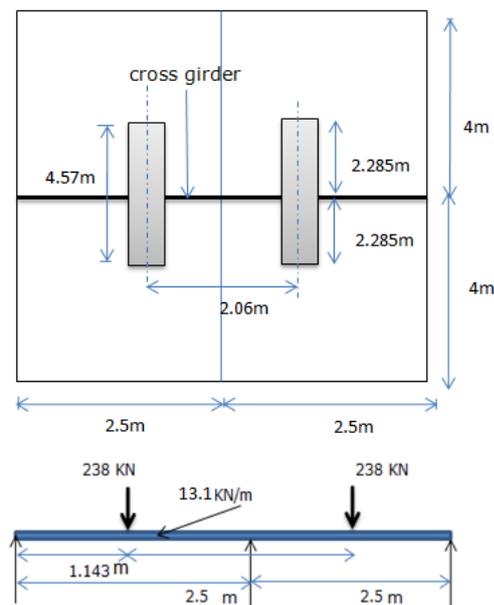


Figure 4.10: Position of Vehicle for Maximum B.M in Cross Girder

Dimensions:

Length	=	2.5 m
Width	=	0.25 m
Depth	=	1.165 m
self-wt.	=	209.7 kN
slab wt.	=	533.9 kN
w.c.wt.	=	141 kN
Railing kerb	=	314.4 kN
Girder weight	=	671.4 kN
Total Dead load	=	1661 kN

Total load of superstructure on one side = 1043 kN

Live Load calculation:

Total 8 jacks per end will be used to lift the superstructure i.e.2 outside and 2 inside between the girders for design consider worst case of girder at centre of 2 jacks.

$$\begin{aligned} \text{force per jeck} &= 130 \text{ kN} \\ \text{load per girder} &= 260 \text{ kN} \\ \text{Max. B.M} &= wl/4 = 325 \text{ kNm} \\ \text{Max. S.F} &= wl/2 = 650 \text{ kN} \end{aligned}$$

Table 4.3: Diaphragm bending moment and shear force

External diaphragm						
Thickness	Depth	Unfactored		Factored		Remark
(m)		B.M(kNm)	S.F(kN)	B.M(kNm)	S.F(kN)	
0.25	1.165	325	650	447	895	LSD
0.3	1.165	338	676	408	826	LRFD
Internal diaphragm						
Thickness	Loading	Unfactored		Factored		Remark
(m)		B.M(kNm)	S.F(kN)	B.M(kNm)	S.F(kN)	
0.25	1.165	254	220	377	324	LSD
0.3	1.165	272	237	468	402	LRFD

4.6 Girder Analysis

In order to simplify the computation of load distribution some rational methods like, Courbon's method, Guyon Massonet method, Hendry Jaegar method are used. IRC prefers Courbon's method, which is simple easily calculated manually. And using SAP2000 software both can be verified.

4.6.1 Courbon's method:

Courbon's method is the simplest method to calculate live load distribution factor. when the live load are positioned nearer to the kerb as shown in fig. 4.10, the centre of gravity of live load acts eccentrically with the centre of gravity of the girder system. Due to this eccentricity, the load shared by each girder is increased or decreased depending upon the position of the girders. Forces are distributed by reaction factor.

Reaction factor is calculated for position of vehicle for maximum force in all girders. The reaction factor is given by equation 4.2.

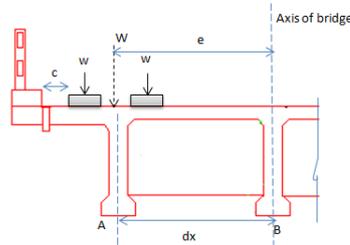


Figure 4.11: Position of Live Load for Maximum Moment in Girder 'A'

$$R_x = \left(\sum \frac{W}{n} \right) \left[1 + \left(\frac{\sum I}{\sum dx^2 \times I} \right) dx \times e \right] \quad (4.1)$$

Courbon's method can be used when the following conditions are satisfied,

- Courbon's method can be used when the following conditions are satisfied,
- The ratio of span to width of deck is greater than 2 but less than 4.
- The longitudinal girders are interconnected by at least five symmetrically spaced cross girders.
- The cross girder extends to a depth of at least 0.75 times the depth of the longitudinal girders.

4.6.2 SAP 2000:

SAP 2000 is very efficient finite element based powerful tool to analyses any kind of structure for different loading. It is user-friendly software with graphical interface. The analysis is done in SAP2000 using bridge modular and inputting the bridge dimensions in it and bridge model is shown in fig.4.12.

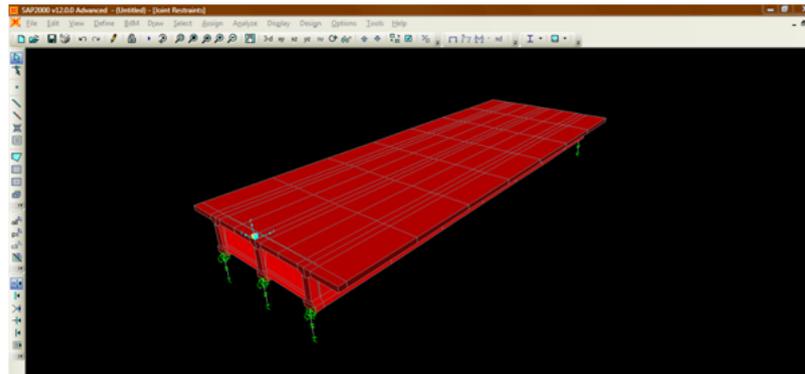


Figure 4.12: SAP2000 Bridge Model

4.6.3 Live load position

The analysis is done for Dead Load, Super Imposed Dead Load and in vehicle load all IRC vehicle. To get maximum forces in external girder, vehicle is placed at minimum distance ('c') provided in IRC6-2000 clause 207.1.3, from the kerb. The position of vehicle is shown in fig 4.13.

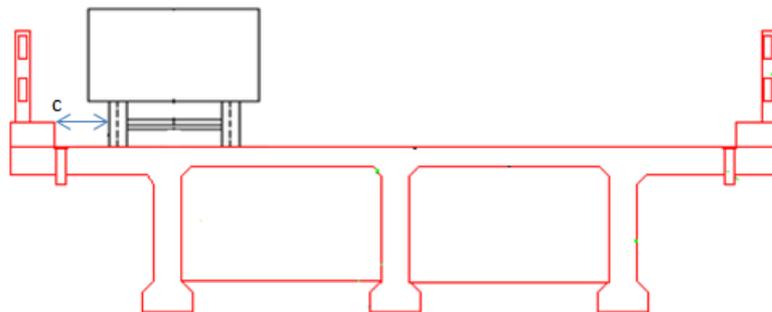


Figure 4.13: Class-70R At Minimum Distance From Kerb For External Girder

The maximum bending moment obtain center of girder, which is due to IRC 70 R vehicle. The position of vehicle is as shown in fig.4.14.

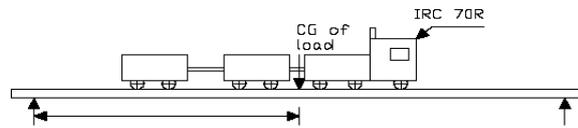


Figure 4.14: Position of Class-70R Vehicle For Max. Bending Moment

The maximum shear forces obtain at support of girder, which is due to IRC 70 R vehicle. The position of vehicle is as shown in fig.4.15.

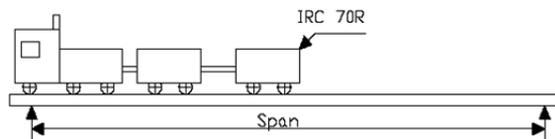


Figure 4.15: Position of Class-70r Vehicle for Max. Shear Force

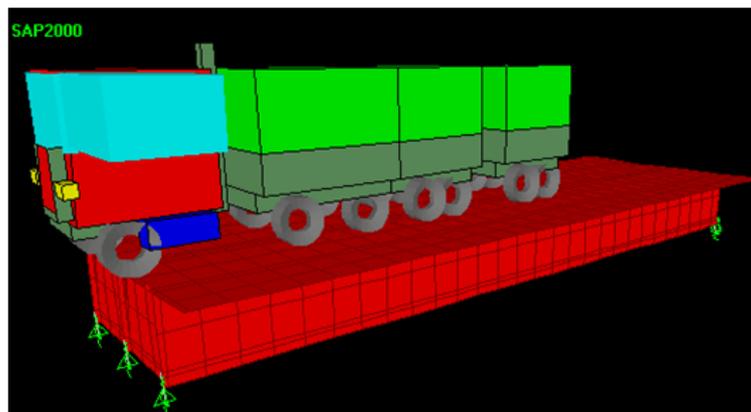


Figure 4.16: IRC Class-70R Vehicle on Moving Bridge Deck

4.6.4 Girder Force

The design force for girder is obtained from results of forces for individual girder. The maximum bending moment and shear force from all vehicle load and dead load among all girder is used for designing all girders. The results obtained from SAP 2000 and courbons method, for maximum forces at different sections out of all girders are recapitulated in Table. And maximum design forces are computed in table.

NOTE:Units in table for bending moment in KN.m and shear force in KN

Table 4.4: Comparison of bending moment

Total bending moment(KN.m)					
Section	Length (m)	External girder		Internal girder	
		Courbon's method	SAP2000	Courbon's method	SAP2000
0L	0	0	0	0	0
0.1L	2	1537	1436	1085	1014
0.25L	5	3497	3268	2400	2243
0.3L	6	3974	3714	2715	2537
0.4L	8	4650	4346	3162	2955
0.5L	10	4918	4596	3322	3105

Table 4.5: Comparison of shear force

Total shear force(KN)					
Section	Length (m)	External girder		Internal girder	
		Courbon's method	SAP2000	Courbon's method	SAP2000
0L	0	0	0	595.99	557
0.1L	2	1084.98	1014	485.78	454
0.25L	5	2400.01	2243	374.5	350
0.3L	6	2714.59	2537	291.04	272
0.4L	8	3161.85	2955	172.27	161
0.5L	10	3322.35	3105	14.98	14

Table 4.6: Unfactored moment and forces on external girder(SAP2000)

External girder							
		D.L		W.C.L		L.L(Class70-R)	
Section	L(m)	B.M	S.F	B.M	S.F	B.M	S.F
0L	0	0	244	0	34	0	445
0.1L	2	538	191	62	27	836	377
0.25L	5	1170	122	129	17	1969	377
0.3L	6	1309	99	144	14	2261	276
0.4L	8	1502	54	165	7	2679	174
0.5L	10	1562	0	172	0	2862	31

Table 4.7: Unfactored moment and forces on internal girder (SAP2000)

Internal girder							
		D.L		W.C.L		L.L(Class70-R)	
Section	L(m)	B.M	S.F	B.M	S.F	B.M	S.F
0L	0	0	319	0	34	0	204
0.1L	2	569	254	62	27	383	173
0.25L	5	1212	160	129	17	902	173
0.3L	6	1357	132	144	14	1036	126
0.4L	8	1562	74	165	7	1228	80
0.5L	10	1621	0	172	0	1312	14

Table 4.8: Factored moment and forces on external girder for LSD

External girder							
		1.35*D.L		1.75*W.C.L		1.5*L.L(Class70-R)	
Section	L(m)	B.M	S.F	B.M	S.F	B.M	S.F
0L	0	0	329	0	60	0	668
0.1L	2	726	257	108	48	1254	566
0.25L	5	1580	165	225	30	2953	566
0.3L	6	1767	134	252	24	3391	414
0.4L	8	2028	73	288	12	4018	262
0.5L	10	2108	0	300	0	4293	46

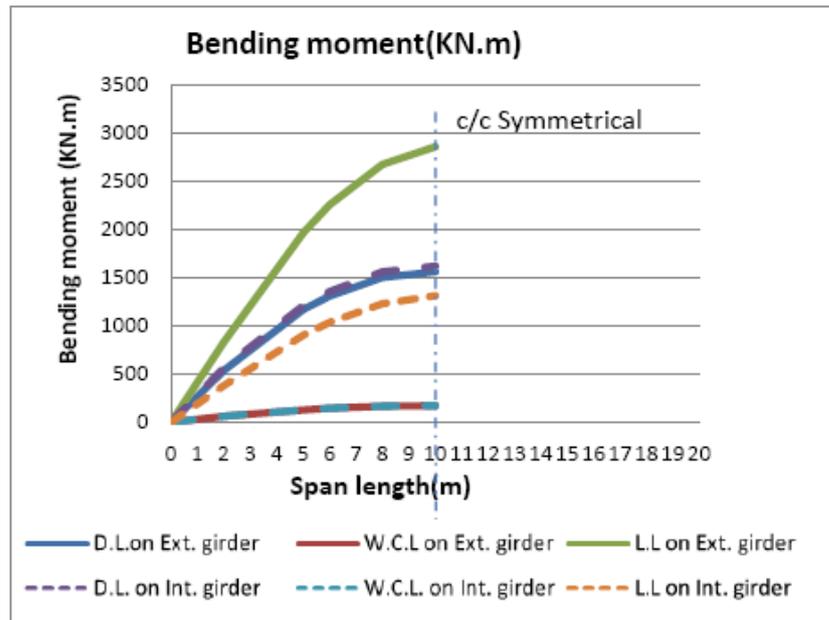


Figure 4.17: Variation in B.M of various load along longitudinal span

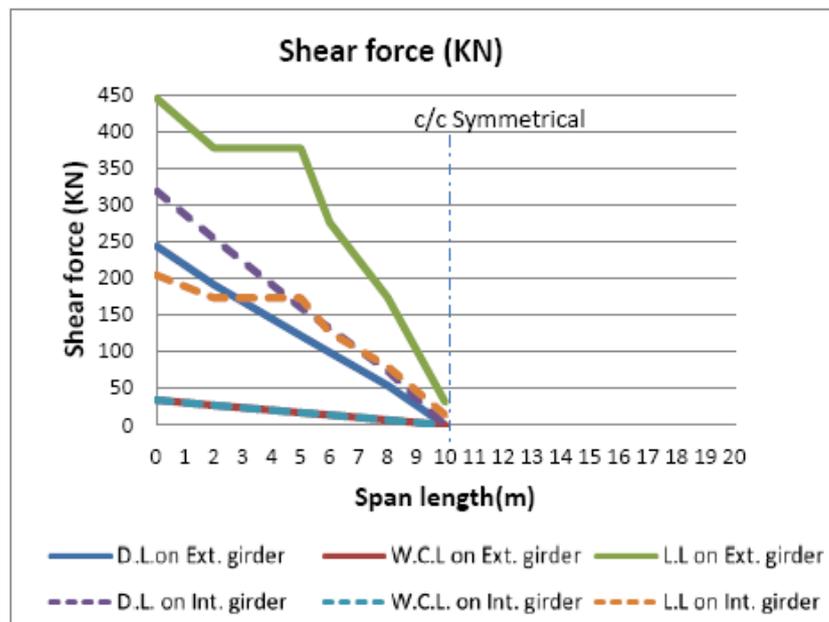


Figure 4.18: Variation in S.F of various load along longitudinal span

Table 4.9: Factored moment and forces on internal girder for LSD

Internal girder							
		1.35*D.L		1.75*W.C.L		1.5*L.L(Class70-R)	
Section	L(m)	B.M	S.F	B.M	S.F	B.M	S.F
0L	0	0	430	0	60	0	306
0.1L	2	768	343	108	48	575	260
0.25L	5	1636	216	225	30	1353	260
0.3L	6	1831	178	252	24	1554	190
0.4L	8	2109	100	288	12	1842	120
0.5L	10	2188	0	300	0	1968	21

Table 4.10: Factored moment and forces on external girder for LRFD

External girder							
		1.25*D.L		1.5*W.C.L		1.75*L.L(Class70-R)	
Section	L(m)	B.M	S.F	B.M	S.F	B.M	S.F
0L	0	0	305	0	51	0	756.5
0.1L	2	672.5	238.8	93	40.5	1421.2	640.9
0.25L	5	1463	152.5	193.5	25.5	3347.3	640.9
0.3L	6	1636	123.8	216	21	3843.7	469.2
0.4L	8	1878	67.5	247.5	10.5	4554.3	295.8
0.5L	10	1953	0	258	0	4865.4	52.7

Table 4.11: Factored moment and forces on internal girder for LRFD

Internal girder							
		1.25*D.L		1.5*W.C.L		1.75*L.L(Class70-R)	
Section	L(m)	B.M	S.F	B.M	S.F	B.M	S.F
0L	0	0	398.8	0	51	0	346.8
0.1L	2	711.3	317.5	93	40.5	651.1	294.1
0.25L	5	1515	200	193.5	25.5	1533.4	294.1
0.3L	6	1696	165	216	21	1761.2	214.2
0.4L	8	1953	92.5	247.5	10.5	2087.6	136
0.5L	10	2026	0	258	0	2230.4	23.8

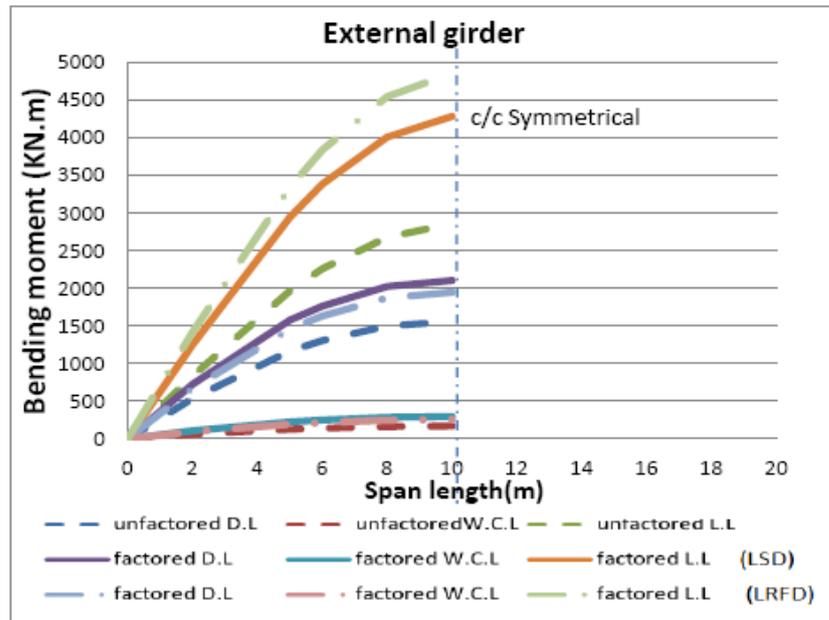


Figure 4.19: Factored bending moment on external girder

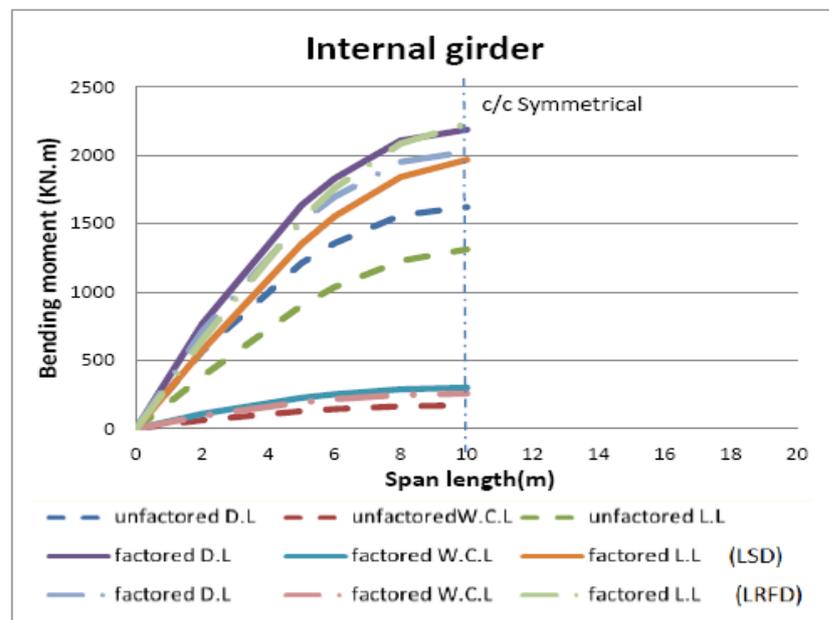


Figure 4.20: Factored bending moment on internal girder

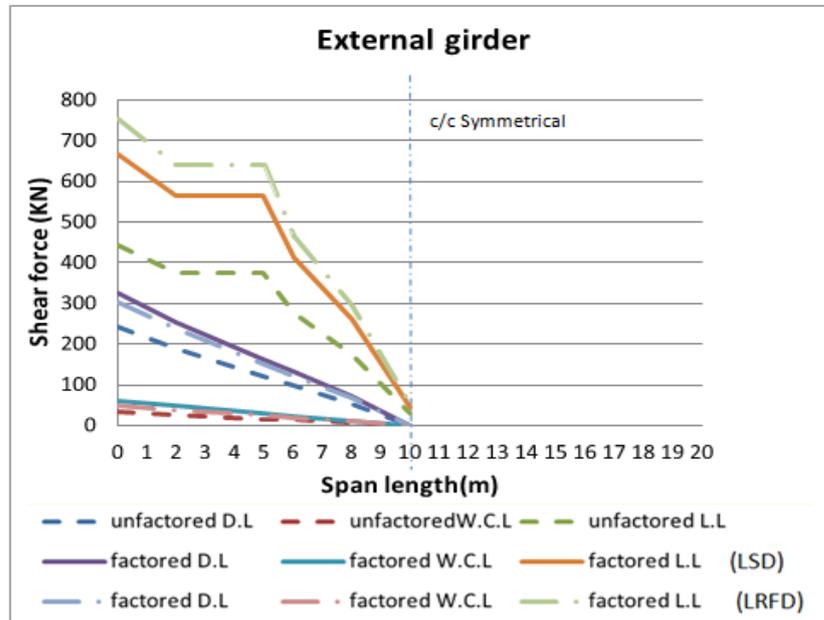


Figure 4.21: Factored shear force on external girder

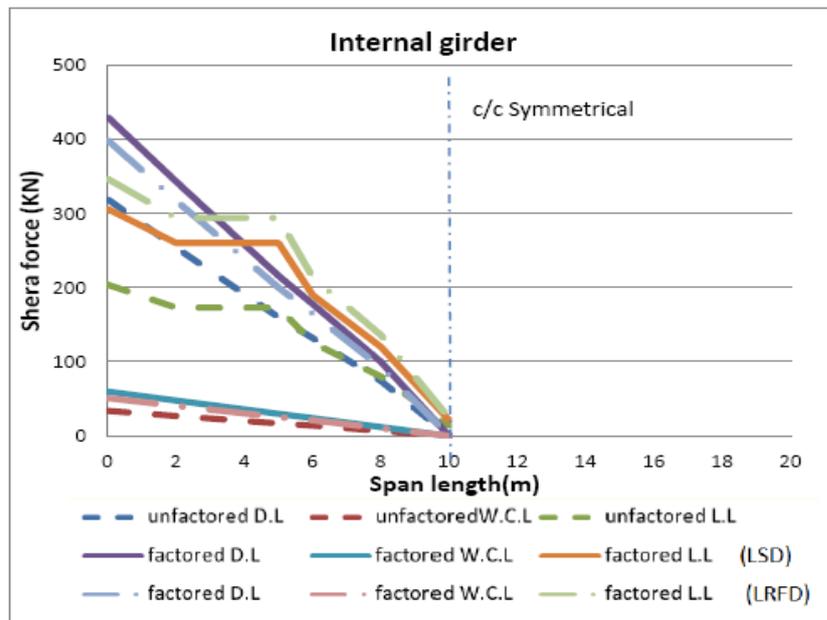


Figure 4.22: Factored shear force on internal girder

4.7 Summary

The difference shows that Courbon's method gives higher moment on girder which is conservative side, at the same time it increases cost of girder. Thus, it can be concluded that by exact analysis design optimization can be done. The maximum bending moment and shear force is on external girder as compared to internal girder. And also show the factored moment which will be required for limit state design and for load and resistance design, which is high then the unfactored moment which will be useful for working stress design. And it is also observed that partial load factors from AASTHO specification gives more moment & forces for live load and less for dead load as compared to partial load factors from IRC-6 amendment no.8.

Chapter 5

Bridge Superstructure Design

5.1 General

R.C.C flyover superstructure sections is taken here to design for the maximum bending moment and shear force using limit state design philosophy and load and resistance factored design.

5.1.1 Problem Formulation

In this study the cross section and data taken same as in chapter 4 which is already analysed for design, section shown in fig:

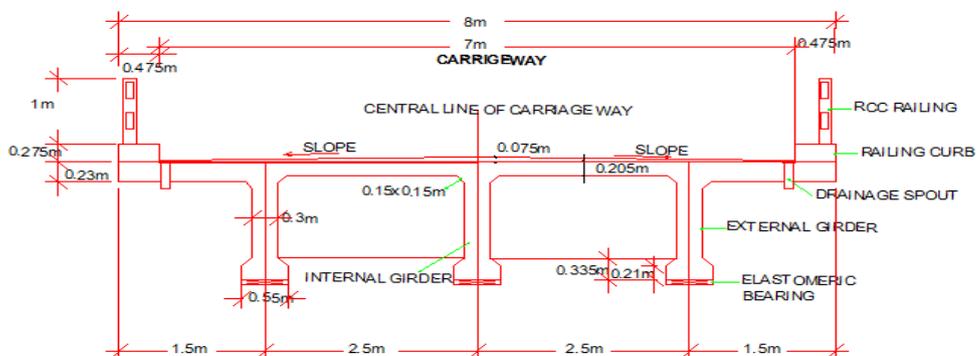


Figure 5.1: Cross Section of Bridge Deck Slab

5.2 Limit State Design Method

5.2.1 Cantilever Slab Design

1) **Design force and moment:**

Unfactored design moment, M	=	61.6 kNm
Unfactored design force, V	=	94 kN
Using, basic load combination, 1.35D.L+1.75W.C+1.5L.L		
Factored Design moment, Mu	=	89 kNm
Factored Design force, Vu	=	138 kN

2) **Dimension:**

Thickness, D	=	230 mm
Effective cover, d'	=	30 mm

3) **Depth check:**

$$k_{u \max} = \frac{700}{1100 + 0.87f_y} = 0.48$$

$$R_{U \max} = 0.36f_{ck}k_{u \max}(1 - 0.42k_{u \max}) = 4.13$$

$$d_{\text{required}} = \sqrt{\frac{M_u}{R_{U \max} b}} = 147 \text{ mm}$$

$$d_{\text{provided}} = 230 - 30 - 12/2 = 194 \text{ mm}$$

$d_{\text{provided}} > d_{\text{required}}$, hence safe.

4) **Moment check:**

$$M_{ur \max} = R_{u \max} b d_{req}^2 = 155 \text{ kNm} \gg M_u$$

Therefore, section in under-reinforced.

5) **Main steel:**

$$A_{st} = \frac{0.5f_{ck}}{f_y} \left[1 - \sqrt{1 - \frac{4.6M_u}{f_{ck} b d^2}} \right] \times b \times d = 1531 \text{ mm}^2$$

Provide 12mm@140mmc/c (top r/f) = 808 mm²

Provide 12mm@150mmc/c (bottom r/f) = 754 mm²

$$\text{Total Ast provided} = 1562 \text{ mm}^2$$

Ast provides $>$ Ast required, safe.

6) **Distribution Steel:-**

Ast required=0.12% of Db for Fe-415

$$\text{Ast} = 0.12 \times 230 \times 1500 / 100 = 414 \text{ mm}^2$$

Prov. half steel at top and half at bottom

$$\text{Provide } 12\text{mm}@250\text{mmc}/c = 452 \text{ mm}^2$$

$$\text{Total Ast provided} = 904 \text{ mm}^2$$

Hence, safe.

7) **Check for shear:-**

$$V_u = 138 \text{ kN}$$

$$pt(\%) = \text{Ast} \times 100 / bd = 0.65$$

$$\tau_c \text{ (From table 19, IS456:2000)} = 0.96$$

for, 230mm slab,

$$k = 1.125$$

$$V_{uc} = (\tau_c \times k) \times bd = 282.85 \text{ kN} > V_u$$

$$\tau_v = 0.53 \text{ N/mm}^2$$

$$\tau_{cmax} \text{ (From table 20, IS456:2000)} = 3.1 \text{ N/mm}^2$$

$$= 1.55 \text{ N/mm}^2 > \tau_v$$

Hence no, need to provide shear reinforcement.

8) **Check for deflection:-**

Using servicibility, basic load combination, D.L+W.C+L.L

Assume section 1000x230mm

$$M_{L.L} = 47.45 \text{ kNm}$$

$$M_{D.L} = 14.09 \text{ kNm}$$

$$\text{Asc (pc\%=1\%)} = 2262 \text{ mm}^2$$

$$\text{Ast (pt\%=4\%)} = 8042.48 \text{ mm}^2$$

$$\begin{aligned}
E_s &= 200000 \text{ N/mm}^2 \\
E_c &= 27386 \text{ N/mm}^2 \\
m &= 7 \\
I_{cr} &= \frac{Bd^3}{12} = 1.01\text{E}+09 \text{ mm}^4 \\
f_{cr} &= 0.75\sqrt{f_{ck}} = 3.8 \text{ N/mm}^2 \\
y_t &= D/2 = 115 \text{ mm} \\
M_r &= \frac{f_{cr}I_{cr}}{y_t} = 34 \text{ kNm}
\end{aligned}$$

Short term deflection:

$$\begin{aligned}
bx^2 + (m - 1)A_{sc}(x - d') &= mA_{st}(d - x) \\
x &= 78 \text{ mm} \\
z=d-x/3 &= 168 \text{ mm} \\
I_r = bx^3/3 + (m - 1)A_{sc}(x - d')^2 + mA_{st}(d - x)^2 &= 9.68\text{E}+08 \text{ mm}^4 \\
\text{Perm. load , } I_{eff} &= \frac{I_r}{1.2 - \frac{M_r z}{M} \left(1 - \frac{x}{d}\right) \frac{bw}{b}} \\
I_{eff} < I_r, \text{ so, } I_{eff} &= I_r = 9.68\text{E}+08 \text{ mm}^4 \\
ai(\text{perm}) = \delta_{DL} &= \frac{M_{D.L}l^2}{4E_cI_{eff}} = 0.120 \text{ mm/m}
\end{aligned}$$

Long term deflection due to shrinkage:

$$\begin{aligned}
k_3 = 0.5, k_4 = 1 \text{ from eq(3.28)} \\
\psi_{cs} &= k_4 \frac{\epsilon_{cs}}{D} = 1.24\text{E}-06 \\
a_{c3} &= k_3 \psi_{cs} l^2 = 1.4 \text{ mm}
\end{aligned}$$

Long term deflection due to creep

$$\begin{aligned}
E_{ec} &= E_c / (1 + \Theta) = 13041 \text{ N/mm}^2 \\
\Theta &= 1.1 \\
m &= 15.33 \\
m-1 &= 14.33 \\
bx^2 + (m - 1)A_{sc}(x - d') &= mA_{st}(d - x) \\
x &= 99 \text{ mm} \\
z=d-x/3 &= 161 \text{ mm} \\
I_r = bx^3/3 + (m - 1)A_{sc}(x - d')^2 + mA_{st}(d - x)^2 &= 1.55\text{E}+09 \text{ mm}^4
\end{aligned}$$

$$\begin{aligned}
\text{Perm. load , } I_{eff} < I_{r,so}, I_{eff} = I_r &= 1.55\text{E}+09 \text{ mm}^4 \\
\text{ai.cc(perm)} &= 1.3 \text{ mm} \\
\text{acc(perm)=ai.cc(perm)-ai(perm)} &= 0.3 \text{ mm} \\
\text{allowable dead load deflection(L/350)} &= 4.3 \text{ mm} \\
\text{Total perm. load deflection} &= 3.69 \text{ mm} < 4.3 \text{ mm}
\end{aligned}$$

Deflection due to L.L

$$\begin{aligned}
\text{Live load , } I_{eff} &= 1.28\text{E}+09 \text{ mm}^4 \\
\text{allowable live load deflection(L/800)} &= 1.9 \text{ mm} \\
ai_{L.L} = \frac{M_{L.L}l^2}{3E_cI_{eff}} &= 1.32 \text{ mm} < 1.9\text{mm}
\end{aligned}$$

9) **Check for crack**

$$\begin{aligned}
M_{D.L} + 50\% M_{L.L} &= 36 \text{ kN} \\
A_{st} &= 8042 \text{ mm}^2/\text{mm} \\
A_{sc} &= 2262 \text{ mm}^2/\text{mm} \\
E_c &= 27386.12 \text{ mm}^2/\text{mm} \\
E_s &= 200000 \text{ N/mm}^2 \\
E_{ce} &= 13693.06 \text{ N/mm}^2 \\
m &= 14.60593907 \\
d &= 194 \text{ mm} \\
D &= 230 \text{ mm} \\
b &= 1000 \text{ mm}
\end{aligned}$$

Determine neutral axis at working load,

$$x = 56.74 \text{ mm}$$

$$d-x = 137.26 \text{ mm}$$

$$I_c = 2.27\text{E}+09 \text{ mm}^4$$

$$\varepsilon_1 M(D-x)/E_{ce}I_c$$

$$\varepsilon_1 = 0.00104$$

$$\varepsilon_m = \varepsilon_1 - \frac{b(D-x)(a-x)}{3E_s A_{st}(d-x)}$$

$$\varepsilon_m = 0.0010$$

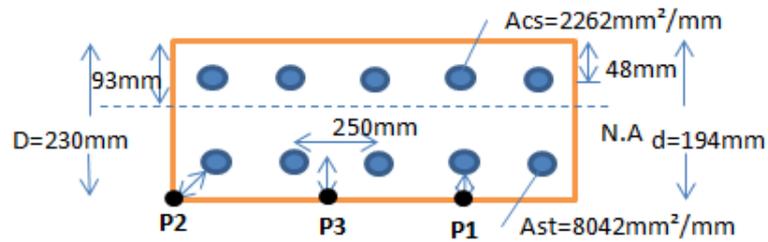


Figure 5.2: Cracked section of cantilever slab

- (a) Crack width directly under a bar on tension face at point P1

$$a_{cr} = \text{nominal cover} + \text{distribution bar dia}/2 = 48 \text{ mm}$$

$$\text{Crack width} = 3a_{cr}\varepsilon_m = 0.14 \text{ mm}$$

<0.3mm ,Safe

- (b) Crack width at bottom corner of beam at P2

$$a_{cr} = \sqrt{((48)^2 + (48)^2)} - (12/2) = 62 \text{ mm}$$

Crack width,

$$W_{cr} = \frac{3a_{cr}\varepsilon_m}{1+2\left(\frac{a_{cr}-C_{\min}}{D-x}\right)} = 0.16\text{mm}$$

<0.3mm ,Safe

- (c) Crack width between bars mid-way at P3

$$a_{cr} = \sqrt{((75)^2 + (48)^2)} - (12/2) = 83 \text{ mm}$$

Crack width,

$$W_{cr} = \frac{3a_{cr}\varepsilon_m}{1+2\left(\frac{a_{cr}-C_{\min}}{D-x}\right)} = 0.19 \text{ mm}$$

<0.3mm ,Safe

5.2.2 Continous Slab panel design

1) **Design force and moment:**

Unfactored design moment, M_x	=	34.23 kNm
Unfactored design moment, M_y	=	23 kNm
Unfactored design force, V	=	94 kN
Using, basic load combination, $1.35D.L+1.75W.C+1.5L.L$		
Factored Design moment, M_{ux}	=	51.25 kNm
Factored Design moment, M_{uy}	=	35.72
Factored Design force, V_u	=	142 kN

2) **Dimension:**

Thickness, D	=	205 mm
Slab panel size,	=	2.5 m x 4 m
Effective cover, d'	=	30 mm

3) **Depth check:**

$$k_{u \max} = \frac{700}{1100 + 0.87f_y} = 0.48$$

$$R_{U \max} = 0.36f_{ck}k_{u \max}(1 - 0.42k_{u \max}) = 4.13$$

$$d_{required} = \sqrt{\frac{M_u}{R_{U \max} b}}$$

$$d_{xreq} = 111 \text{ mm}$$

$$d_{yreq} = 93 \text{ mm}$$

$$d_{provided} = 205 - 30 - 12/2 = 159 \text{ mm}$$

$d_{provided} > d_{required}$, hence safe.

3) **Moment check:**

$$M_{urmax} = R_{urmax} b d_{req}^2 = 105 \text{ kNm} \gg M_{ux}$$

Therefore, section in under-reinforced.

4) **Reinforcement :**

$$A_{st} = \frac{0.5f_{ck}}{f_y} \left[1 - \sqrt{1 - \frac{4.6M_u}{f_{ck}bd^2}} \right] \times b \times d$$

$$A_{stx} = 978 \text{ mm}^2$$

$$\text{Provide 12mm@200mmc/c (bottom r/f)} = 565 \text{ mm}^2$$

$$\text{Provide 12mm@160mmc/c(top r/f)} = 707 \text{ mm}^2$$

$$\text{Total } A_{st} \text{ provided} = 1272 \text{ mm}^2$$

A_{stx} provides $>$ A_{stx} required, safe.

$$A_{sty} = 621 \text{ mm}^2$$

$$\text{Provide 10mm@170mmc/c(top \& bottom r/f)} = 665 \text{ mm}^2$$

A_{sty} provides $>$ A_{sty} required, safe.

$$\text{Extra bar @ support, } a_{st} = 636 \text{ mm}^2$$

$$\text{Provide 10mm@120mmc/c} = 654.4985 \text{ mm}^2$$

6) **Check for shear:-**

$$V_u = 1420 \text{ kN}$$

$$p_t(\%) = A_{stx}100/bd = 0.9$$

$$t_c \text{ (From table 19, IS456:2000)} = 0.6$$

for, 230mm slab,

$$k = 1.125$$

$$V_{uc} = (t_c \times k) \times bd = 263 \text{ kN} > V_u$$

$$t_v = 0.9 \text{ N/mm}^2$$

$$t_{cmax} \text{ (From table 20, IS456:2000)} = 3.1 \text{ N/mm}^2$$

$$= 1.55 \text{ N/mm}^2$$

Hence no, need to provide shear reinforcement.

7) **Check for deflection:-**

Using servicibility, basic load combination, D.L+W.C+L.L

Assume section 1000x205mm

$$\begin{aligned}
M_{L.L} &= 32.27 \text{ kNm} \\
M_{D.L} &= 4.16 \text{ kNm} \\
A_{sc} \text{ (pc\%=5\%)} &= 7972 \text{ mm}^2 \\
A_{st} \text{ (pt\%=6\%)} &= 9703 \text{ mm}^2 \\
E_s &= 200000 \text{ N/mm}^2 \\
E_c &= 27386.13 \text{ N/mm}^2 \\
m &= 7 \text{ N/mm}^2 \\
I_{cr} = \frac{Bd^3}{12} &= 1302 \text{ mm}^4 \\
f_{cr} = 0.75\sqrt{f_{ck}} &= 3.8 \text{ N/mm}^2 \\
y_t = D/2 &= 102.5 \text{ mm} \\
M_r = \frac{f_{cr}I_{cr}}{y_t} &= 48.705 \text{ kNm}
\end{aligned}$$

Short term deflection:

$$\begin{aligned}
bx^2 + (m-1)A_{sc}(x-d') &= mA_{st}(d-x) \\
x &= 18 \text{ mm} \\
z=d-x/3 &= 153 \text{ mm} \\
I_r = bx^3/3 + (m-1)A_{sc}(x-d')^2 + mA_{st}(d-x)^2 &= 1.41\text{E}+09 \text{ mm}^4 \\
\text{Perm. load , } I_{eff} = \frac{I_r}{1.2 - \frac{M_r z}{M} \left(1 - \frac{x}{d}\right) \frac{b_w}{b}} & \\
I_{eff} < I_r, \text{ so, } I_{eff} = I_r &= 1.41\text{E}+09 \text{ mm}^4 \\
\text{ai(perm)} = M_{perm}^2 / 4 * E_c * I_{eff} &= 0.047672 \text{ mm}
\end{aligned}$$

Long term deflection due to shrinkage:

$$\begin{aligned}
k_3 = 0.063, k_4 = 0.133 \\
\psi_{cs} = k_4 \frac{\epsilon_{cs}}{D} &= 1.73\text{E}-07 \\
a_{c3} = k_3 \psi_{cs} l^2 &= 0.024591 \text{ mm}
\end{aligned}$$

Long term deflection due to creep

$$\begin{aligned}
E_{ec} = E_c / (1 + \Theta) &= 13041.01 \\
\Theta = 1.1 \\
m = 15.33 \\
m-1 = 14.33
\end{aligned}$$

$$\begin{aligned}
 bx+(m-1)Asc(x-d) &= mAst(d-x) \\
 x &= 19.5 \text{ mm} \\
 z=d-x/3 &= 152.4 \text{ mm} \\
 Ir=bx^3/3+(m-1)Asc(x-d)^2+mAst(d-x)^2 &= 1.48E+08 \\
 \text{Perm. load , } I_{\text{eff}} = Ir &= 1.79E+09 \text{ mm}^4 \\
 ai.cc(\text{perm}) &= 1.21 \text{ mm} \\
 acc(\text{perm})=ai.cc(\text{perm})-ai(\text{perm}) &= 0.18 \text{ mm} \\
 \text{Total perm. load deflection} &= 1.280513 \text{ mm} < 7.14\text{mm} \\
 \text{allowable dead load deflection}(L/350) &= 7.14 \text{ mm}
 \end{aligned}$$

Deflection due to L.L

$$\begin{aligned}
 \text{Live load , } I_{\text{eff}} &= 1.79E+09 \text{ mm}^4 \\
 a(L.L)=ML.L*L/3*Ec*I_{\text{eff}} &= 0.343 \text{ mm} < 3.125\text{mm} \\
 \text{allowable live load deflection}(L/800) &= 3.125 \text{ mm}
 \end{aligned}$$

7) Check for crack

$$\begin{aligned}
 MW \text{ (D.L+50\% L.L)} &= 18.9 \text{ kN} \\
 A_{st} &= 9703 \text{ mm}^2/\text{mm} \\
 A_{sc} &= 7971 \text{ mm}^2/\text{mm} \\
 E_c &= 27386.12 \text{ N/mm}^2 \\
 E_s &= 200000 \text{ N/mm}^2 \\
 E_{ce} &= 13693 \text{ N/mm}^2 \\
 m &= 14.6 \\
 d &= 157 \text{ mm} \\
 D &= 205 \text{ mm} \\
 b &= 1000 \text{ mm} \\
 \text{Now, determine neutral axis at working load,} \\
 x &= 86.86 \text{ mm}
 \end{aligned}$$

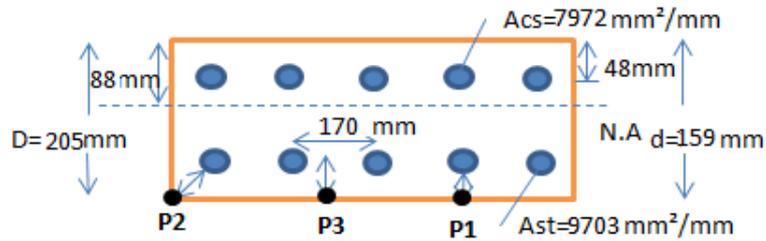


Figure 5.3: Cracked section of continuous slab panel

$$d-x = 70 \text{ mm}$$

$$I_c = 1703294291 \text{ mm}^4$$

$$\varepsilon_1 = 0.000192178$$

$$\varepsilon_m = 0.000148396$$

- (a) Crack width directly under a bar on tension face

$$a_{cr} (c_{min}) = 48 \text{ mm}$$

$$\begin{aligned} \text{Crack width} &= 0.02 \text{ mm} \\ &< 0.3 \text{ mm, Safe} \end{aligned}$$

- (b) Crack width at bottom corner of beam

$$a_{cr} = \sqrt{((48^2) + (48^2))} - (12/2) = 62 \text{ mm}$$

$$0.02 \text{ mm}$$

$$W_{cr} = \frac{3a_{cr}\varepsilon_m}{1+2\left(\frac{a_{cr}-C_{min}}{D-x}\right)} < 0.3 \text{ mm, Safe}$$

- (c) Crack width between midway of bars

$$a_{cr} = \sqrt{((125^2) + (48^2))} - (12/2) = 128 \text{ mm}$$

$$W_{cr} = \frac{3a_{cr}\varepsilon_m}{1+2\left(\frac{a_{cr}-C_{min}}{D-x}\right)} = 0.09 \text{ mm}$$

$$< 0.3 \text{ mm, Safe}$$

5.2.3 Diaphragm design

Internal diaphragm design

1) **Design force and moment:**

$$\text{Unfactored design moment, } M = 254 \text{ kNm}$$

$$\text{Unfactored design force, } V = 220 \text{ kN}$$

Using, basic load combination, $1.35D.L + 1.75W.C + 1.5L.L$

$$\text{Factored Design moment, } M_u = 377 \text{ kNm}$$

$$\text{Factored Design force, } V_u = 324 \text{ kN}$$

2) **Dimension**

$$\text{Length} = 2500 \text{ mm}$$

$$\text{Thickness} = 250 \text{ mm}$$

$$\text{Depth} = 1165 \text{ mm}$$

$$\text{Cover} = 40 \text{ mm}$$

3) **Depth check:**

$$R_{U \max} = 0.36 f_{ck} k_{u \max} (1 - 0.42 k_{u \max}) = 0.47$$

$$k_{u \max} = \frac{700}{1100 + 0.87 f_y} = 4.13$$

$$d_{req} = \sqrt{\frac{M_u}{R_{U \max} b}}$$

$$d_{required} = 604 \text{ mm}$$

$$d_{provided} = 1115 \text{ mm}$$

$d_{provided} > d_{required}$, hence safe.

4) **Steel :**

Longitudinal Reinforcement:

$$A_{st} = \frac{0.5 f_{ck}}{f_y} \left[1 - \sqrt{1 - \frac{4.6 M_u}{f_{ck} b d^2}} \right] \times b \times d$$

$$A_{st \text{ req}} = 985 \text{ mm}^2$$

$$\text{Provide 4 no.-20mm dia bar} = 1256 \text{ mm}^2$$

$$A_{st \text{ req}} > A_{st \text{ prov}} \quad \text{Safe}$$

Skin reinforcement

$$A_{st}(0.1\% \text{ of web area}) = 252.25 \text{ mm}^2$$

$$4 \text{ nos. Of } 10 \text{ mm @ } 300 \text{ mm c/c} = 314 \text{ mm}^2$$

(on each face)

5) Design of shear reinforcement:-

$$V_u = 327.20 \text{ kN}$$

$$p_t(\%) = 0.45$$

$$\tau_{uc} = 0.37 \text{ (From table 19 IS 456)}$$

$$\tau_v = 0.293 \text{ N/mm}$$

Shear resistance by concrete ,

$$V_{uc} = 107.76 \text{ kN}$$

Shear resistance by min r/f ,

$$V_{usv.min} = 116.5 \text{ kN}$$

$$V_{ur.min} = 107.76 + 116.5$$

$$V_{ur.min} = 224.26 \text{ kN} < V_u(327.2 \text{ kN})$$

Minimum shear reinforcement sufficient.

Min. Shear reinforcement required

$$A_{sv}/S = 0.4 * b / 0.87 * f_y = 276.96 \text{ mm}^2/\text{m}$$

$$V_{us} = V_u - V_{uc} = 219.44 \text{ kN}$$

$$A_{sv} \text{ (2-legged 10mm dia.)} = 157 \text{ mm}^2$$

$$\text{Spacing, } s = 280 \text{ mm} < 300 \text{ mm}$$

$$\text{Hence provide spacing, } s = 280 \text{ mm}$$

providing 10mm 2-legged striups@280mm c/c

$$A_{sv}/S \text{ (provided)} = 544 \text{ mm}^2 > (A_{sv}/S \text{ req} = 277 \text{ mm}^2)$$

6) Check for deflection

$$\text{allowable L/D ratio} = 2.5$$

$$\text{permissible L/D ratio} = 2500/1165 = 2.145 < 2.5 \text{ Hence safe}$$

7) Check for crack

$$\begin{aligned}
 MW &= 338 \text{ kN} \\
 A_{st} &= 1256 \text{ mm}^2 \\
 E_c &= 27386.12 \text{ N/mm}^2 \\
 E_s &= 200000 \text{ N/mm}^2 \\
 E_{ce} &= 13693.06 \text{ N/mm}^2 \\
 m &= 14.6 \\
 d &= 1116 \text{ mm} \\
 D &= 1165 \text{ mm}
 \end{aligned}$$

Determine neutral axis at working load,

$$\begin{aligned}
 x &= 337.92 \text{ mm} \\
 d-x &= 778.08 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 I_c &= 1.43\text{E}+10 \text{ mm}^4 \\
 \varepsilon_1 &= \frac{M_w(d-x)}{E_c e I_c} = 0.00114 \\
 \varepsilon_m &= \varepsilon_1 - \frac{b(D-x)(a-x)}{3E_s A_{st}(d-x)} = 0.0007
 \end{aligned}$$

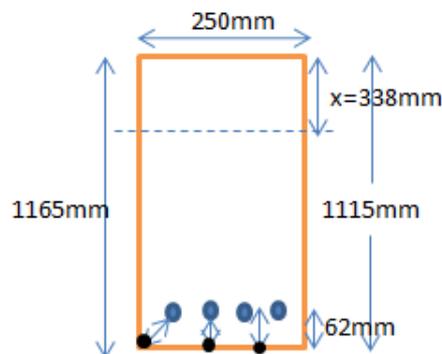


Figure 5.4: Cracked section of internal diaphragm

- (a) Crack width directly under a bar on tension face
 $a_{cr}(\text{cmin}) = \text{nominal cover} + \text{stirrp dia} = 50 \text{ mm}$

$$\begin{aligned} \text{Crack width} &= 0.11 \text{ mm} \\ &< 0.3 \text{ mm, Safe} \end{aligned}$$

- (b) Crack width at bottom corner of beam

$$\begin{aligned} a_{cr} &= \sqrt{(60^2) + (60^2)} - (20/2) = 70.9 \text{ mm} \\ &= 0.145 < 0.3 \text{ mm, Safe} \end{aligned}$$

- (b) Crack width between midway of bar

$$\begin{aligned} a_{cr} &= \sqrt{(30^2) + (60^2)} - (20/2) = 57 \text{ mm} \\ &= 0.12 < 0.3 \text{ mm, Safe} \end{aligned}$$

External diaphragm design

- 1) **Design force and moment:**

$$\text{Unfactored design moment, } M = 338 \text{ kNm}$$

$$\text{Unfactored design force, } V = 667 \text{ kNm}$$

Using, basic load combination, $1.35D.L + 1.75W.C + 1.5L.L$

$$\text{Factored Design moment, } M_u = 447 \text{ kNm}$$

$$\text{Factored Design force, } V_u = 894 \text{ kN}$$

- 2) **Dimension**

$$\text{Length} = 2500 \text{ mm}$$

$$\text{Thickness} = 250 \text{ mm}$$

$$\text{Depth} = 1165 \text{ mm}$$

$$\text{Cover} = 40 \text{ mm}$$

3) **Depth check:**

$$R_{U \max} = 0.36 f_{ck} k_{u \max} (1 - 0.42 k_{u \max}) = 0.479107$$

$$k_{u \max} = \frac{700}{1100 + 0.87 f_y} = 4.133149$$

$$d_{req} = \sqrt{\frac{M_u}{R_{U \max} b}}$$

$$d_{required} = 669 \text{ mm}$$

$$d_{provided} = 1115 \text{ mm}$$

$d_{provided} > d_{required}$, hence safe.

4) **Steel :****Longitudinal Reinforcement:**

$$A_{st} = \frac{0.5 f_{ck}}{f_y} \left[1 - \sqrt{1 - \frac{4.6 M_u}{f_{ck} b d^2}} \right] \times b \times d$$

$$A_{st \text{ req}} = 1225 \text{ mm}^2$$

$$\text{Provide 5 no.-20mm dia bar} = 1570 \text{ mm}^2$$

$$A_{st \text{ req}} > A_{st \text{ prov}} \quad \text{Safe}$$

Skin reinforcement

$$A_{st}(0.1\% \text{ of web area}) = 252.25 \text{ mm}^2$$

$$4 \text{ nos. Of 10 mm @300mm c/c} = 314 \text{ mm}^2$$

(on each face)

5) **Design of shear reinforcement:-**

$$V_u = 894 \text{ kN}$$

$$p_t(\%) = 0.378$$

$$\tau_{uc} = 0.37 \text{ (From table 19 IS 456)}$$

$$\tau_v = 0.8 \text{ N/mm}$$

Shear resistance by concrete ,

$$V_{uc} = 223 \text{ kN}$$

Shear resistance by min r/f ,

$$V_{usv.min} = 116.5 \text{ kN}$$

$$V_{ur.min} = 223 + 116.5$$

$$V_{ur.min} = 350\text{kN} < V_u(894\text{kN})$$

Minimum shear reinforcement sufficient.

Min. Shear reinforcement required

$$A_{sv}/S = 0.4*b/0.87*f_y = 277\text{mm}^2/\text{m}$$

$$V_{us} = V_u - V_{uc} = 660\text{kN}$$

$$A_{sv} \text{ (2-legged 10mm dia.)} = 157 \text{ mm}^2$$

$$\text{Spacing, } s = 90\text{mm} \leq 300\text{mm}$$

$$\text{Hence provide spacing, } s = 110\text{mm}$$

providing 10mm 2-legged striiups@110mmc/c

$$A_{sv}/S \text{ (provided)} = 1614\text{mm} > (A_{sv}/S \text{ req}=277\text{mm})$$

6) **Check for deflection**

$$\text{allowable L/D ratio} = 2.5$$

$$\text{permissible L/D ratio} = 2500/1165 = 2.145 < 2.5 \text{ Hence safe.}$$

7) **Check for crack**

$$M_w = 338 \text{ kN}$$

$$A_{st} = 1256 \text{ mm}^2$$

$$E_c = 27386 \text{ N/mm}^2$$

$$E_s = 200000 \text{ N/mm}^2$$

$$E_{ce} = 13693 \text{ N/mm}^2$$

$$m = 14.6$$

$$d = 1116 \text{ mm}$$

$$D = 1165 \text{ mm}$$

Determine neutral axis at working load,

$$x = 589 \text{ mm}$$

$$d-x = 527 \text{ mm}$$

$$2(d-x)/3 = 352 \text{ mm}$$

$$I_c = 22091429722 \text{ mm}^4$$

$$\varepsilon_1 = \frac{M_w(d-x)}{E_c e I_c} = 0.00129$$

$$\varepsilon_m = \varepsilon_1 - \frac{b(D-x)(a-x)}{3E_s A_{st}(d-x)} = 0.00108$$

(a) Crack width directly under a bar on tension face

$$a_{cr} (\text{cmin}) = \text{nominal cover} + \text{stirrp dia} = 50 \text{ mm}$$

$$\begin{aligned} \text{Crack width} &= 0.16 \text{ mm} \\ &< 0.3 \text{ mm, Safe} \end{aligned}$$

(b) Crack width at bottom corner of beam

$$\begin{aligned} a_{cr} &= \sqrt{(60^2) + (60^2)} - (20/2) = 70.9 \text{ mm} \\ &0.2 \text{ mm} \\ &< 0.3 \text{ mm, Safe} \end{aligned}$$

(b) Crack width at bar mid way

$$\begin{aligned} a_{cr} &= \sqrt{(30^2) + (60^2)} - (20/2) = 57 \text{ mm} \\ &0.12 \text{ mm} \\ &< 0.3 \text{ mm, Safe} \end{aligned}$$

5.2.4 External girder

At mid span section 0.5L=10m

1) **Check for flange depth:**

$$b_f = \frac{L_o}{6} + 6D_f + b_w$$

$$\begin{aligned} \text{bf} &= (14000/6) + 6217.5 + 300 \\ &= 3938.33 \text{ mm} \\ &> 2000 \text{ mm here bf sufficient} \end{aligned}$$

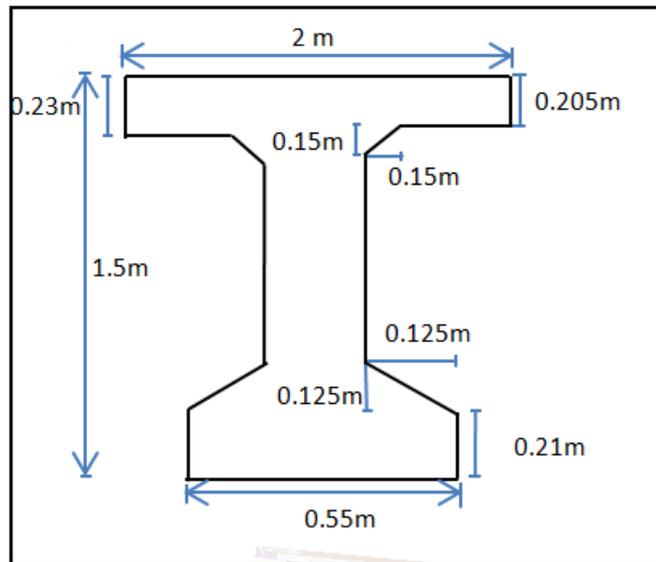


Figure 5.5: Sectional properties of external girder

2) **Check for depth:**

$$\begin{aligned} k_{\max} &= 700 / (1100 + 0.87415) \\ &= 0.48 \end{aligned}$$

$$\begin{aligned} R_{\max} &= 0.36 * 30 * 0.479 (1 - 0.42 * 0.479) \\ &= 4.13 \end{aligned}$$

$$d_{\text{required}} = \sqrt{\frac{Mu}{R U_{\max} b}}$$

$$\begin{aligned} d_{\text{req}} &= \sqrt{5980.2692175 * 10^6 / 4.133 * 2000} \\ &= 850.55 \text{ mm} \end{aligned}$$

3) **Check for width:**

$$\text{required width} = 2C_1 + N + (N-1)C_2$$

$$C_1 = 40 \text{ mm}$$

$$C_2 = 28 \text{ mm}$$

$$N = 8 \text{ nos.}$$

$$\text{width req} = 500 \text{ mm} < \text{provided } 550 \text{ mm, i.e. safe.}$$

4) **Exterior girder factored moments:**

Basic load combination for finding ultimate strength

$$[1.35DL+1.75WCL+1.5(LL)]$$

Total factored moment, $M_u = 5980 \text{ kNm}$ refer table4.8

Check for moment:(Limit State Of Collapse-Flexure)

Assume neutral axis, $x_u=D_f$

$$\begin{aligned} M_{ur1} &= 0.36f_{ck}b_fD_f(d - 0.42D_f) \\ &= 0.36*30*2000*217.5(1441.2-0.42*217.5) \\ &= 6341\text{kNm} \text{ ; } M_u \end{aligned}$$

$$A_{st} = \frac{0.5f_{ck}}{f_y} \left[1 - \sqrt{1 - \frac{4.6M_u}{f_{ck}bd^2}} \right] \times b \times d$$

$$\begin{aligned} A_{st} &= (0.5*30/415)(1-\sqrt{1 - 4.6 * 5980.27 * 10^6/30 * 2000 * 1441.2^2}) \\ &\quad *(2000*1441) \\ &= 12214.67\text{mm}^2 \end{aligned}$$

$$\begin{aligned} x_u &= (0.87*415*12214.67)/(0.36*30*2000) \\ &= 204.17 \text{ mm} \end{aligned}$$

Here,Neutral axis lies in flange.

Table 5.1: Longitudinal reinforcement at 0.5L external girder

Longitudinal Reinforcement:						
LAYER	Φ	No	Ast(mm ²)	Y(mm)	c.g(mm)	deff(mm)
4	-	-	-	-	-	-
3	28	4	2461.76	126	58.8	1441.2
2	28	8	4923.52	70		
1	28	8	4923.52	14		
TOTAL		20	12308.8			

At mid span section $0.25L=5m$

1) Check for flange depth:

$$b_f = \frac{L_o}{6} + 6D_f + b_w$$

$$\begin{aligned} b_f &= (14000/6)+6217.5+300 \\ &= 3938.33\text{mm} \\ &>2000\text{mm here } b_f \text{ sufficient} \end{aligned}$$

2) Check for depth:

$$\begin{aligned} k_{\text{max}} &= 700/(1100+0.87415) \\ &= 0.48 \end{aligned}$$

$$\begin{aligned} R_{\text{max}} &= 0.36*30*0.479(1-0.42*0.479) \\ &= 4.13 \end{aligned}$$

$$d_{\text{required}} = \sqrt{\frac{Mu}{RU_{\text{max}}b}}$$

$$\begin{aligned} d_{\text{req}} &= \sqrt{4758.038424 * 10^6 / 4.133 * 2000} \\ &= 758.68 \text{ mm} \end{aligned}$$

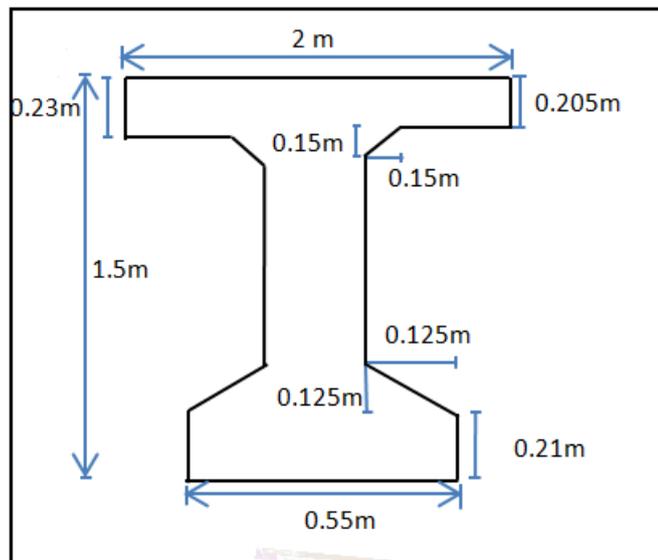


Figure 5.6: Sectional properties of internal girder

3) **Check for width:**

required width = $2C1 + N + (N-1)C2$

$$C1 = 40\text{mm}$$

$$C2 = 28\text{mm}$$

$$N = 8 \text{ nos.}$$

$$\text{width req} = 500\text{mm} < \text{provided } 550\text{mm, i.e. safe.}$$

4) **Exterior girder factored moments and shear:**

Basic load combination for finding ultimate strength

$$[1.35\text{DL} + 1.75\text{WCL} + 1.5(\text{LL})]$$

$$\text{Total factored moment, } M_u = 5980 \text{ kNm} \quad \text{refer table 4.8}$$

Check for moment:(Limit State Of Collapse-Flexure)

Assume neutral axis, $x_u = D_f$

$$\begin{aligned} M_{ur1} &= 0.36 f_{ck} b_f D_f (d - 0.42 D_f) \\ &= 0.36 * 30 * 2000 * 217.5 (1441.2 - 0.42 * 217.5) \\ &= 6341 \text{ KN.m} > M_u \end{aligned}$$

$$\begin{aligned} A_{st} &= \frac{0.5 f_{ck}}{f_y} \left[1 - \sqrt{1 - \frac{4.6 M_u}{f_{ck} b d^2}} \right] \times b \times d \\ A_{st} &= (0.5 * 30 / 415) (1 - \sqrt{1 - 4.6 * 5980.27 * 10^6 / 30 * 2000 * 1441.2^2}) * (2000 * 1441) \\ &= 12214.67 \text{ mm} \end{aligned}$$

$$\begin{aligned} x_u &= \frac{0.87 f_y A_{st}}{0.36 f_{ck} b_f} \\ x_u &= (0.87 * 415 * 12214.67) / (0.36 * 30 * 2000) \\ &= 204.17 \text{ mm} \end{aligned}$$

Here, Neutral axis lies in flange.

Table 5.2: Longitudinal reinforcement at 0.25L external girder

Longitudinal Reinforcement:						
LAYER	Φ	No	$A_{st}(mm^2)$	Y(mm)	c.g(mm)	deff(mm)
4	-	-	-	-	-	-
3	-	-	-	-	-	38
2	28	6	3692.64	70		
1	28	8	4923.52	14		
TOTAL		14	8616.16			

Shear Reinforcement Design

$A_{sv}/S = 0.4*b/0.87*f_y$ Min. Shear reinforcement required = $609.34mm^2/m$

Shear resistance by concrete, $V_{uc} = 332.9172$ KN

Shear resistance by min r/f, $V_{usv.min} = 172.944$ KN

Total resistance = 505.8612 KN < V_u

SECTION	S.F.(KN)	width-b(mm)	Eff. Depth(mm)	Long. Rf.	
				Nos.	dia
At support (0.00m)	875.8	550	1441.2	20	28
At 1/4th (5m)	554.8	300	1462	14	28

Table 5.3: Shear reinforcement of external girder

	Pt	T_{uc}	$T_v = T - T_c$	V_s	A_s/S	Provided striiups
At support (0.00m)	1.55	0.73	0.73	217.1	1683.18	2legged 12 ϕ stirrups 130mm c/c
At 1/4th (5m)	1.96	0.78	0.78	265.29	907.30	2legged 12 ϕ stirrups 240mm c/c

Check for deflection

i) Moment of inertia of Gross uncracked section without reinforcement:-

$$\begin{aligned} A_g &= (2000 \times 217.5) + (300 \times 947.5) + (335 \times 550) \\ &= 903500 \text{ mm}^2 \end{aligned}$$

$$\begin{aligned} Y &= (2000 \times 217.5 \times (1282.5 + (217.5/2))) + \\ &\quad (300 \times 947.5 \times 1282.5/2) + (550 \times 335 \times 335/2) / 903500 \\ &= 905.734 \text{ mm} \end{aligned}$$

$$\begin{aligned} I_g &= (1/12 \times 2000 \times 217.5^3) + (947.5^3 \times 300/12) + \\ &\quad (2000 \times 217.5 \times ((1282.5 - 905.73) + (217.5/2))^2) + \\ &\quad (947.5 \times 300 \times ((905.73 - (1282.5/2)))^2) + \\ &\quad (335 \times 550 \times (905.73 - (335/2))^2) \end{aligned}$$

$$I_g = 245819269089.716 \text{ mm}^4$$

$$y_t = 1500/2 = 750 \text{ mm}$$

$$f_{cr} = 3.834 \text{ N/mm}^2$$

$$M_r = 3.83 \times 245819269089.72 / 750$$

$$M_r = 1256647081.6 \text{ N.mm}$$

$$M_r = 1256.65 \text{ KN.m}$$

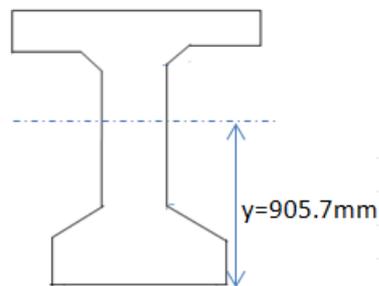


Figure 5.7: Centroidal distance from bottom of I-section

ii) Moment of inertia cracked section with reinforcement:-

$$\begin{aligned}
E_s &= 200000 \text{ N/mm} \\
E_c &= 27386.12 \text{ N/mm} \\
m &= E_s/E_c = 7.3 \\
x &= (2000 \cdot 217.5^2 / 2) + (7.3 \cdot 12308.8 \cdot 1441.2) / (2000 \cdot 217.5) + (7.3 \cdot 12308.8) \\
x &= 336.94 \text{ mm} \\
z &= d - (x/3) \\
z &= 1441.2 - (336.94/3) \\
z &= 1328.88 \text{ mm} \\
I_r &= (2000 \cdot 336.94^3 / 3) - ((2000 - 300) \cdot (336.94 - 217.5)^3 / 3) \\
&\quad + 7.3 \cdot 12308.8 \cdot (1441.2 - 336.94)^2 \\
&= 134147902636.459 \text{ mm}^4 \\
C &= 1.2 - (1256.65 / 4114.44) \cdot (1328.89 / 1441.2) \cdot (1 - (336.94 / 1441.2)) \cdot (300 / 2000) \\
&= 1.17 > 1, \text{ i.e. } I_r = I_{eff} \\
I_{eff} &= 134147902636.459 \text{ mm}^4 \\
\Delta_{D.L} &= \frac{5ML^2}{48E_c I_{eff}} \\
\Delta_{L.L} &= \frac{k(3-4k^2)}{48E_c I_{eff}}
\end{aligned}$$

Table 5.4: Deflection check for external girder

Section	Due to creep(mm)	Due to shrinkage(mm)	$\Delta_{D.L}$ (mm)	Total D.L(mm)	$\Delta_{D.Lallow}$ (mm)	$\Delta_{L.L}$ (mm)	$\Delta_{L.Lallow}$ (mm)
0.5L	5.76	0.3	16.26	22.32	57	1.37	25
0.25L	4.97	0.25	15.35	20.6		0.75	

5.2.5 Internal girder

Sectional properties:

Table 5.5: Crack check for external girder

Section	Crack under tension bar (mm)	Crack at corner (mm)	Crack at midway of bar (mm)	Permissible (mm)
0.5L	0.2	0.25	0.23	0.3
0.25L	0.16	0.23	0.19	0.3

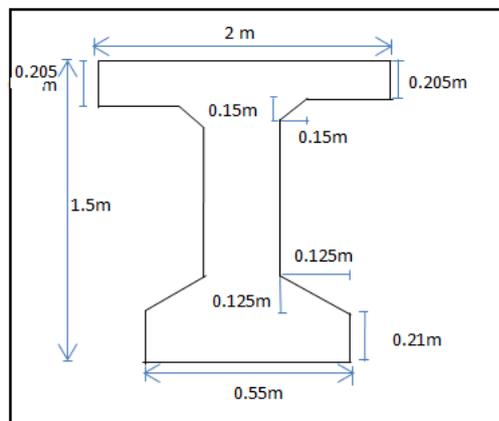


Figure 5.8: Sectional properties of internal girder

At mid span section $0.5L=10m$

1) Check for flange depth:

$$\begin{aligned}
 bf &= (14000/6)+6217.5+300 \\
 &= 3938.33\text{mm} \\
 &>2000\text{mm here bf sufficient}
 \end{aligned}$$

2) Check for depth:

$$\begin{aligned}
 k_{\text{max}} &= 700/(1100+0.87415) \\
 &= 0.48
 \end{aligned}$$

$$\begin{aligned}
 R_{\text{max}} &= 0.36*30*0.479(1-0.42*0.479) \\
 &= 4.13
 \end{aligned}$$

$$\begin{aligned}
 d_{\text{req}} &= \sqrt{5980.2692175 * 10^6 / 4.133 * 2000} \\
 &= 850.55\text{mm}
 \end{aligned}$$

3) **Check for width:**

$$\text{required width} = 2C1 + N + (N-1)C2$$

$$C1 = 40\text{mm}$$

$$C2 = 28\text{mm}$$

$$N = 8 \text{ nos.}$$

$$\text{width req} = 500\text{mm} < \text{provided } 550\text{mm, i.e. safe.}$$

4) **Exterior girder factored moments and shear:**

Basic load combination for finding ultimate strength

$$[1.35DL + 1.75WCL + 1.5(LL)]$$

$$\text{Total factored moment, } M_u = 5980 \text{ kNm}$$

refer table 4.8

Check for moment:(Limit State Of Collapse-Flexure)

Assume neutral axis, $x_u = D_f$

$$\begin{aligned} M_{ur1} &= 0.36 f_{ck} b_f D_f (d - 0.42 D_f) \\ &= 0.36 * 30 * 2000 * 205 (1462 - 0.42 * 205) \\ &= 6092.49 \text{ KN.m} > M_u \end{aligned}$$

$$A_{st} = \frac{0.5 f_{ck}}{f_y} \left[1 - \sqrt{1 - \frac{4.6 M_u}{f_{ck} b d^2}} \right] \times b \times d$$

$$A_{st} = 8180.3 \text{ mm}^2$$

$$x_u = \frac{0.87 f_y A_{st}}{0.36 f_{ck} b_f}$$

$$\begin{aligned} x_u &= (0.87 * 415 * 8180.35) / (0.36 * 30 * 2000) \\ &= 136.74 \text{ mm} \end{aligned}$$

Here, Neutral axis lies in flange.

Table 5.6: Longitudinal reinforcement at 0.5L internal girder

Longitudinal Reinforcement:						
LAYER	Φ	No	Ast(mm ²)	Y(mm)	c.g(mm)	deff(mm)
4	-	-	-	-	-	-
3	-	-	-	-	-	38
2	28	6	3692.64	70		
1	28	8	4923.52	14		
TOTAL		14	8616.16			

At mid span section 0.25L=5m1) **Check for flange depth:**

$$b_f = \frac{L_o}{6} + 6D_f + b_w$$

$$\begin{aligned} bf &= (14000/6)+6217.5+300 \\ &= 3938.33\text{mm} \\ &\text{;} 2000\text{mm here bf sufficient} \end{aligned}$$

2) **Check for depth:**

$$\begin{aligned} k_{\max} &= 700/(1100+0.87415) \\ &= 0.48 \end{aligned}$$

$$\begin{aligned} R_{\max} &= 0.36*30*0.479(1-0.42*0.479) \\ &= 4.13 \end{aligned}$$

$$d_{\text{required}} = \sqrt{\frac{Mu}{R_{U_{\max}} b}}$$

$$\begin{aligned} d_{\text{req}} &= \sqrt{2867.58 * 10^6 / 4.133 * 2000} \\ &= 588.98 \text{ mm} \end{aligned}$$

3) **Check for width:**

$$\text{required width} = 2C1 + N + (N-1)C2$$

$$C1 = 40\text{mm}$$

$$C2 = 28\text{mm}$$

$$N = 8 \text{ nos.}$$

$$\text{width req} = 500\text{mm} < \text{provided } 550\text{mm, i.e. safe.}$$

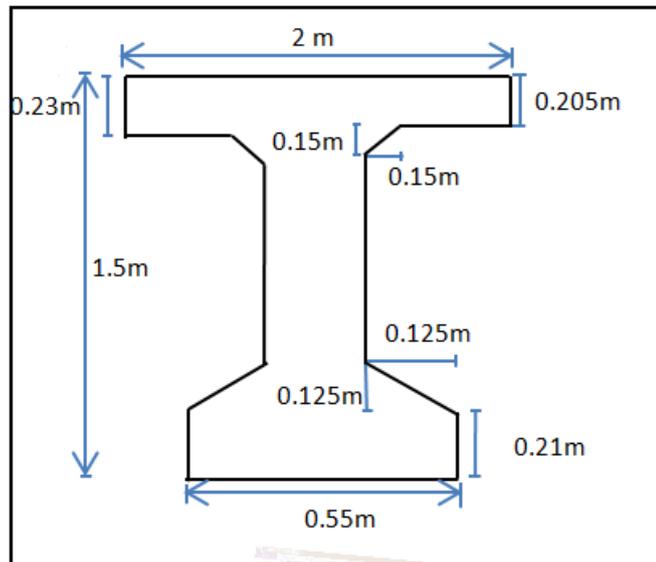


Figure 5.9: Sectional properties of internal girder

4) **Exterior girder factored moments and shear:**

Basic load combination for finding ultimate strength

$$[1.35DL+1.75WCL+1.5(LL)]$$

Total factored moment, $M_u = 2867.58 \text{ kNm}$

refer table 4.8

Check for moment:(Limit State Of Collapse-Flexure)

Assume neutral axis, $x_u = D_f$

$$\begin{aligned} M_{ur1} &= 0.36 f_{ck} b_f D_f (d - 0.42 D_f) \\ &= (0.36 * 30 * 2000 * 205 (1474.8 - 0.42 * 205)) \\ &= 6149.16 \text{ KN.m} > M_u \end{aligned}$$

$$\begin{aligned} A_{st} &= \frac{0.5 f_{ck}}{f_y} \left[1 - \sqrt{1 - \frac{4.6 M_u}{f_{ck} b d^2}} \right] \times b \times d \\ &= 5531.6 \text{ mm} \end{aligned}$$

$$x_u = \frac{0.87 f_y A_{st}}{0.36 f_{ck} b_f}$$

$$\begin{aligned} x_u &= (0.87 * 415 * 5531.56) / (0.36 * 30 * 2000) \\ &= 92.46 \text{ mm} \end{aligned}$$

Here, Neutral axis lies in flange.

Table 5.7: Longitudinal reinforcement at 0.25L internal girder

Longitudinal Reinforcement:						
LAYER	Φ	No	$A_{st}(mm^2)$	Y(mm)	c.g(mm)	deff(mm)
4	-	-	-	-	-	-
3	-	-	-	-	-	25
2	28	2	1230.88	70		
1	28	8	4923.52	14		
TOTAL		10	6154.40			

Shear Reinforcement Design

$A_{sv}/S = 0.4*b/0.87*f_y$ Min. Shear reinforcement required = $609.34mm^2/m$

Shear resistance by concrete, $V_{uc} = 332.9172$ KN

Shear resistance by min r/f, $V_{usv.min} = 172.944$ KN

Total resistance = 505.8612 KN $< V_u$

SECTION	S.F.(KN)	width-b(mm)	Eff. Depth(mm)	Long. Rf.	
				Nos.	dia
At support (0.00m)	704.83	550	1462	14	28
At 1/4th (5m)	628.41	300	1474.8	10	28

Table 5.8: Shear reinforcement of internal girder

	Pt	Tuc	$V_s = V_u - V_{uc}$	As/S	Provided striiups
At support (0.00m)	1.07	0.66	407.83	772.6226928	2legged 12 Φ stirrups 250mm c/c
At 1/4th (5m)	1.39	0.71	314.28	590.2	2legged 12 Φ stirrups 300mm c/c

Check for deflection

i) Moment of inertia of Gross uncracked section without reinforcement:-

$$\begin{aligned}
 A_g &= 882250 \\
 Y &= 895.7 \text{ mm} \\
 I_g &= 2.42239\text{E}+11 \text{ mm}^4 \\
 y_t &= 1500/2 = 750\text{mm} \\
 f_{cr} &= 3.834\text{N/mm} \\
 M_r &= 1238.3 \text{ KN.m}
 \end{aligned}$$

ii) Moment of inertia cracked section with reinforcement:-

$$\begin{aligned}
 E_s &= 200000\text{N/mm}^2 \\
 E_c &= 27386.12\text{N/mm}^2 \\
 m &= E_s/E_c=7.3 \\
 x &= 283.38 \text{ mm} \\
 z &= d -(x/3) \\
 z &= 1367.54 \text{ mm} \\
 I_r &= (2000*336.94^3/3)-((2000-300)*(336.94-217.5)^3/3) \\
 &\quad +7.3*12308.8*(1441.2-336.94)^2 \\
 &= 1.02308\text{E}+11 \text{ mm}^4 \\
 I_{eff} &= 8.76\text{E}+10\text{mm}^4 \\
 &= I_r > I_{eff}, \text{ i.e. } I_r = I_{eff} \\
 I_{eff} &= 134147902636.459\text{mm}^4
 \end{aligned}$$

$$\begin{aligned}
 \Delta_{D.L} &= \frac{5ML^2}{48E_c I_{eff}} \\
 \Delta_{L.L} &= \frac{k(3-4k^2)}{48E_c I_{eff}}
 \end{aligned}$$

Table 5.9: Deflection check for external girder

Section	Due to creep(mm)	Due to shrinkage(mm)	$\Delta_{D.L}$ (mm)	Total D.L(mm)	$\Delta_{D.Lallow}$ (mm)	$\Delta_{L.L}$ (mm)	$\Delta_{L.Lallow}$ (mm)
0.5L	7.01	0.32	23.27	30	57	2.7	25
0.25L	6	0.25	21		27	2.4	

Table 5.10: Crack check for internal girder

Section	Crack under tension bar(mm)	Crack at corner (mm)	Crack at midway of bar(mm)	Permissible (mm)
0.5L	0.16	0.211	0.195	0.3
0.25L	0.13	0.170	0.157	0.3

5.3 Load and resistance factor design

5.3.1 Cantilever Slab Design

1) **Design force and moment:**

$$\text{Unfactored design moment, } M = 59 \text{ kNm}$$

$$\text{Unfactored design force, } V = 90 \text{ kN}$$

Using, basic load combination, $1.25D.L + 1.5W.C + 1.75L.L$

$$\text{Factored Design moment, } M_u = 95 \text{ kNm}$$

$$\text{Factored Design force, } V_u = 146 \text{ kN}$$

2) **Dimension:**

$$\text{Thickness, } D = 230 \text{ mm}$$

$$\text{Effective cover, } d' = 30 \text{ mm}$$

3) **Depth check:**

$$D_{req} = 1.2 \frac{S+3000}{30} = 147 \text{ mm}$$

$$d_{req} = 1.2 * ((2500 * 1000) + 3000) / 30 = 220 \text{ mm} > 175 \text{ mm}$$

Adding sacrificial surfacing 15mm + 25mm to overhanging portion of slab

$$d_{provided} = 260 - 30 - 12 / 2 = 224 \text{ mm}$$

$d_{provided} > d_{required}$, hence safe.

4) **Strength Limit State :**

Using basic load combination, $1.25D.L + 1.5W.C + 1.75L.L$

Assuming the lever arm $(d - a/2)$ is independent of A_s , we can replace it by jd and solve for approximate A_s required to resist $\phi M_n = M_u$

$$j = 0.92$$

$$\phi = 0.9 \text{ (AASHTO, A5.5.4.2.1)}$$

$$A_s = \frac{M_u / \phi}{f_y j d} = 1167.460968 \text{ mm}^2$$

Maximum reinforcement is limited by the ductility requirement

$$\text{neutral axis, } a \geq 0.35d = 78.4 \text{ mm}$$

$$a = \frac{A_s f_y}{0.85 f_c b} = 14 \text{ mm} < 78.4 \text{ mm safe.}$$

Minimum reinforcement (A5.7.3.3.2)

$$\rho = \frac{A_s}{bd} \geq 0.03 \frac{f_c}{f_y} = 0.003860651 \geq 0.002168675 \text{ ok}$$

$$\text{min } A_s = 655.8072289 \text{ mm}^2$$

Moment capacity check:-

$$\phi M_n = \phi A_s f_y (d - \frac{a}{2}) = 94.61 \text{ kNm} > 89.6 \text{ kNm}$$

Main Steel:-

$$A_{st} = 1167.460968 \text{ mm}^2$$

$$\text{Provide } 12 \text{ mm @ } 160 \text{ c/c} = 706.8 \text{ mm}^2 \text{ (top r/f)}$$

$$\text{Provide } 12 \text{ mm @ } 200 \text{ c/c} = 565.4 \text{ mm}^2 \text{ bottom r/f)}$$

$$\text{total } A_{stpr} = 1272.345025 \text{ mm}^2$$

Distribution Steel:-

$$\text{percentage} = \frac{3540}{\sqrt{S_e}} \geq 67\%$$

$$S_e = 1200 \text{ mm}$$

percentage = 110.85 % > 67% use 67% dist $A_s = 852.5 \text{ mm}^2$

Prov. Half steel at top and half at bottom

Prov. 12 mm dia @ 200 mm = 565.2 mm^2

at top and bottom

Total steel provided = 1130.4 mm > 852.5 mm

Prov. Half steel at top and half at bottom

$V_u < 0.5\phi V_c$ Hence no, need to provide shear reinforcement.

5) **Control of cracking:**

$$f \leq f_{sa} = \frac{Z}{(d_c A)^{1/3}}$$

$$Z = 30000 \text{ N/mm}$$

$$bx^2 + (m - 1)Asc(x - d) = mAst(d - x)$$

$$x = 98.6 \text{ mm}$$

$$I_{cr} = bx^3/3 + (m - 1)Asc(x - d')^2 + mAst(d - x)^2$$

$$I_{cr} = 566759743.7 \text{ mm}^4$$

The tensile stress in bottom steel becomes

$$f_s = n \left(\frac{M_y}{I_{cr}} \right)$$

$$f_s = 195 \text{ MPa}$$

$$f_{sa} = 292 \text{ MPa} > 0.6f_y$$

$$f_{sa} = 0.6f_y = 249 \text{ MPa} > f_s = 195 \text{ MPa}$$

5.3.2 Continous Slab panel design

1) **Design force and moment:**

$$\text{Unfactored design moment, } M_x = 35 \text{ kNm}$$

$$\text{Unfactored design moment, } M_y = 24 \text{ kNm}$$

$$\text{Unfactored design force, } V = 95 \text{ kN}$$

Using, basic load combination, $1.35D.L + 1.75W.C + 1.5L.L$

$$\text{Factored Design moment, } M_{ux} = 60 \text{ kNm}$$

$$\text{Factored Design moment, } M_{uy} = 40 \text{ kNm}$$

$$\text{Factored Design force, } V_u = 165 \text{ kN}$$

2) **Dimension:**

$$\text{Thickness, } D = 235 \text{ mm}$$

$$\text{Slab panel size,} = 2.5 \text{ m x 4 m}$$

$$\text{Effective cover, } d' = 30 \text{ mm}$$

3) **Depth check:**

$$D_{req} = 1.2 \frac{S+3000}{30} = 147 \text{ mm}$$

$$d_{req} = 1.2 * ((2500 * 1000) + 3000) / 30 = 220 \text{ mm} > 175 \text{ mm}$$

Adding sacrificial surfacing 15mm

$$d_{provided} = 235 - 30 - 12 / 2 = 199 \text{ mm}$$

$d_{provided} > d_{required}$, hence safe.

4) **Strength Limit State :**

Using basic load combination, $1.25D.L + 1.5W.C + 1.75L.L$

Assuming the lever arm $(d - a/2)$ is independent of A_s , we can replace it by jd and

solve for approximate A_s required to resist $\phi M_n = M_u$

$$j = 0.92$$

$$\phi = 0.9 \text{ (AASHTO, A5.5.4.2.1)}$$

$$A_{sx} = \frac{M_u / \phi}{f_y j d} = 839.7 \text{ mm}^2$$

$$A_{sy} = \frac{M_u / \phi}{f_y j d} = 540.5 \text{ mm}^2$$

Maximum reinforcement is limited by the ductility requirement neutral axis,

$$a \geq 0.35d = 69.65 \text{ mm}$$

$$a = \frac{A_s f_y}{0.85 f_c b} = 14 \text{ mm} < 69.65 \text{ mm safe.}$$

Minimum reinforcement (A5.7.3.3.2)

$$\rho = \frac{A_s}{bd} \geq 0.03 \frac{f_c}{f_y} = 0.003860651 \geq 0.002168675 \text{ ok}$$

$$\text{min } A_s = 427 \text{ mm}^2$$

Moment capacity check:-

$$\phi M_n = \phi A_s f_y (d - \frac{a}{2}) = 60.27 \text{ kNm } i, 57.42 \text{ kNm}$$

Main Steel:-

$$A_{st} = 839.7 \text{ mm}^2$$

$$\text{Provide } 12 \text{ mm @ } 200 \text{ mm/c} = 565.4 \text{ mm}^2 \text{ (top r/f)}$$

$$\text{Provide } 12 \text{ mm @ } 190 \text{ mm/c} = 595.2491344 \text{ mm}^2 \text{ bottom r/f)}$$

$$\text{total } A_{stpr} = 1160.7 \text{ mm}^2$$

$$\text{Provide } 10 \text{ mm @ } 120 \text{ mm/c} = 655 \text{ mm}^2 \text{ extra top bar}$$

Distribution Steel:-

$$\text{percentage} = \frac{3540}{\sqrt{S_e}} \geq 67\%$$

$$S_e = 1200 \text{ mm}$$

$$\text{percentage} = 110.85 \% > 67\% \text{ use } 67\% \text{ dist } A_s = 852.5 \text{ mm}^2$$

Prov. Half steel at top and half at bottom

$$\text{Prov. } 12 \text{ mm dia @ } 200 \text{ mm} = 565.2 \text{ mm}^2$$

at top and bottom

$$\text{Total steel provided} = 1130.4 \text{ mm} > 852.5 \text{ mm}$$

Prov. Half steel at top and half at bottom

$V_u < 0.5\phi V_c$ Hence no, need to provide shear reinforcement.

5) Control of cracking:

$$f \leq f_{sa} = \frac{Z}{(d_c A)^{1/3}}$$

$$Z = 30000 \text{ N/mm}$$

$$bx^2 + (m - 1)Asc(x - d) = mAst(d - x)$$

$$x = 84.80 \text{ mm}$$

$$I_{cr} = bx^3/3 + (m - 1)Asc(x - d')^2 + mAst(d - x)^2$$

$$I_{cr} = 1416439093 \text{ mm}^4$$

The tensile stress in bottom steel becomes

$$f_s = n \left(\frac{M_y}{I_{cr}} \right)$$

$$f_s = 175 \text{ MPa}$$

$$f_{sa} = 250 \text{ MPa} > 0.6f_y$$

$$f_{sa} = 0.6f_y = 249 \text{ MPa} > f_s = 195 \text{ MPa}$$

Hence, safe.

5.3.3 Diaphragm design

External diaphragm

1) **Design force and moment:**

$$\text{Unfactored design moment, } M = 338 \text{ kNm}$$

$$\text{Unfactored design force, } V = 667 \text{ kNm}$$

Using, basic load combination, $1.35D.L + 1.75W.C + 1.5L.L$

$$\text{Factored Design moment, } M_u = 408 \text{ kNm}$$

$$\text{Factored Design force, } V_u = 826 \text{ kN}$$

2) **Dimension**

$$\text{Length} = 2500 \text{ mm}$$

$$\text{Thickness} = 300 \text{ mm}$$

$$\text{Depth} = 1165 \text{ mm}$$

$$\text{Cover} = 40 \text{ mm}$$

3) **Depth check:**

$$D = 0.7L = 0.7 * 2500$$

$$d_{req} = 560 \text{ mm}$$

$$d_{provided} = 1115 \text{ mm}$$

$d_{provided} > d_{required}$, hence safe.

4) **Steel :**

Longitudinal Reinforcement:

$$A_{st} = \frac{M_u / \phi}{f_y j d}$$

$$\begin{aligned} \text{Ast req} &= 1018 \text{ mm}^2 \\ \text{Provide 4 no.-20mm dia bar} &= 1256 \text{ mm}^2 \\ \text{Ast req} > \text{Ast prov} &\quad \text{Safe} \end{aligned}$$

5) Check for shear: De-

Skin reinforcement

$$4\text{nos. Of } 10 \text{ mm @}300\text{mm}/\text{c} = 314 \text{ mm}^2$$

(on each face)

sign of shear reinforcement:- $V_u = 826 \text{ kN}$

$$A_s = 1256 \text{ mm}^2$$

$$a = 408 \text{ mm}$$

$$d_e = 1115 \text{ mm}$$

$$d_v = d - a/2 = 1003.50 \text{ mm}$$

$$d_v = 0.9 d_e = 1253.52 \text{ mm}$$

$$d_v = 0.72h = 835.2 \text{ mm}$$

Select the maximum one.

Calculate the shear stress ratio

$$v = \frac{V_u}{\phi_n b_v d_v} = 3.18 \text{ Mpa}$$

$$v/f_c = 0.106119266$$

Calculate strain ,

estimate $\theta = 40^\circ$ and $\cot \theta = 1.192$ for trial.

$$\varepsilon_x = \frac{M_u/d_v + 0.5V_u \cot \theta}{E_s A_s d} = 0.001956524$$

$$\beta = 2.2$$

Calculate the required web reinforcement $V_s = \frac{V_u}{\phi_v} - 0.083\beta\sqrt{f_c}b_v d_v$

$$V_s = 603.24 \text{ kN}$$

Calculate the required spacing of stirrups $s \geq \frac{A_v f_y d_v}{V_s} \cot \theta = 178 \text{ mm}$

$$s \geq \frac{A_v f_y}{0.083\sqrt{f_c} b_v} = 687 \text{ mm}$$

$$V_u < 0.1f_c b_v d_v = 864 \text{ kN Safe.}$$

providing 10 mm 2-legged stirrups 140 mm

Internal diaphragm1) **Design force and moment:**

$$\text{Unfactored design moment, } M = 272 \text{ kNm}$$

$$\text{Unfactored design force, } V = 676 \text{ kNm}$$

Using, basic load combination, $1.35D.L + 1.75W.C + 1.5L.L$

$$\text{Factored Design moment, } M_u = 468 \text{ kNm}$$

$$\text{Factored Design force, } V_u = 402 \text{ kN}$$

2) **Dimension**

$$\text{Length} = 2500 \text{ mm}$$

$$\text{Thickness} = 300 \text{ mm}$$

$$\text{Depth} = 1165 \text{ mm}$$

$$\text{Cover} = 40 \text{ mm}$$

3) **Depth check:**

$$D = 0.7L = 0.7 * 2500$$

$$d_{req} = 560 \text{ mm}$$

$$d_{provided} = 1115 \text{ mm}$$

$d_{provided} > d_{required}$, hence safe.

4) **Steel :****Longitudinal Reinforcement:**

$$A_{st} = \frac{M_u / \phi}{f_y j d}$$

$$A_{st \text{ req}} = 1018 \text{ mm}^2$$

$$\text{Provide 4 no.-20mm dia bar} = 1256 \text{ mm}^2$$

$$A_{st \text{ req}} > A_{st \text{ prov}} \quad \text{Safe}$$

Skin reinforcement

$$4 \text{ nos. Of } 10 \text{ mm @ } 300 \text{ mm } / \text{c} = 314 \text{ mm}^2$$

(on each face)

5) **Check for shear:** Design of shear reinforcement:- $V_u = 826 \text{ kN}$

$$A_s = 1256 \text{ mm}^2$$

$$a = 408 \text{ mm}$$

$$d_e = 1115 \text{ mm}$$

$$d_v = d - a/2 = 1003.50 \text{ mm}$$

$$d_v = 0.9 d_e = 1253.52 \text{ mm}$$

$$d_v = 0.72h = 835.2 \text{ mm}$$

Select the maximum one.

Calculate the shear stress ratio

$$v = \frac{V_u}{\phi_n b_v d_v} = 3.18 \text{ Mpa}$$

$$v/f_c = 0.001108554$$

Calculate strain ,

estimate $\theta = 40^\circ$ and $\cot \theta = 1.192$ for trial.

$$\varepsilon_x = \frac{M_u/d_v + 0.5V_u \cot \theta}{E_s A_s d} = 0.001108554$$

$$\beta = 2.2$$

Calculate the required web reinforcement $V_s = \frac{V_u}{\phi_v} - 0.083\beta\sqrt{f_c}b_v d_v$

$$V_s = 205 \text{ kN}$$

Calculate the required spacing of stirrups $s \geq \frac{A_v f_y d_v}{V_s} \cot \theta = 523 \text{ mm}$

$$s \geq \frac{A_v f_y}{0.083\sqrt{f_c} b_v} = 687 \text{ mm}$$

$$V_u < 0.1f_c b_v d_v = 864 \text{ kN Safe.}$$

providing 10 mm 2-legged stirrups 200 mm

5.3.4 External girder

1) Check for flange depth:

$$bf \geq 1/4 \text{ of effective span} = 3500 \text{ mm}$$

$$bf \geq 6t_s + b_w = 3320 \text{ mm}$$

$$bf \geq \text{Width of overhang} = 1500 + 3320/2 = 3160 \text{ mm}$$

$$bf = 2000 \text{ mm o.k}$$

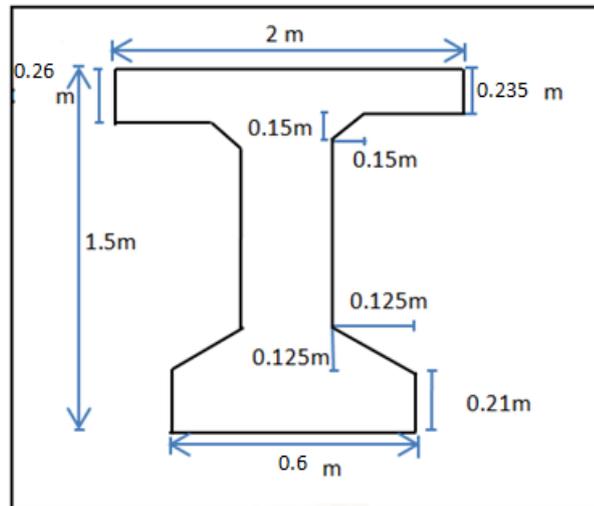


Figure 5.10: Sectional properties of external girder

2) Check for depth:

$$D_{req} = 0.7L$$

$$D_{req} = 1400 \text{ mm}$$

$$D_{prov} = 1500 \text{ mm o.k}$$

3) Check for width:

$$b_{min} = 2(C + d_s) + Nd_b + (N - 1)(1.5d_b)$$

$$C = 40 \text{ mm}$$

$$d_b = 28 \text{ mm}$$

$$d_s = 12 \text{ mm}$$

$$N = 8$$

$$\text{width req} = 598 \text{ mm} < 600 \text{ mm sufficient width}$$

4) Select Resistance Factors

i) Strength Limit State = ϕ (A5.5.42.1)

$$\text{Flexure and tension} = 0.9$$

Shear and torsion = 0.9

ii) Nonstrength Limit States = 1 (A1.3.2.1)

5) Select Load Modifiers

	Strength	Service	Fatigue
Ductility, η_D	0.95	1	1
Redundancy, η_R	0.95	1	1
Imoportance, η_I	1.05	N/A	N/A
$\eta = \eta_D * \eta_R * \eta_I$	0.95	1	1

6) **Multiple presence factor:**

No.of Loaded Lanes	m
1	1.2
2	1

7) Dynamic Load Allowance: 33%

8) Select Applicable Load Combination:

Strength -I Limit State

$$U = 1.25DC + 1.5DW + 1.75(LL + IM) \text{ (ref table 4.11)}$$

Service- I Limit State

$$U = 1(DC + DW) + 1(LL + IM)$$

9) Exterior girder factored moments and shear:

$$U = \eta [1.25DC + 1.5DW + 1.75(LL + IM)]$$

$$\text{Total factored moment} = 7789 \text{ kNm}$$

10) Check for Neutral axis position

$$\omega = \rho \frac{f_y}{f_c} = 0.03$$

$$c = \frac{1.18\omega d}{\beta_1} = 57 \ll D_f$$

Therefore, neutral axis lies in flange.

Table 5.11: Longitudinal reinforcement at 0.5L external girder

Longitudinal Reinforcement:						
LAYER	Φ	No	Ast(mm ²)	Y(mm)	c.g(mm)	deff(mm)
4	28	6	3692.64	222		
3	28	6	3692.64	166	130	1370
2	28	8	4923.52	110		
1	28	8	4923.52	54		
TOTAL		28	17232.32			

Assuming the lever arm ($d-a/2$) is independent of A_s , we can replace it by jd and solve for approximate A_s required to resist $\phi M_n = M_u$

$$j = 0.9 \quad A_s = \frac{M_u / \phi}{f_y j d} = 16913 \text{ mm}^2$$

Maximum reinforcement is limited by the ductility requirement

$$a \geq 0.35d = 478.66 \text{ mm} \quad a = \frac{A_s f_y}{0.85 f_c b} = 137 \text{ mm} < 478.66 \text{ mm safe.}$$

Minimum reinforcement (A5.7.3.3.2)

$$\rho = \frac{A_s}{bd} \geq 0.03 \frac{f_c}{f_y} = 0.006172884 \geq 0.002168675$$

$$\text{min } A_s = 5942 \text{ mm}^2$$

Moment capacity check:-

$$\phi M_n = \phi A_s f_y \left(d - \frac{a}{2}\right) = 8219 \text{ kNm} \quad ; 7789 \text{ kNm}$$

11) **Check for shear:** Design of shear reinforcement:- $V_u = 1223 \text{ kN}$ (at support)

$$A_s = 17232.32 \text{ mm}^2$$

$$a = 137.6 \text{ mm}$$

$$d_e = 1370 \text{ mm}$$

$$d_v = d - a/2 = 1301.18 \text{ mm}$$

$$d_v = 0.9 d_e = 1233.00 \text{ mm}$$

$$d_v = 0.72h = 792 \text{ mm}$$

Select the maximum one.

Calculate the shear stress ratio

$$v = \frac{V_u}{\phi_n b_v d_v} = 3.06 \text{ Mpa}$$

$$v/f_c = 0.102066862$$

Calculate strain ,

estimate $\theta = 40^\circ$ and $\cot \theta = 1.192$ for trial.

$$\varepsilon_x = \frac{M_u/d_v + 0.5V_u \cot \theta}{E_s A_s d} = 0.000185719$$

$$\beta = 2.4$$

Calculate the required web reinforcement $V_s = \frac{V_u}{\phi_v} - 0.083\beta\sqrt{f_c}b_v d_v$

$$V_s = 769.36 \text{ kN}$$

Calculate the required spacing of stirrups $s \geq \frac{A_v f_y d_v}{V_s} \cot \theta = 189 \text{ mm}$

$$s \geq \frac{A_v f_y}{0.083\sqrt{f_c} b_v} = 687 \text{ mm}$$

$$V_u < 0.1f_c b_v d_v = 1171 \text{ kN Safe.}$$

providing 12 mm 2-legged stirrups 140 mm (at support)

12) Control of cracking:

Elastic -Cracked transformed section analysis required to check crack control (A5.7.3.4)

$$E_s = 200000 \text{ N/mm}$$

$$E_c = 26290.68276 \text{ N/mm}$$

$$n = E_s/E_c = 7.6$$

$$f \leq f_{sa} = \frac{Z}{(d_c A)^{1/3}}$$

$$Z = 30000 \text{ N/mm}$$

$$bx^2 + (m - 1)Asc(x - d) = mAst(d - x)$$

$$x = 381 \text{ mm}$$

$$I_{cr} = bx^3/3 + mAst(d - x)^2$$

$$I_{cr} = 1.E+11 \text{ mm}^4$$

The tensile stress in bottom steel becomes

$$f_s = n\left(\frac{M_y}{I_{cr}}\right)$$

$$f_s = 226.31 \text{ MPa}$$

$$f_{sa} = 470.03 \text{ MPa} > 0.6f_y$$

$$f_{sa} = 0.6f_y = 249 \text{ MPa} > f_s = 250.60 \text{ MPa}$$

Hence, here, fsjfsa, safe.

13) **Deflection check:**

i) Moment of inertia of Gross uncracked section without reinforcement:-

$$\begin{aligned} A_g &= (2000 \cdot 235) + (350 \cdot 930) + (335 \cdot 600) \\ &= 996500 \text{ mm}^2 \end{aligned}$$

$$\begin{aligned} Y &= (2000 \cdot 235 \cdot (1265 + (235/2))) + (350 \cdot 930 \cdot 1265/2) + (600 \cdot 335 \cdot 335/2) / 996500 \\ Y &= 892 \text{ mm} \end{aligned}$$

$$\begin{aligned} I_g &= (1/12 \cdot 2000 \cdot 235^3) + (930^3 \cdot 350/12) + (2000 \cdot 235 \cdot ((1265 - 892.44) + \\ &(235/2))^2) + (930 \cdot 350 \cdot ((892.44 - (1265/2)))^2) + \\ &(335 \cdot 600 \cdot (892.44 - (335/2))^2) \end{aligned}$$

$$I_g = 2.66125\text{E}+11 \text{ mm}^4$$

$$y_t = 1500/2 = 750 \text{ mm}$$

$$f_{cr} = 3.45 \text{ N/mm}^2$$

$$M_r = 3.45 \cdot 266124813631.04 / 750$$

$$M_r = 1224405534 \text{ Nmm}$$

$$M_r = 1224.4 \text{ kNm}$$

ii) Moment of inertia cracked section without reinforcement:-

$$E_s = 200000 \text{ N/mm}^2$$

$$E_c = 26290.68276 \text{ N/mm}^2$$

$$m = E_s/E_c = 7.61$$

$$x = 305 \text{ mm}$$

$$I_{cr} = 1.24692\text{E}+11 \text{ mm}^4$$

$$I_e = \left(\frac{M_{cr}}{M_a} \right)^3 I_g + \left[1 - \left(\frac{M_{cr}}{M_a} \right)^3 \right] I_{cr} \leq I_g$$

$$I_{eff} = 1.3013\text{E}+11 \text{ mm}^2 < I_{gr} \text{ ok}$$

$$I_{eff} = ((1163.64/3697.6)^3 * 2.529E + 11) + ((1 - (1163.64/3697.6)^3) * 6.07E + 10)$$

$$EI = 3.4212E+15 \text{ Nmm}^2$$

$$\Delta_{D.L} = 14.15 \text{ mm} < 57\text{m}$$

$$\Delta_{D.L} = 3.2 \text{ mm} < 25\text{m}$$

5.3.5 Internal girder

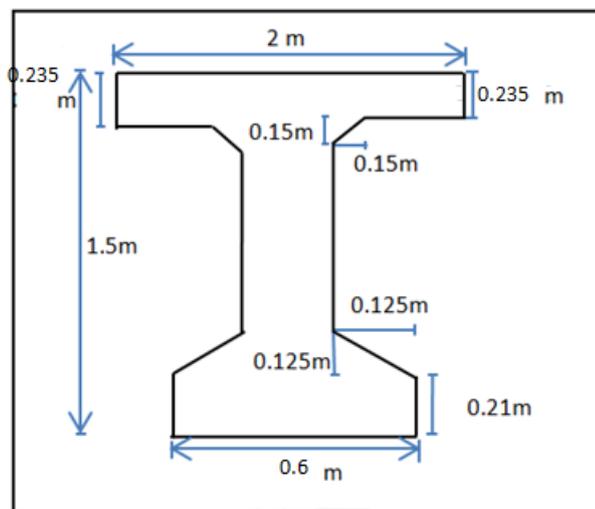


Figure 5.11: Sectional properties of internal girder

1) Check for flange depth:

$$bf \geq 1/4 \text{ of effective span} = 3500 \text{ mm}$$

$$bf \geq 12t_s + b_w = 3320 \text{ mm}$$

$$bf \geq \text{Average spacing} = 2500 \text{ mm}$$

$$bf = 2000 \text{ mm o.k}$$

2) Check for depth:

$$D_{req} = 0.7L$$

$$D_{req} = 1400 \text{ mm}$$

Dprov = 1500 mm o.k

3) Check for width:

$$b_{min} = 2(C + d_s) + Nd_b + (N - 1)(1.5d_b)$$

$$C = 40 \text{ mm}$$

$$d_b = 28 \text{ mm}$$

$$d_s = 12 \text{ mm}$$

$$N = 8$$

width req = 598 mm <600mm sufficient width

4) Select Resistance Factors

i) Strength Limit State = ϕ (A5.5.42.1)

Flexure and tension = 0.9

Shear and torsion = 0.9

ii) Nonstrength Limit States = 1 (A1.3.2.1)

5) Select Load Modifiers

	Strength	Service	Fatigue
Ductility, η_D	0.95	1	1
Redundancy, η_R	0.95	1	1
Impoatance, η_I	1.05	N/A	N/A
$\eta = \eta_D * \eta_R * \eta_I$	0.95	1	1

6) **Multiple presence factor:**

No.of Loaded Lanes	m
1	1.2
2	1

7) Dynamic Load Allowance: 33%

8) Select Applicabile Load Combination:

Strength -I Limit State $U = 1.25DC+1.5DW+1.75(LL+IM)$

Service- I Limit State

$$U = 1(DC+DW)+1(LL+IM)$$

9) Exterior girder factored moments and shear:

$$U = \eta[1.25DC+1.5DW+1.75(LL+IM)]$$

Total factored moment = 4773.94 kNm

10) Check for Neutral axis position

$$\omega = \rho \frac{f_y}{f_c} = 0.03$$

$$c = \frac{1.18\omega d}{\beta_1} = 49.647 \ll D_f$$

Therefore, neutral axis lies in flange.

Assuming the lever arm $(d-a/2)$ is independent of A_s , we can replace it by jd

and solve for approximate A_s required to resist $\phi M_n = M_u$

$$j = 0.9 \quad A_s = \frac{M_u/\phi}{f_y j d} = 10126 \text{ mm}^2$$

Maximum reinforcement is limited by the ductility requirement

$$a \geq 0.35d = 490 \text{ mm} \quad a = \frac{A_s f_y}{0.85 f_c b} = 82 \text{ mm} < 490 \text{ mm safe.}$$

Minimum reinforcement (A5.7.3.3.2)

$$\rho = \frac{A_s}{bd} \geq 0.03 \frac{f_c}{f_y} = 0.003610292 \geq 0.002168675$$

$$\min A_s = 6082.8 \text{ mm}^2$$

Moment capacity check:-

$$\phi M_n = \phi A_s f_y \left(d - \frac{a}{2}\right) = 5148 \text{ kNm} > 4773.94 \text{ kNm}$$

11) **Check for shear:**

Design of shear reinforcement:-

$$V_u = 1312 \text{ kN (at support)}$$

$$A_s = 11077.92 \text{ mm}^2$$

$$a = 82.4 \text{ mm}$$

Table 5.12: Longitudinal reinforcement at 0.5L internal girder

Longitudinal Reinforcement:						
LAYER	Φ	No	Ast(mm ²)	Y(mm)	c.g(mm)	deff(mm)
4	-	-	-	-	-	-
3	28	4	2461.76	166	130	1370
2	28	6	3692.64	110		
1	28	8	4923.52	54		
TOTAL		18	11077.92			

$$d_e = 1402 \text{ mm}$$

$$d_v = d-a/2 = 1328.80 \text{ mm}$$

$$d_v = 0.9 d_e = 1262.20 \text{ mm}$$

$$d_v = 0.72h = 792 \text{ mm}$$

Select the maximum one.

Calculate the shear stress ratio

$$v = \frac{V_u}{\phi_n b_v d_v} = 3.66 \text{ Mpa}$$

$$v/f_c = 0.121899551$$

Calculate strain ,

estimate $\theta = 40^\circ$ and $\cot \theta = 1.192$ for trial.

$$\epsilon_x = \frac{M_u/d_v + 0.5V_u \cot \theta}{E_s A_s d} = 0.000352353$$

$$\beta = 2.4$$

Calculate the required web reinforcement

$$V_s = \frac{V_u}{\phi_v} - 0.083\beta\sqrt{f_c}b_v d_v$$

$$V_s = 1022 \text{ kN}$$

Calculate the required spacing of stirrups

$$s \geq \frac{A_v f_y d_v}{V_s} \cot \theta = 145 \text{ mm}$$

$$s \geq \frac{A_v f_y}{0.083\sqrt{f_c} b_v} = 687 \text{ mm}$$

$$V_u < 0.1f_c b_v d_v = 1195 \text{ kN Safe.}$$

providing 12 mm 2-legged stirrups 150 mm (at support)

12) Control of cracking:

Elastic -Cracked transformed section analysis required to check crack control (A5.7.3.4)

$$E_s = 200000 \text{ N/mm}$$

$$E_c = 26290.68276 \text{ N/mm}$$

$$n = E_s/E_c = 7.6$$

$$f \leq f_{sa} = \frac{Z}{(d_c A)^{1/3}}$$

$$Z = 30000 \text{ N/mm}$$

$$bx^2 + (m - 1)Asc(x - d) = mAst(d - x)$$

$$x = 235 \text{ mm}$$

$$I_{cr} = bx^3/3 + mAst(d - x)^2$$

$$I_{cr} = 1.E+11 \text{ mm}^4$$

The tensile stress in bottom steel becomes

$$f_s = n \left(\frac{M_y}{I_{cr}} \right)$$

$$f_s = 259.26 \text{ MPa}$$

$$f_{sa} = 544.93 \text{ MPa} > 0.6f_y$$

$$f_{sa} = 0.6f_y = 249 \text{ MPa} \quad | \quad f_s = 259.26 \text{ MPa}$$

Hence, here, $f_s \leq f_{sa}$, safe.

13) Deflection check:

i) Moment of inertia of Gross uncracked section without reinforcement:-

$$A_g = 996500 \text{ mm}^2$$

$$Y = 892 \text{ mm}$$

$$I_g = 2.66125E+11 \text{ mm}^4$$

$$y_t = 1500/2 = 750 \text{ mm}$$

$$f_{cr} = 3.45 \text{ N/mm}^2$$

$$M_r = 1224405534 \text{ Nmm}$$

$$M_r = 1224.4 \text{ kNm}$$

ii) Moment of inertia cracked section without reinforcement:-

$$E_s = 200000 \text{ N/mm}^2$$

$$E_c = 26290.68276 \text{ N/mm}^2$$

$$m = E_s/E_c = 7.61$$

$$x = 305 \text{ mm}$$

$$I_{cr} = 1.24692\text{E}+11 \text{ mm}^4$$

$$I_e = \left(\frac{M_{cr}}{M_a}\right)^3 I_g + \left[1 - \left(\frac{M_{cr}}{M_a}\right)^3\right] I_{cr} \leq I_g$$

$$I_{eff} = ((1163.64/3697.6)^3 * 2.529\bar{E} + 11) + ((1 - (1163.64/3697)^3) * 6.07\bar{E} + 10)$$

$$I_{eff} = 1.33374\text{E}+11 \text{ mm}^2 < I_{gr} \text{ ok}$$

$$EI = 3.4212\text{E}+15 \text{ Nmm}^2$$

$$\Delta_{D.L} = 21.2 \text{ mm} < 57\text{m}$$

$$\Delta_{D.L} = 3.13 \text{ mm} < 25\text{m}$$

5.4 Summary

Table 5.13: Flexure and collapse summary

		Collapse			
	Long. Girder	flexure		Shear	
		M.R of section	Actual M.R	S.F of section	Actual S.F
LSD (IS456:2000)	External	5980 kNm	6341kNm	1000kN	522kN
	Internal	4149 kNm	6093 kNm	704kN	477kN
LRFD (ASSTHO)	External	7789 kNm	8219.9 kNm	1075kN	1366kN
	Internal	4774 kNm	5148 kNm	832kN	1195.9kN

Table 5.14: Serviceability summary

		Serviceability			
	Long. Girder	Deflection		Cracking	
		Total deflection	Permissible	cracking width	Permissible
LSD (IS456:2000)	External	30mm	33mm	0.21mm	0.3mm
	Internal	31mm		0.25mm	
LRFD (ASSTHO)	External	26mm	33mm	173MPa	470MPa
	Internal	28mm		257MPa	517MPa

Chapter 6

Estimation of Quantity and cost

6.1 General

This chapter includes the methodology of estimation of cost for bridge Superstructure. The estimation of cost for any structure includes quantity analysis and rate analysis. The estimation of cost is necessary for selection of final design alternative amongst all the available various designs alternatives.

6.2 Quantity analysis

The quantity analysis is a schedule or list of quantities of all the possible items required for construction of any structure. These quantities are worked out by reading the drawing of the structure. Thus the quantity analysis indicates the amount of work to be done under each item, which when priced per unit of work gives the amount of cost of that particular item. It should be noted that the quantity analysis mentions all the items in the estimate. The quantity analysis does not give the list of materials required. The quantity analysis for problem in chapter 4 is given as under.

6.2.1 Estimation of concrete and wearing coat quantity

The total concrete quantity of 20m span, three girder bridge superstructure having 10 diaphragm and also estimated total quantity of wearing surface.

Table 6.1: Concrete and wearing coat quantity

Description	Quantity	unit
Slab	34.3	m ³
Girder	32	m ³
Diaphragm	8	m ³
Total concrete	74.3	m ³
Wearing coat	23.265	ton

6.2.2 Estimation of steel quantity

6.2.3 Rate analysis

In order to determine the rate of a particular item, the factors affecting the rate of that item are studied carefully and then finally a rate is decided for that item. With the use of that rate and estimated quantity the total tentative cost of the Whole structure can be obtained. For cost estimate rate analysis of concrete is worked out wherein the rates of cement and other ingredients are considered based on current market rates. The rates of structural as well as high tensile steel are based on current market rates.

The following current market rates:

Concrete = 5116 Rs/m³ (including scaffolding, shuttering,labour)

Steel = 40 Rs/kg

Wearing coat = 4000 Rs/kg

6.2.4 Total cost

Description	Quantity	Rate	Unit	Cost(Rs)
Slab concrete	34	5116	<i>Rs/m³</i>	175479
Slab R/F	3963	40	<i>Rs/kg</i>	158504
Girder concrete	40	5116	<i>Rs/m³</i>	203339
Girder R/F	16284	40	<i>Rs/kg</i>	16284
Wearing coat	23	4000	<i>Rs/tonne</i>	93060
Total cost				1123218

6.2.5 Summary

Estimation of different items like , concrete including (shuttering and scaffolding), reinforcement of deck slab and girder is carried out. For rate analysis, rate considered as a current market rate. After estimation and costing it is found that total cost of bridge superstructure for 20m span with L/D ratio 13 is 1123218 Rs.

Chapter 7

Parametric Study

7.1 General

The various span to depth ratio, design alternatives are required to be evaluated for quantity and costing of the superstructure to arrive at effective economical span to depth ratio. To obtain the most effective span to depth ratio parametric study was done for 15m, 20m and 25m span by taking various depths for various L/D ratios. Total 9 cases for different spans of various L/D ratios with three depths are discussed in this chapter.

7.2 Section at various depth

The forces calculated and summary of design quantity trials shown in this chapter is based on various L/D ratios at three various depths and the R.C.C bridge cross section is as shown in fig 7.1 for a span of 15m, 20m and 25m.

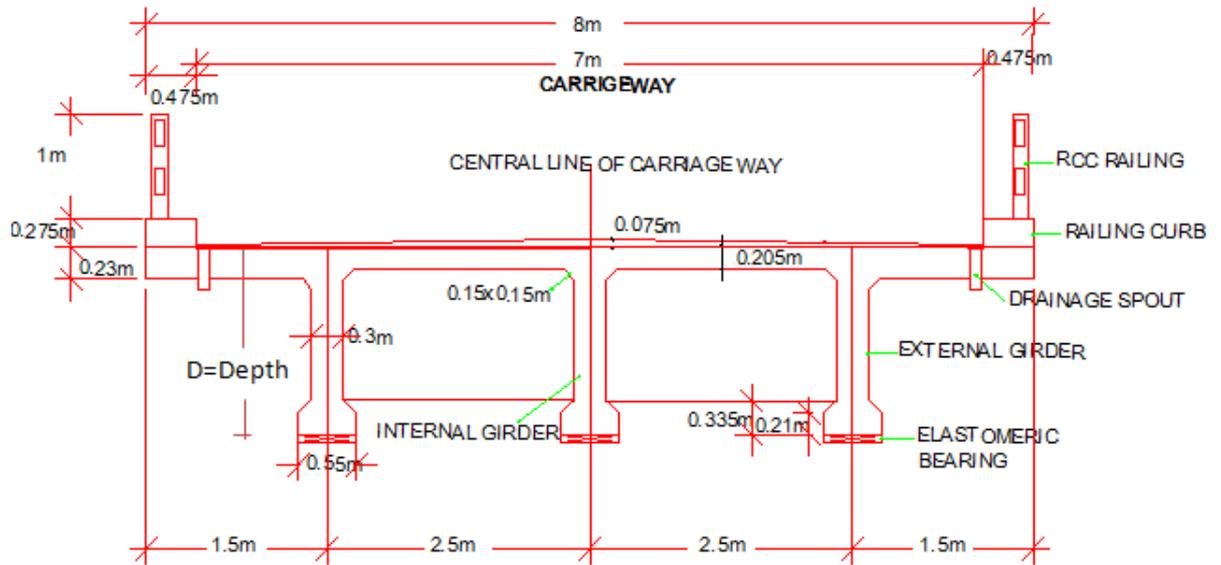


Figure 7.1: Cross Section of Bridge Deck Slab

Material of girder is with $f_c k = M30$, $f_y = Fe415$.

D= Trial Depth of girder	1.1m	1.5m	1.9m
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7.3 Results

The analysis was done in SAP software. The maximum Bending moment and shear force at different three depths for 15m, 20m and 25m with different L/D ratio alternatives are tabulated in table 7.1 and 7.2. Corresponding graphical variations are also shown in Fig. 7.2, Fig. 7.3, Fig. 7.4 and Fig. 7.5.

Table 7.1: Maximum bending moment in girder

Span (m)	Depth (m)	L/D ratio	External girder(kNm)		Internal girder(kNm)	
			Unfactored Moment	Factored Moment	Unfactored Moment	Factored Moment
15	1.1	14	3274	4951	2232	3411
	1.5	10	3373	4951	2352	3411
	1.9	8	3475	5089	2473	3575
20	1.1	18	4397	6434	2877	4289
	1.5	13	4595	6434	2877	4630
	1.9	11	4728	6880	3104	4953
25	1.1	23	5620	8183	4267	6136
	1.5	17	5891	8549	4581	6561
	1.9	13	6158	8910	4898	6989

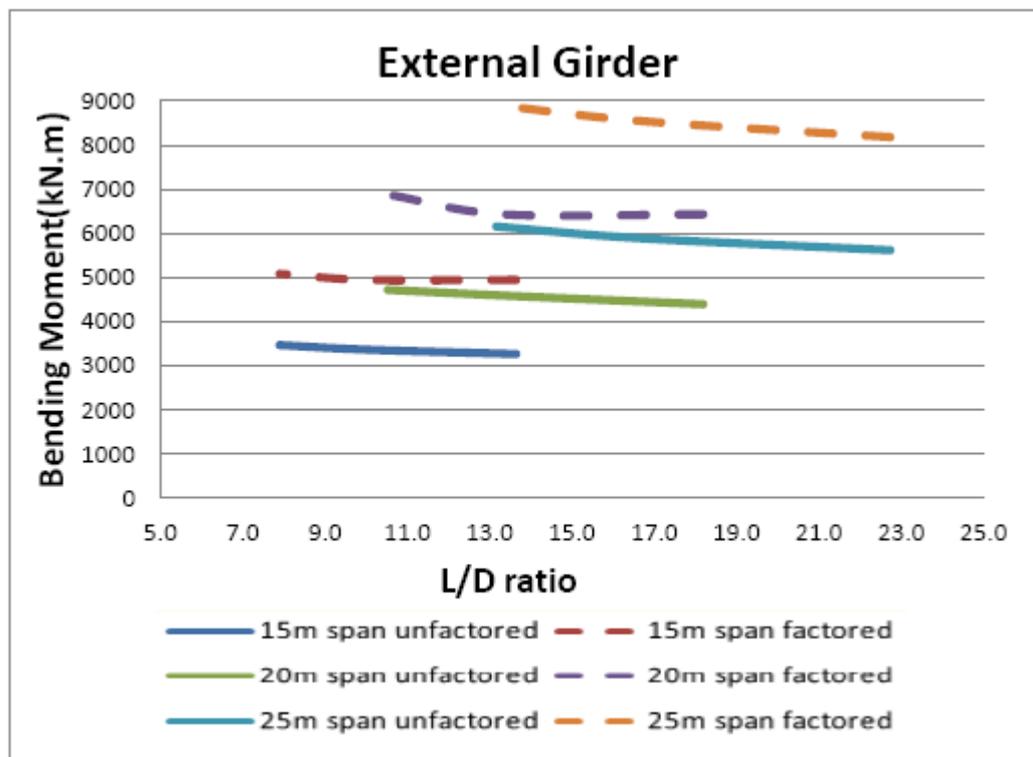


Figure 7.2: Bending moment variation in external girder along various L/D ratio

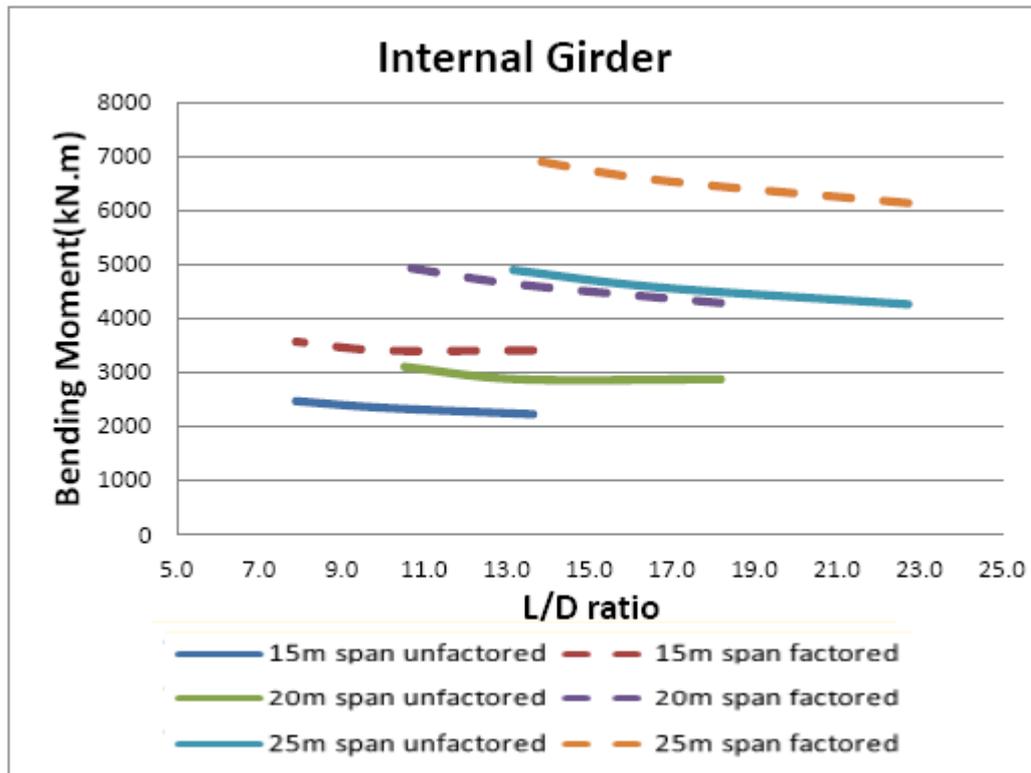


Figure 7.3: Bending moment variation in internal girder along various L/D ratio

Table 7.2: Maximum shear force in girder

Span (m)	Depth (m)	L/D ratio	External girder(kN)		Internal girder(kN)	
			Unfactored force	Factored force	Unfactored force	Factored force
15	1.1	14	518	759	325	476
	1.5	10	543	793	449	644
	1.9	8	569	828	480	685
20	1.1	18	681	1000	489	729
	1.5	13	723	1057	557	830
	1.9	11	758	1104	557	830
25	1.1	23	675	984	596	853
	1.5	17	718	1042	646	919
	1.9	13	760	1099	695	986

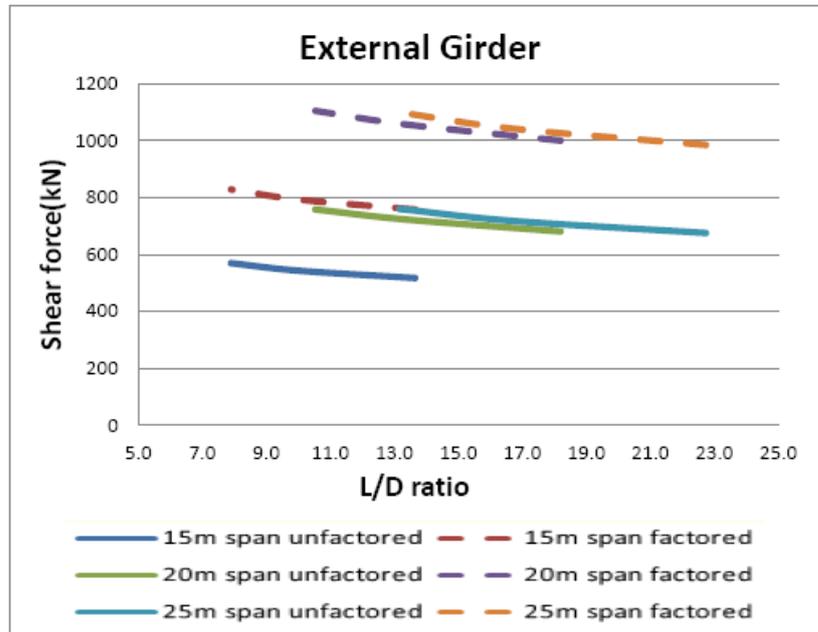


Figure 7.4: Shear force variation in external girder along various L/D ratio

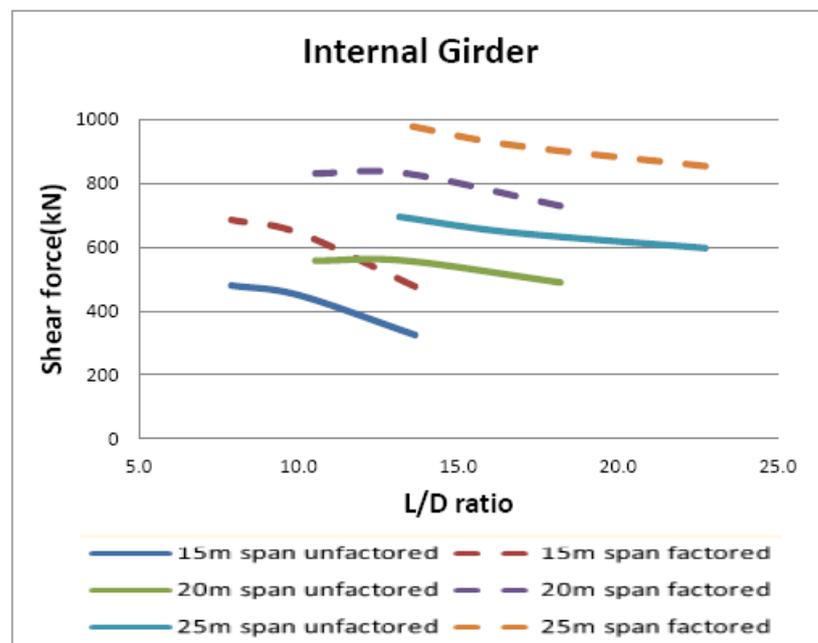


Figure 7.5: Shear force variation in internal girder along various L/D ratio

7.4 Results of costing

The design was done by prepared spreadsheet. The overall analysis methodology and step by step design procedure is described in chapter 5. For all the various spans and span to depth ratio deck slab and structural composite longitudinal girder is designed. For all various spans and depth slab and longitudinal girder designed. Initially the depth of longitudinal girder is selected on trial bases to study the behavior of of span 15m, 20m and 25m with three different depth 1.1m ,1.5m and 1.9m. Fig 7.6, 7.7 and 7.8 shows the concrete cost, slab reinforcement cost, wearing coat cost and girder reinforcement Cost for 15m, 20m and 25m respectively.

With different L/D ratio. Table 7.3, 7.4 and 7.5 shows that the slab concrete, slab reinforcement and wearing coat cost does not affects the L/D ratio . From the Fig 7.6, 7.7 and 7.8 it is clear that total cost of super structure is mainly affected by girder reinforcement and concrete cost. It is commonly observed that as the depth increases the cost of concrete increases. From table 7.3 observed that as the girder depth increases the steel cost decreases and from table 7.4 as the depth increases steel cost first increases, decrease then again increases. L/D ratio 10 is most economical L/D ratio for 15m span 13 L/D ratio for 20m and 25m span among all L/D ratio alternatives. From table 7.4 L/D ratio beyond 17 is uneconomical and structure is even not safe in deflection and cracking.

Table 7.3: Variation of total cost of material for 15m span with varous L/D ratio

Span =15m					
Depth			1.1	1.5	1.9
L/D			14	10	8
Slab Concrete	Quant.	m3	26	26	26
	Cost	Rs	133016	133016	133016
Slab Reinforcement	Quant.	m2	3004	3004	3004
	Cost	Rs	120155	120155	120155
Girder Concrete	Quant.	m3	23	31	39
	Cost	Rs	119808	159283	198758
Girder Reinforcement	Quant.	kg	12198	11222	11291
	Cost	Rs	487921	448896	451647
Wearing coat	Quant.	tonne	17	17	17
	Cost	Rs	69795	69795	69795
Total Cost		Rs	103869	944369	973372

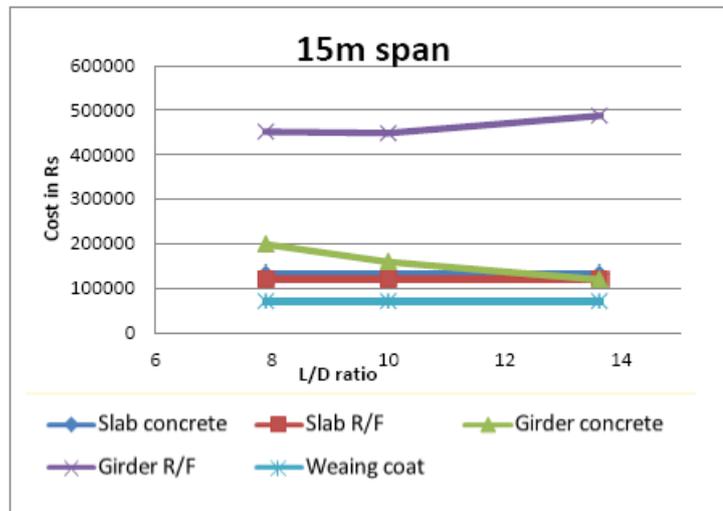


Figure 7.6: Variation of total cost of material for 15m span with varous L/D ratio

Table 7.4: Variation of total cost of material for 20m span with varous L/D ratio

Span =20m					
Depth			1.1	1.5	1.9
L/D			18	13	11
Slab Concrete	Quant.	m3	34	34	34
	Cost	Rs	175479	175479	175479
Slab Reinforcement	Quant.	m2	3963	3963	3963
	Cost	Rs	158504	158504	158504
Girder Concrete	Quant.	m3	30	40	50
	Cost	Rs	152404	203339	255800
Girder Reinforcement	Quant.	kg	16999	16284	17589
	Cost	Rs	679974	651341	703540
Wearing coat	Quant.	tonne	23	23	23
	Cost	Rs	93060	93060	93060
Total Cost		Rs	1259421	1123218	1386383

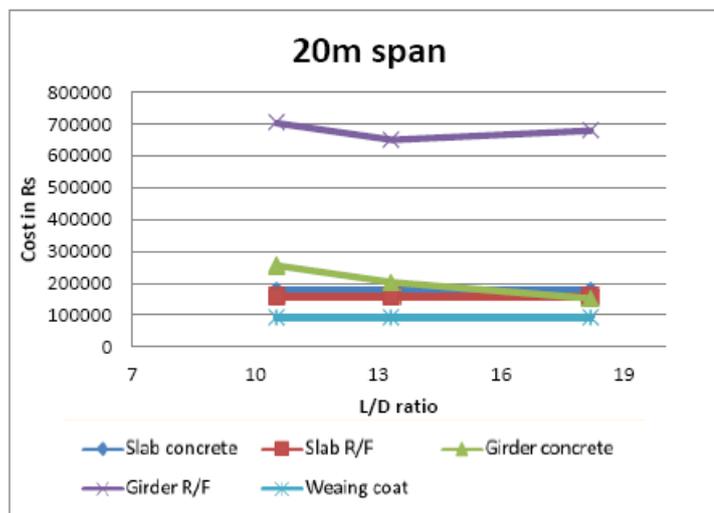


Figure 7.7: Variation of total cost of material for 20m span with various L/D ratio

Table 7.5: Variation of total cost of material for 25m span with varous L/D ratio

Span =25m					
Depth			1.1	1.5	1.9
L/D			23	17	13
Slab Concrete	Quant.	m3	43	43	43
	Cost	Rs	219349	219349	219349
Slab Reinforcement	Quant.	m2	4921	4921	4921
	Cost	Rs	196852	196852	196852
Girder Concrete	Quant.	m3	35	46	58
	Cost	Rs	176656	235695	294733
Girder Reinforcement	Quant.	kg	19864	18333	16208
	Cost	Rs	794558	733331	648336
Wearing coat	Quant.	tonne	29	29	29
	Cost	Rs	116325	116320	116320
Total Cost		Rs	1503741	1501547	1475590

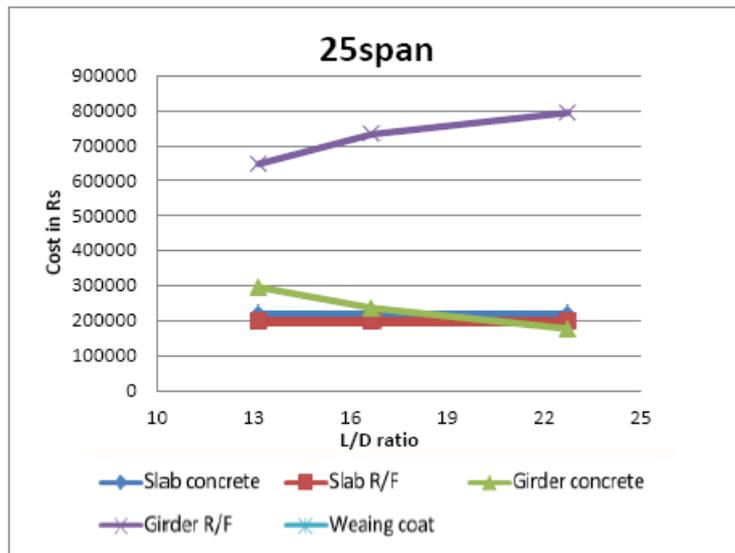


Figure 7.8: Variation of total cost of material for 25m span with varous L/D ratio

Table 7.6: Total cost of 15m, 20m and 25m span

Span	L/D Ratio	Total Cost (Rs)
15	14	1038694
	10	944369
	8	973372
20	18	1259421
	13	1123218
	11	1386383
25	23	1503741
	17	1501547
	13	1475590
	11	1551547

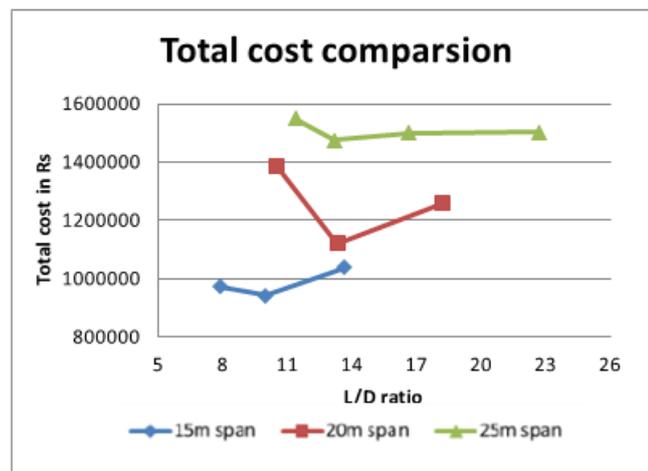


Figure 7.9: Total cost of material for 15m,20m and 25m span with varous L/D ratio

7.5 Total cost comparison of design method

Tables 7.7 shows total cost of concrete, reinforcement and wearing coat for working stress design(WSM), limit state design(LSM) and load and resistance design methods(LRFD) for 20m spans and 13 L/D ratio.It is found that the limit state method

design were 7 percent costlier than working stress method design whereas LRFD is 11% high than the LSD.

Table 7.7: Total cost of comparison of WSD,LSD and LRFD

	Concrete	Reinforcement	Wearing coat	Total cost(Rs)
WSD	393932	692600	93060.0	1179592.0
LSD	378584	809845	93060.0	1281529.0
LRFD	419512	933880	93060.0	1446452.0

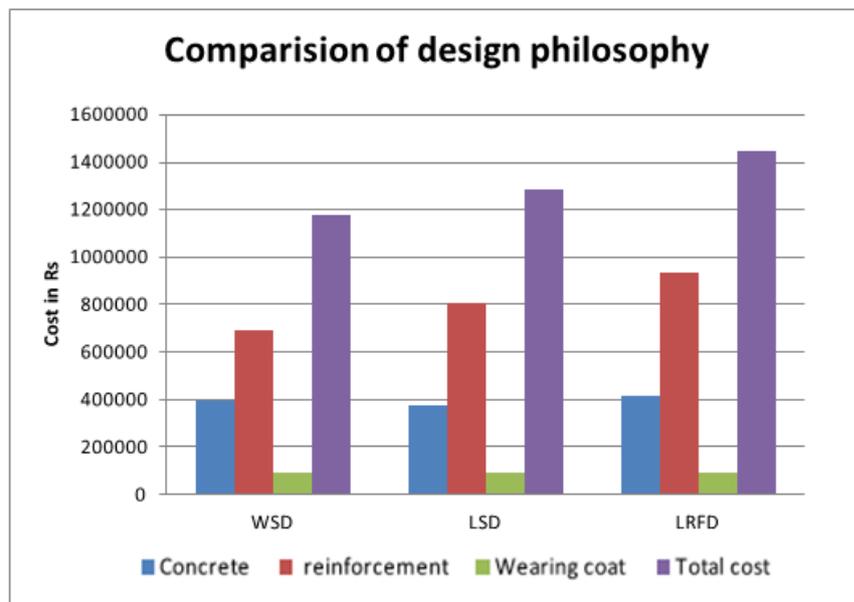


Figure 7.10: Total cost of material for 15m,20m and 25m span with various L/D ratio

7.6 Summary

Parametric study is carried out to find out the effective economical L/D ratio for 15m, 20m and 25m. It is found that L/D ratio 10, 13 and 13 are most economical L/D ratio for 15m, 20m and 25m spans respectively. Cost comparison between WSD design LSM design and LRFD design is carried out for economical L/D ratio 13 for

20m span. It is found that the LSD design were 7 percent costlier than WSD method whereas LRFD is 11% high than the LSD.

Chapter 8

Summary and Conclusion

8.1 Summary

The main objective of the work is to study the design philosophy in the R.C. fly-over bridge superstructures design of slab and girder and to find out the economical span to depth ratio for 15m, 20m and 25m span. R.C. Flyover Bridge is analysed using SAP2000 civil software. Excel spread sheets are prepared for deck slab design, longitudinal girder design as per IS 456:2000 and ASSTHO specification. In dead load self-weight of girder, slab, wearing coat and parapet load considered. And in live load Class-A and Class 70R IRC loading are considered. Total 9 alternatives are done using prepared spread sheet. R.C. girder is designed to satisfy moment capacity check, deflection check and crack check. And costs of all alternatives are carried out for various economical span and l/d ratio safe span to depth ratio.

For 15m span economical l/d ratio is 10, 20m span economical l/d ratio is 13 and for 25m span 13 l/d ratio is economical. Design of 20m span is carried out by limit state design using IS-456:2000 and LRFD using ASSTHO specification.

8.2 Conclusion

- Maximum live load moment is carried out when the two class 70R IRC loading moving at a time on two lanes.
- The various limit state of flexure, shear, deflection and cracking is verified as per IS:456 code and the design is found satisfying all limit state.
- The design is carried out with ASSTHO specifications and it is found to be satisfactory in limit state of flexure, shear, deflection and cracking control criteria.
- The quantities and the total cost are compared for both the design and found that LRFD total cost 11% more than the LSD design.
- The parametric study is carried out to find the most economical (minimum cost) L/D ratio for span 15m,20m and 25m with L/D ratio as shown in table 7.3 ,7.4 and 7.5.
- It is observed from parametric study that for 15m span economical L/D ratio is 10, while for 20m and 25m span it remain same and equal to 13.

8.3 Future Scope

- To study of superstructure design as per limit state method can be further carried out with boxgirder section.

- To study of superstructure design as per limit state method can be further carried out with rectangular and trapezoidal shape of composite box girder.
- Increasing the number of girders the study can be further carried out for optimum number of girders.

Appendix A

Detailing sheet

- Detailing drawing of R.C.C deck slab.
- Detailing drawing of R.C.C longitudinal girder.
- Detailing drawing of R.C.C Diaphragm.

Appendix B

Paper communicated

- Sweta ojha and N.C.Vyas,Limit State Design Approach for Bridge Superstructure,*Dr.S.N.Patel's seminar for structural engineering students,B.V.M Engineering College,Vallabh Vidhyanagar, 7 January 2010,*

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